

A new view on charge and color Breaking minima in the MSSM

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DISCLAIMER: No $\gamma\gamma$ excess!

MSSM may be ruled out anyway. . .

. . . or not? (cf. Djouadi's talk?)



Brout–Englert–Higgs mechanism

$$SU(3)_c \times SU(2)_L \times U(1)_Y \rightarrow SU(3)_c \times U(1)_{em}$$

Consequence: The (in)famous Higgs boson!

- scalar mass sensitive to high scale physics (hierarchy problem)
- Standard Model vacuum metastable (will eventually decay)
[Degrassi et al. 2012]
- its mass could not be predicted (in the SM)

A viable solution / extension of the SM

- The Minimal Supersymmetric Standard Model (MSSM)
- “predicts” the Higgs mass; defines Higgs potential
- solves the hierarchy problem
- stabilizes the potential

The Minimal Supersymmetric Standard Model: A multi-scalar theory

with

$$V = V_F + V_D + V_{\text{soft}}$$

$$V_F = \sum_i \left| \frac{\partial \mathcal{W}}{\partial \phi_i} \right|^2,$$

$$V_D = \frac{1}{2} \sum_a g_a^2 \left(\sum_i \phi_i^\dagger T^a \phi_i \right)^2$$

$$V_{\text{soft}} = \sum_i m_{\phi_i}^2 |\phi_i|^2 + \sum_{ijk} A_{ik}^{(j)} \phi_i^\dagger \phi_j \phi_k$$

$$\leftrightarrow$$

The Standard Model: A single scalar theory

$$V_{\text{SM}} = -\mu^2 H^\dagger H + \frac{\lambda}{4} (H^\dagger H)^2$$

A multi-scalar theory

- 2 Higgs doublets
- 2×6 scalar quarks, $6 + 3$ scalar leptons
- 12 colored and $18 + 2$ charged directions
- charged Higgs directions “safe”
- SM Higgs potential: $SO(4)$ symmetry

[Casas et al. 1996]

The hazard

- impossible to minimize directly, analytically
- colored directions sensitive to all kinds of SUSY breaking
- spontaneous breaking of color charge: $\langle \tilde{q} \rangle \neq 0$

The true vacuum

- effective potential: average energy density
- global minimum: true ground state of the theory

The third generation MSSM

$$\mathcal{W} = \mu H_1 \cdot H_2 + y_t H_2 \cdot Q_L \bar{T}_R - y_b H_1 \cdot Q_L \bar{B}_R$$

- large couplings to Higgs doublets (y_t and y_b comparably large)
- large stop contribution (X_t, A_t) to light Higgs mass needed
- $\tan \beta$ resummation for m_b influences y_b

Properties of the (effective) scalar potential

- no UFB directions (due to quantum corrections)
- D -terms: (comparably) large contributions ϕ^4
- “dangerous” directions: small quadrilinears + large trilinears

Analytic constraints

- define certain directions in field space: great simplification
- e.g. D -terms absent: $|\tilde{Q}_L| = |\tilde{t}_R| = |h_2|$ (possibly miss sth.)

$$\begin{aligned}
 V_{\tilde{q},h} = & \tilde{t}_L^* (\tilde{m}_L^2 + |y_t h_2|^2) \tilde{t}_L + \tilde{t}_R^* (\tilde{m}_t^2 + |y_t h_2|^2) \tilde{t}_R \\
 & + \tilde{b}_L^* (\tilde{m}_L^2 + |y_b h_1|^2) \tilde{b}_L + \tilde{b}_R^* (\tilde{m}_b^2 + |y_b h_1|^2) \tilde{b}_R \\
 & - [\tilde{t}_L^* (\mu^* y_t h_1^* - A_t h_2) \tilde{t}_R + \text{h.c.}] \\
 & - [\tilde{b}_L^* (\mu^* y_b h_2^* - A_b h_1) \tilde{b}_R + \text{h.c.}] \\
 & + |y_t|^2 |\tilde{t}_L|^2 |\tilde{t}_R|^2 + |y_b|^2 |\tilde{b}_L|^2 |\tilde{b}_R|^2 \\
 & + \frac{g_1^2}{8} \left(|h_2|^2 - |h_1|^2 + \frac{1}{3} |\tilde{b}_L|^2 + \frac{2}{3} |\tilde{b}_R|^2 + \frac{1}{3} |\tilde{t}_L|^2 - \frac{4}{3} |\tilde{t}_R|^2 \right)^2 \\
 & + \frac{g_2^2}{8} \left(|h_2|^2 - |h_1|^2 + |\tilde{b}_L|^2 - |\tilde{t}_L|^2 \right)^2 \\
 & + \frac{g_3^2}{8} \left(|\tilde{t}_L|^2 - |\tilde{t}_R|^2 + |\tilde{b}_L|^2 - |\tilde{b}_R|^2 \right)^2 \\
 & + (m_{h_2}^2 + |\mu|^2) |h_2|^2 + (m_{h_1}^2 + |\mu|^2) |h_1|^2 - 2 \text{Re}(B_\mu h_1 h_2).
 \end{aligned}$$

The tree-level scalar potential

$$\begin{aligned}
 V_{\tilde{q},h} = & \tilde{t}_L^* (\tilde{m}_L^2 + |y_t h_2|^2) \tilde{t}_L + \tilde{t}_R^* (\tilde{m}_t^2 + |y_t h_2|^2) \tilde{t}_R \\
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 & - [\tilde{b}_L^* (\mu^* y_b h_2^* - A_b h_1) \tilde{b}_R + \text{h.c.}] \\
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$$|\tilde{t}_L| = |\tilde{t}_R| = |\tilde{t}|, \quad |\tilde{b}_L| = |\tilde{b}_R| = |\tilde{b}|$$

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 & + |y_t|^2 |\tilde{t}|^2 |\tilde{t}|^2 + |y_b|^2 |\tilde{b}|^2 |\tilde{b}|^2 \\
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$$|\tilde{t}_L| = |\tilde{t}_R| = |\tilde{t}|, |\tilde{b}_L| = |\tilde{b}_R| = |\tilde{b}|; |\tilde{b}| = |h_1| = |\phi_1|, |\tilde{t}| = |h_2| = |\phi_2|$$

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 V_{\tilde{q},h} = & \phi_2^* (\tilde{m}_L^2 + |y_t \phi_2|^2) \phi_2 + \phi_2^* (\tilde{m}_t^2 + |y_t \phi_2|^2) \phi_2 \\
 & + \phi_1^* (\tilde{m}_L^2 + |y_b \phi_1|^2) \phi_1 + \phi_1^* (\tilde{m}_b^2 + |y_b \phi_1|^2) \phi_1 \\
 & - [\phi_2^* (\mu^* y_t \phi_1^* - A_t \phi_2) \phi_2 + \text{h.c.}] \\
 & - [\phi_1^* (\mu^* y_b \phi_2^* - A_b \phi_1) \phi_1 + \text{h.c.}] \\
 & + |y_t|^2 |\phi_2|^2 |\phi_2|^2 + |y_b|^2 |\phi_1|^2 |\phi_1|^2 \\
 & + (m_{h_2}^2 + |\mu|^2) |\phi_2|^2 + (m_{h_1}^2 + |\mu|^2) |\phi_1|^2 - 2 \text{Re}(B_\mu \phi_1 \phi_2).
 \end{aligned}$$

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The tree-level scalar potential

$$V_{\tilde{q},h} = \phi_2^* (\tilde{m}_L^2 + |y_t \phi_2|^2) \phi_2 + \phi_2^* (\tilde{m}_t^2 + |y_t \phi_2|^2) \phi_2$$

$$- [\phi_2^* (\quad - A_t \phi_2) \phi_2 + \text{h.c.}]$$

$$+ |y_t|^2 |\phi_2|^2 |\phi_2|^2$$

$$+ (m_{h_2}^2 + |\mu|^2) |\phi_2|^2$$

$$|\tilde{t}_L| = |\tilde{t}_R| = |\tilde{t}|, |\tilde{b}_L| = |\tilde{b}_R| = |\tilde{b}|; \quad \cancel{|\tilde{b}| = |h_1| = |\phi_1|}, |\tilde{t}| = |h_2| = |\phi_2|$$

Minimize the potential

$$V(\phi) = m^2\phi^2 - A\phi^3 + \lambda\phi^4,$$

with $m^2 = m_{h_2}^2 + |\mu|^2 + \tilde{m}_L^2 + \tilde{m}_t^2$, $A = -A_t$ and $\lambda = 3y_t^2$.

Minimize the potential

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Answer:

$$\phi_0 = 0, \quad \phi_{\pm} = \frac{3A \pm \sqrt{9A^2 - 32\lambda m^2}}{8\lambda}.$$

Condition to be safe from non-standard (i.e. non-trivial) minima:

$$V(\phi_{\pm}) > 0 \quad \Leftrightarrow \quad m^2 > \frac{A^2}{4\lambda}$$

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Well-known constraints

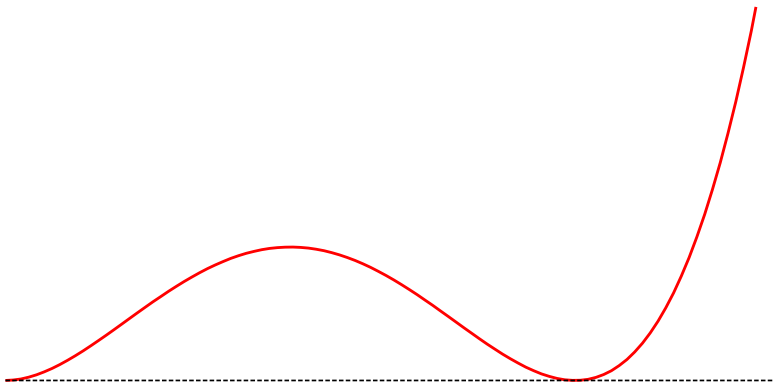
[Gunion, Haber, Sher '88]

$$|A_t|^2 < 3y_t^2 (m_{h_2}^2 + |\mu|^2 + \tilde{m}_L^2 + \tilde{m}_t^2)$$

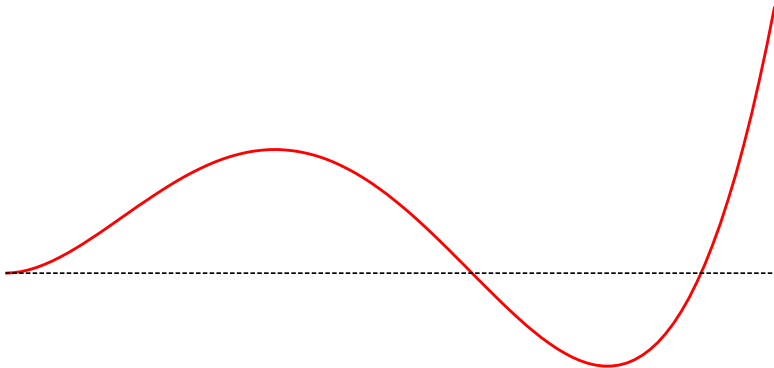
$$|A_b|^2 < 3y_b^2 (m_{h_1}^2 + |\mu|^2 + \tilde{m}_L^2 + \tilde{m}_b^2)$$

for the limiting cases $|\tilde{t}_L| = |\tilde{t}_R| = |h_2|$ and $|\tilde{b}_L| = |\tilde{b}_R| = |h_1|$!

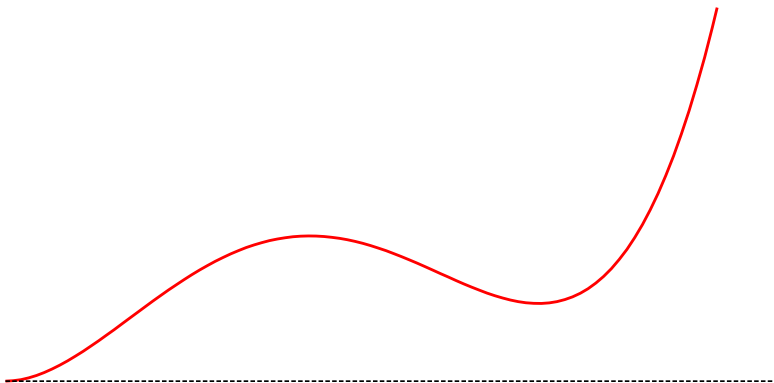
$$A^2 = 4\lambda m^2$$



$$A^2 > 4\lambda m^2$$



$$A^2 < 4\lambda m^2$$



Problem already known for a while

- problem noticed [Frere, Jones, Raby '83]
- “ A -parameter bounds” [Gunion, Haber, Sher '87]
- classification of all dangerous directions [Casas, Lleyda, Muñoz '96]
- including flavor violation [Casas and Dimopoulos '96]

Stability \neq no Instability \Rightarrow Metastability

Vacuum tunneling [Kusenko, Langacker '96; Blinov, Morissey '13]

The tool

VeVacious [Camargo-Molina, O'Leary, Porod, Staub '13]

- finds all (?) tree-level minima
- minimizes scalar potential in the vicinity at one loop
- calculates bounce action / tunneling times [CosmoTransitions]

What has changed since the mid 90s?

- 1 We have discovered the Higgs!
- 2 No sign of SUSY so far...
- 3 $m_h = 125 \text{ GeV}$
(all SUSY literature during LEP era expected it to be $\lesssim 100 \text{ GeV}$)
- 4 Consequently: large radiative corrections!
- 5 large stop mixing needed? heavy SUSY spectrum?
(or hidden in some hardly accessible valley)
- 6 approach today:
 - less focused on unified models
 - still certain scenarios
 - $\tan \beta$ resummation for bottom quark mass (large $\tan \beta$)
 - low $\tan \beta$ favored (for $M_A \lesssim 800 \text{ GeV}$, direct search $A \rightarrow \tau\tau$)

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Semi-analytical bounds/exclusions important for fast processing!

My “pMSSM”

- no unification (more than m_0 , $m_{1/2}$, A_0 , $\tan \beta$ and $\text{sign } \mu$)
- free parameters: (although similar choice as in CMSSM)
 - $\tilde{m}_L^2 = \tilde{m}_t^2 = \tilde{m}_b^2 = M_{\text{SUSY}}^2$
 - μ , $\tan \beta$
 - A_t , A_b (not necessarily equal)
- $m_{h_{1,2}}^2$ determined from ew breaking, B_μ related to M_A
- no RG running needed = parameters taken at the SUSY scale

Why no RG-improvement?

- SUSY scale parameters; limits on this parameters
- destabilization of ew vacuum *around* SUSY scale
- no Planck scale vevs! (maybe there are... in addition)
- in the spirit of the pMSSM as phenomenologically as possible
- only small RG modifications, qualitative features unchanged

Less constraints, more parameters, more fields, more vevs. . .

Restriction to certain directions too restrictive!

- give up $|\tilde{q}_L| = |\tilde{t}_R| = |h_2|$
- allow for $h_1 \neq 0$ and $\tilde{b} \neq 0$
- “break” $\tilde{q}_L \rightarrow \tilde{t}_L + \tilde{b}_L$
- back to full scalar potential!

Simplify your life

- $h_2 = \phi$
- $|\tilde{t}_L| = |\tilde{t}_R| = |\tilde{t}| = \alpha|\phi|$
- $h_1 = \eta\phi$
- $|\tilde{b}_L| = |\tilde{b}_R| = |\tilde{b}| = \beta|\phi|$
- all fields and parameters real, $\alpha, \beta > 0$, $\eta \in \mathbb{R}$
- $SU(3)_c$ -flatness: $\tilde{t}_L = \tilde{t}_R$ and $\tilde{b}_L = \tilde{b}_R$

A simple view of a complicated object

$$h_2 = \phi, \quad |\tilde{t}| = \alpha|\phi|, \quad h_1 = \eta\phi, \quad |\tilde{b}| = \beta|\phi|$$

$$\begin{aligned} V_\phi &= (m_{h_2}^2 + \eta^2 m_{h_1}^2 + (1 + \eta^2)\mu^2 - 2B_\mu\eta \\ &\quad + (\alpha^2 + \beta^2)\tilde{m}_L^2 + \alpha^2\tilde{m}_t^2 + \beta^2\tilde{m}_b^2)\phi^2 \\ &\quad - 2(\alpha^2(\mu y_t \eta - A_t) + \beta^2(\mu y_t - \eta A_b))\phi^3 + (\alpha^2 y_t^2 + \beta^4 y_b^2)\phi^4 \\ &\quad + \left(\frac{g_1^2 + g_2^2}{8} (1 - \eta^2 + \beta^2 - \alpha^2)^2 + 2\alpha^2 y_t^2 + 2\beta^2 y_b^2 \right) \phi^4 \\ &\equiv M^2(\eta, \alpha, \beta)\phi^2 - \mathcal{A}(\eta, \alpha, \beta)\phi^3 + \lambda(\eta, \alpha, \beta)\phi^4, \end{aligned}$$

with

$$\begin{aligned} M^2 &= m_{h_2}^2 + \eta^2 m_{h_1}^2 + (1 + \eta^2)\mu^2 - 2B_\mu\eta \\ &\quad + (\alpha^2 + \beta^2)\tilde{m}_L^2 + \alpha^2\tilde{m}_t^2 + \beta^2\tilde{m}_b^2, \end{aligned}$$

$$\mathcal{A} = 2\alpha^2\eta\mu y_t - 2\alpha^2 A_t + 2\beta^2\mu y_b - 2\eta\beta^2 A_b,$$

$$\begin{aligned} \lambda &= \frac{g_1^2 + g_2^2}{8} (1 - \eta^2 + \beta^2 - \alpha^2)^2 \\ &\quad + (2 + \alpha^2)\alpha^2 y_t^2 + (2\eta^2 + \beta^2)\beta^2 y_b^2. \end{aligned}$$

[Gunion, Haber, Sher '88; Casas, Lleyda, Muñoz '96]

The same but different (“ A -parameter bounds”)

$$\mathcal{A}^2 < 4\lambda M^2$$

$$\downarrow$$

$$4 \min_{\{\eta, \alpha, \beta\}} \lambda(\eta, \alpha, \beta) M^2(\eta, \alpha, \beta) > \max_{\{\eta, \alpha, \beta\}} (\mathcal{A}(\eta, \alpha, \beta))^2$$

$$h_u = \tilde{b}, h_d^0 = 0$$

[WGH'15]

$$m_{H_u}^2 + \mu^2 + \tilde{m}_Q^2 + \tilde{m}_b^2 > \frac{(\mu y_b)^2}{y_b^2 + (g_1^2 + g_2^2)/2}$$

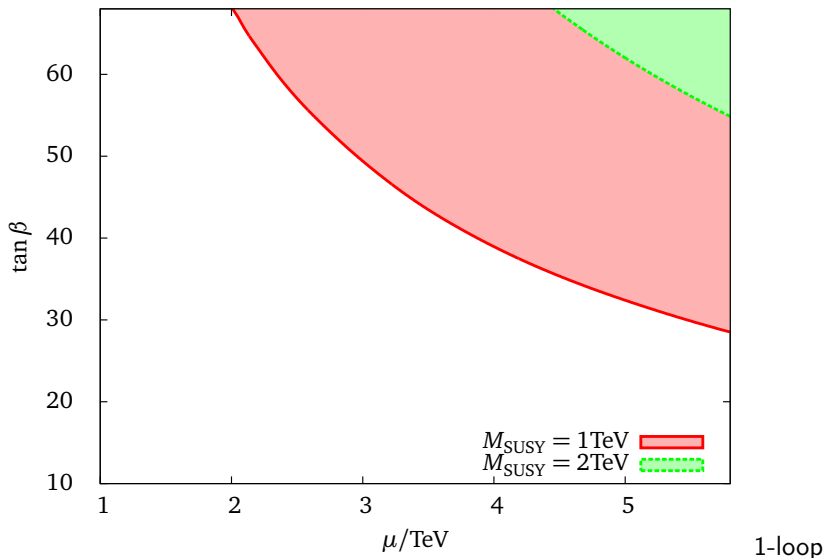
$$|h_d|^2 = |h_u|^2 + |\tilde{b}|^2, \tilde{b} = \alpha h_u$$

[WGH'15]

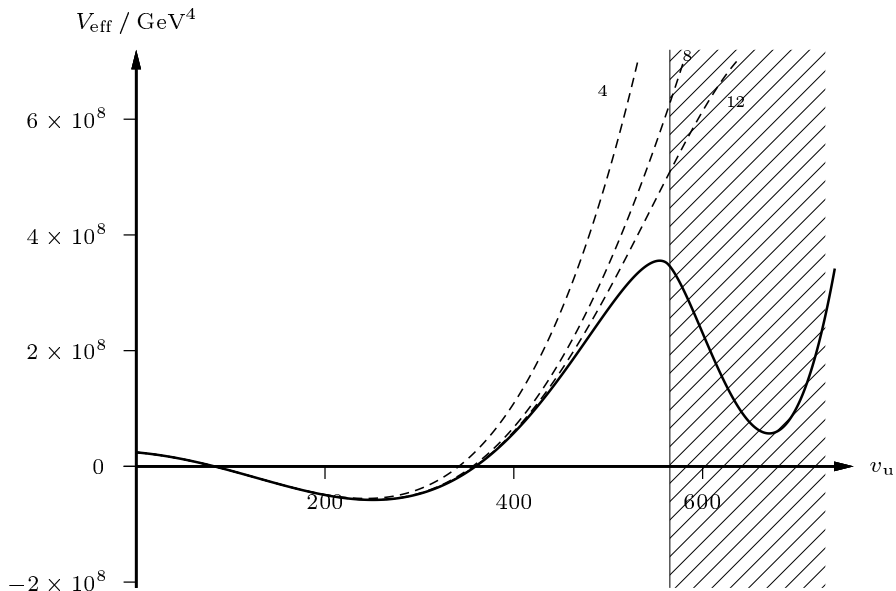
$$m_{11}^2(1 + \alpha^2) + m_{22}^2 \pm 2m_{12}^2 \sqrt{1 + \alpha^2} + \alpha^2(\tilde{m}_Q^2 + \tilde{m}_b^2) > \frac{4\mu^2 \alpha^2}{2 + 3\alpha^2}$$

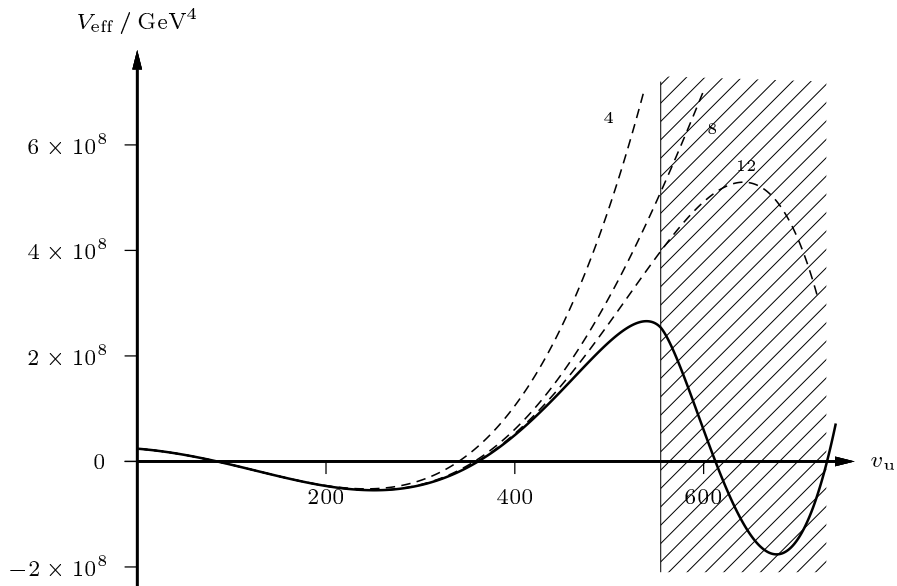
Illustrating the exclusion limits

[Bobrowski, Chalons, WGH, Nierste '14]

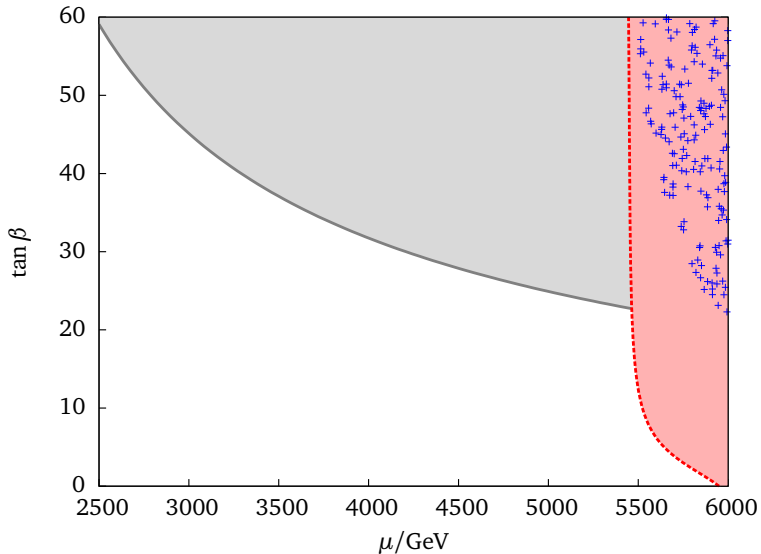


Higgs potential (h_u and h_d), new CC conserving min @ 1-loop



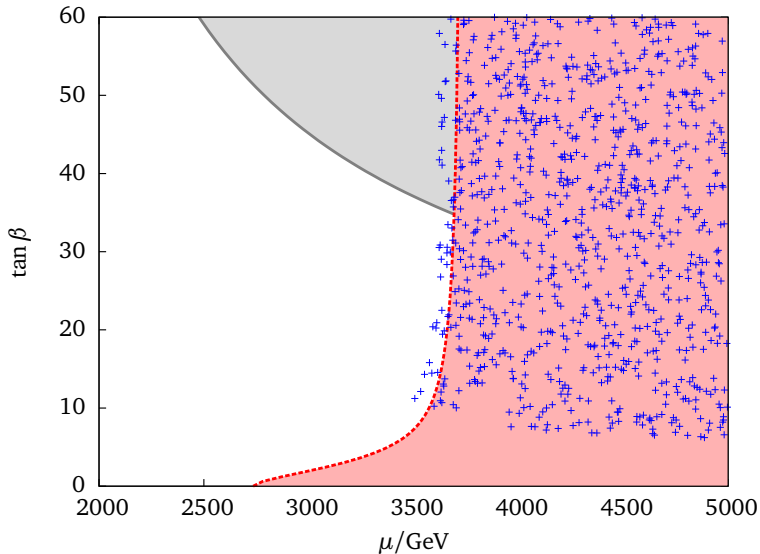


[WGH: PLB752 7 (2016)]



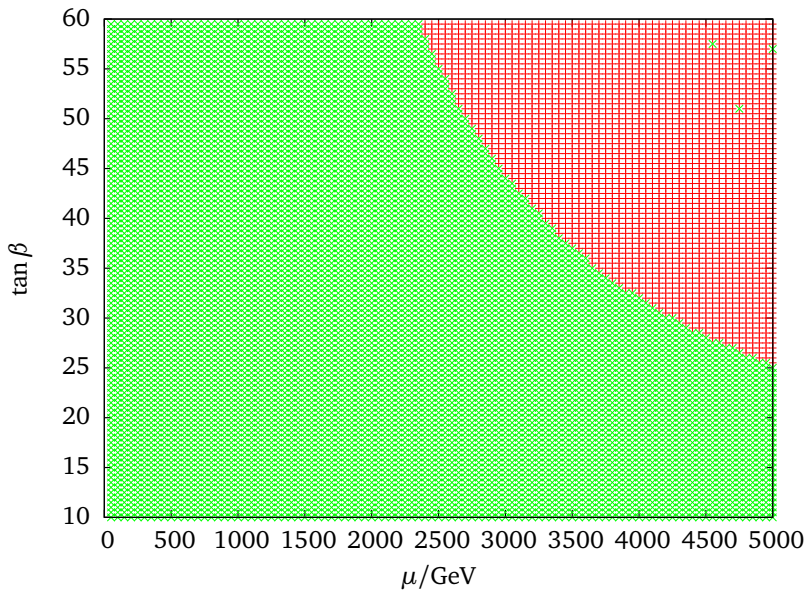
$$\text{CCB sbottom vev, } h_d = -\sqrt{|h_u|^2 + |\tilde{b}|^2}$$

[WGH: PLB752 7 (2016)]


 CCB sbottom vev, $h_d = +\sqrt{|h_u|^2 + |\tilde{b}|^2}$

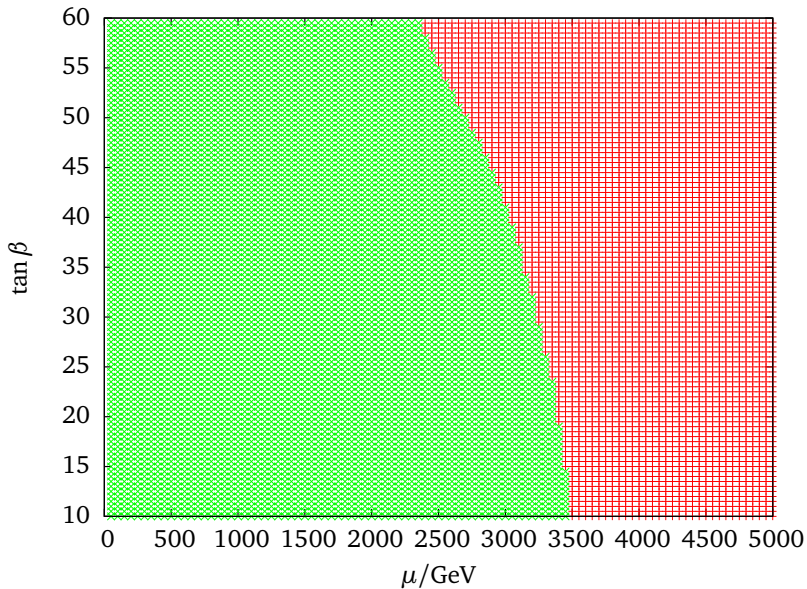
Include more field freedom, extent exclusion bounds.

More fields, more freedom, stronger (!) bounds MSUSY = 1 TeV



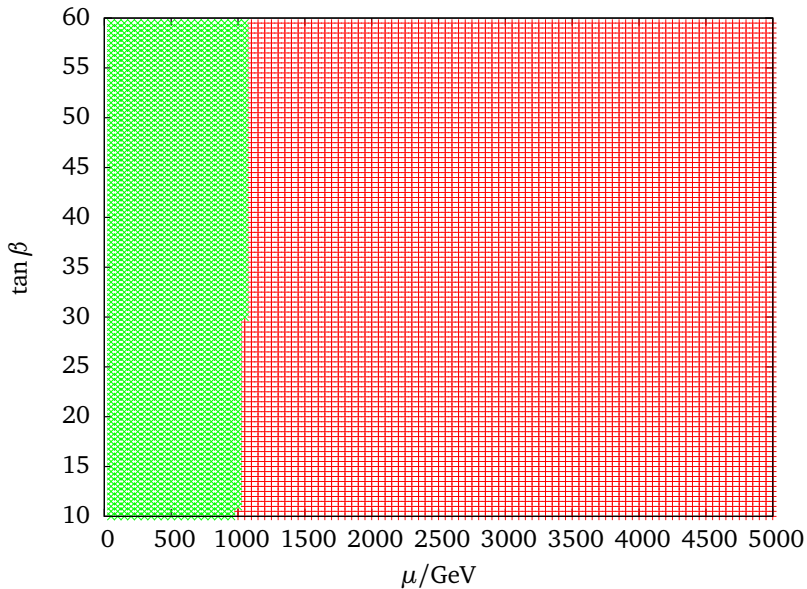
only h_u , and \tilde{b} ; $A_b = 0$

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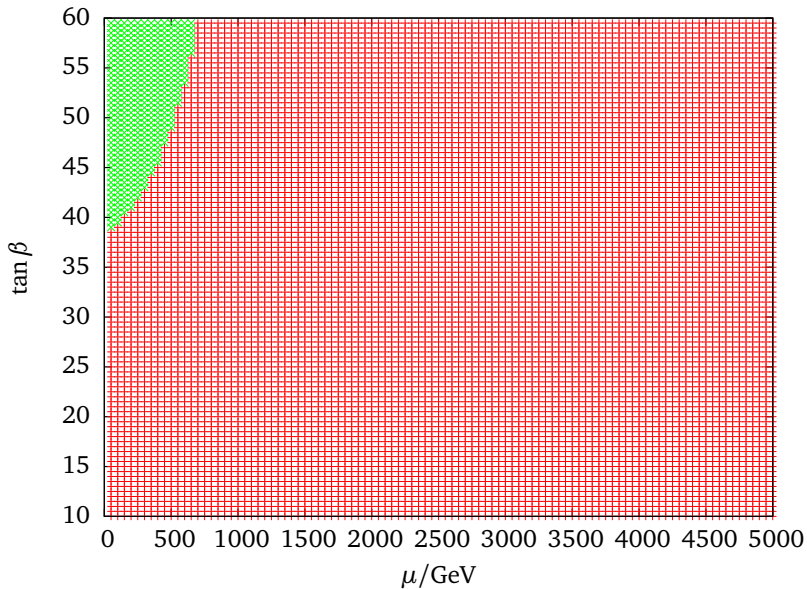
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More fields, more freedom, stronger (!) Bounds MSUSY = 1 TeV



only h_u, h_d, \tilde{t} , and \tilde{b} ; $A_b = 0$

More fields, more freedom, stronger (!) Bounds MSUSY = 1 TeV



only $h_u, h_d, \tilde{t},$ and \tilde{b} ; $A_b = A_t = -1500 \text{ GeV}$

"A-parameter" bounds

$$4\lambda(\eta, \alpha, \beta)M^2(\eta, \alpha, \beta) > (\mathcal{A}(\eta, \alpha, \beta))^2$$

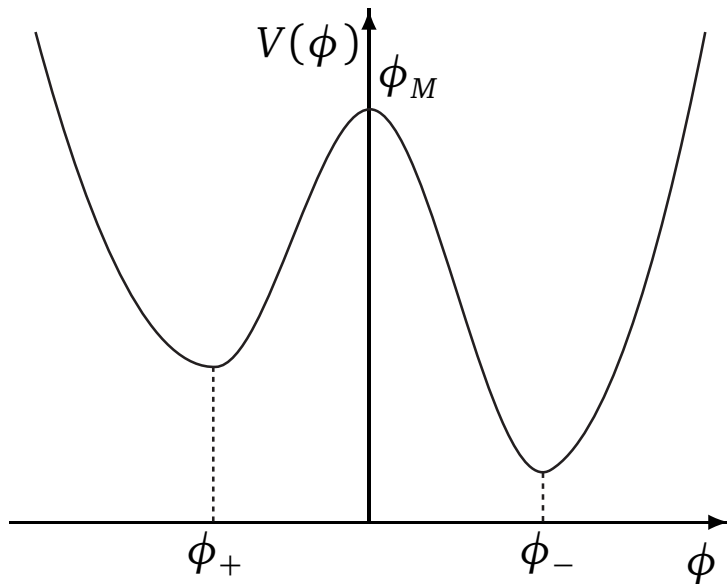
- no unique solution (many combinations possible)
- no clear analytic bound (no robust exclusion)
- numerical exclusions possible
- may run into deep minimum at $\eta, \alpha, \beta \gg 1$
- find pathologic configurations

Global minimum (true vacuum) vs. local minima and saddle points

How much excluded is an excluded point?

Tunneling = Tunneling?

The quantum tunneling effect



The quantum tunneling effect

Decay probability (per unit volume)

$$\frac{\Gamma}{V} = A e^{-B/\hbar}$$

[Coleman '77]

Some approximation . . .

$$B = \frac{2\pi^2}{3} \frac{[(\Delta\phi_+)^2 - (\Delta\phi_-)^2]^2}{\Delta V_+}$$

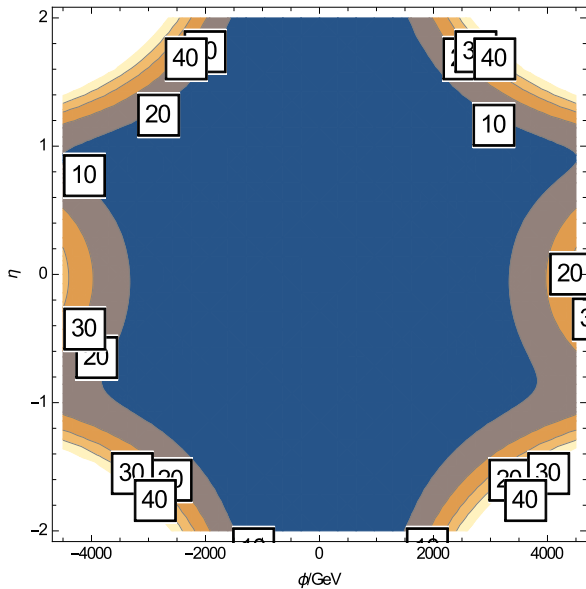
[Duncan, Jensen '92]

Metastability bound

$$B \gtrsim 400$$

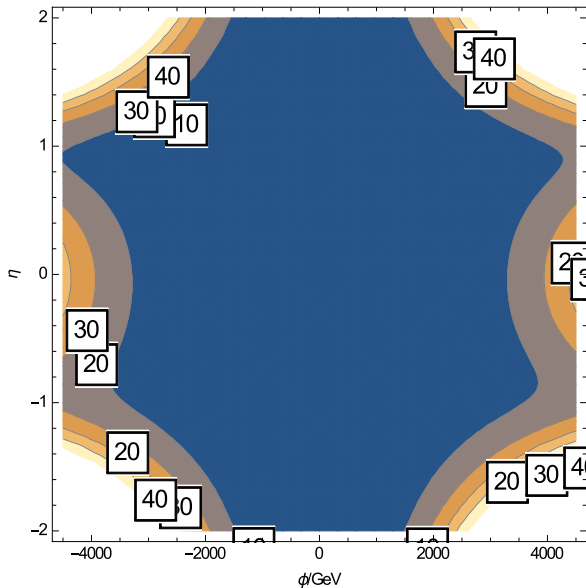
- value of B depends on path
- different conclusions for different η, α, β

Tomography of the scalar potential—sBottom direction



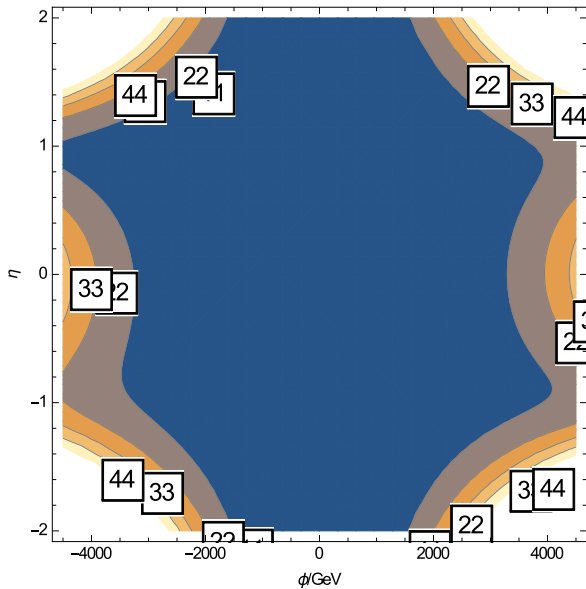
$$\tilde{b} = 0h_u, h_d = \eta h_u$$

Tomography of the scalar potential—sBottom direction



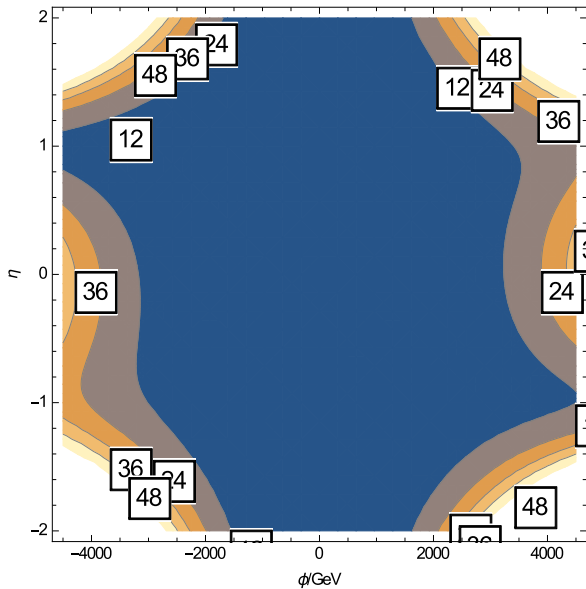
$$\tilde{b} = 0.1h_u, \quad h_d = \eta h_u$$

Tomography of the scalar potential—sBottom direction



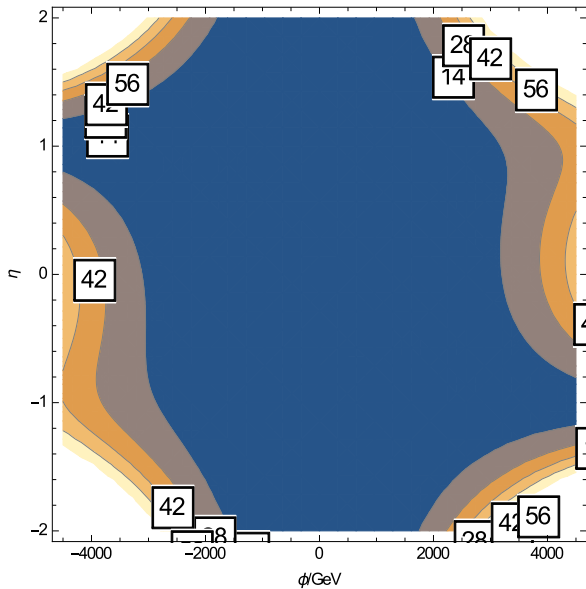
$$\tilde{b} = 0.2h_u, h_d = \eta h_u$$

Tomography of the scalar potential—sBottom direction



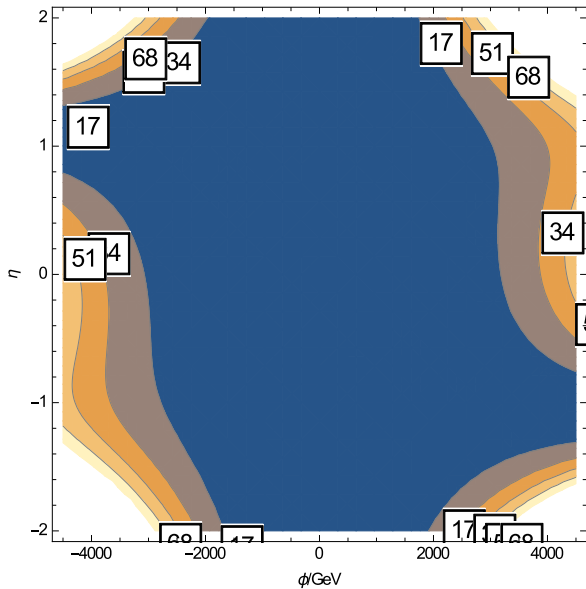
$$\tilde{b} = 0.3h_u, h_d = \eta h_u$$

Tomography of the scalar potential—sBottom direction



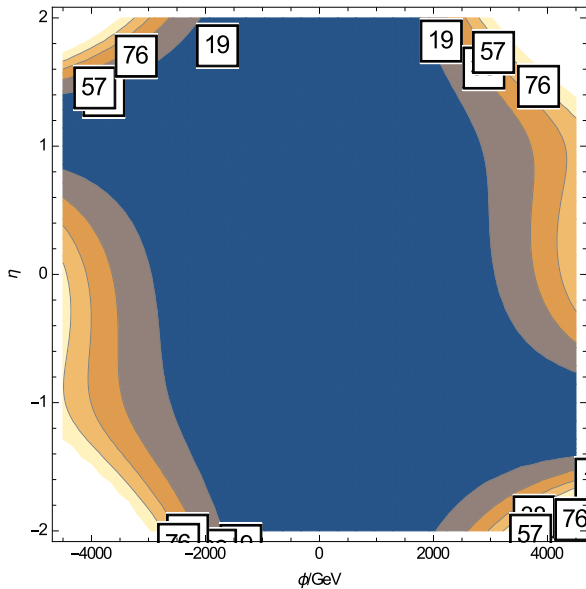
$$\tilde{b}_d = 0.4h_u, h_d = \eta h_u$$

Tomography of the scalar potential—sBottom direction



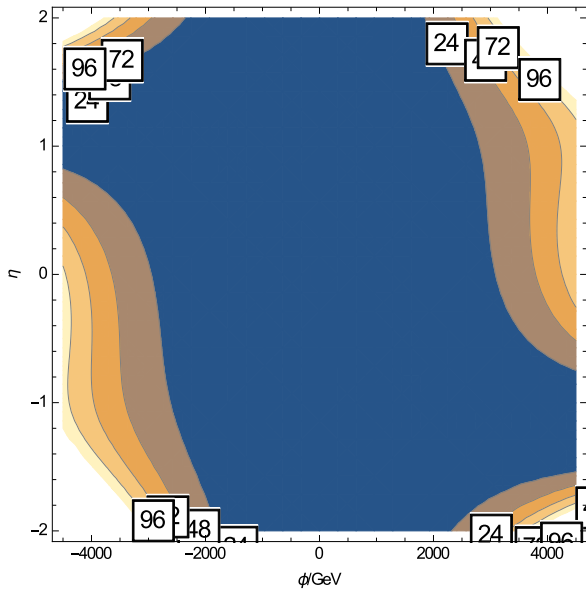
$$\tilde{b} = 0.5h_u, \quad h_d = \eta h_u$$

Tomography of the scalar potential—sBottom direction



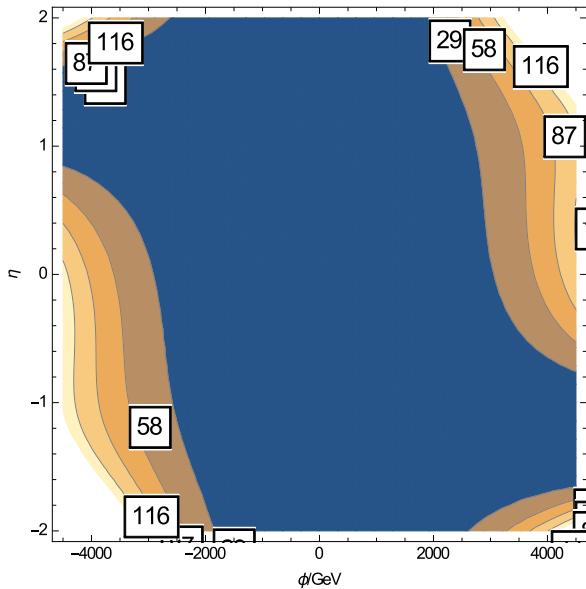
$$\tilde{b} = 0.6h_u, h_d = \eta h_u$$

Tomography of the scalar potential—sBottom direction



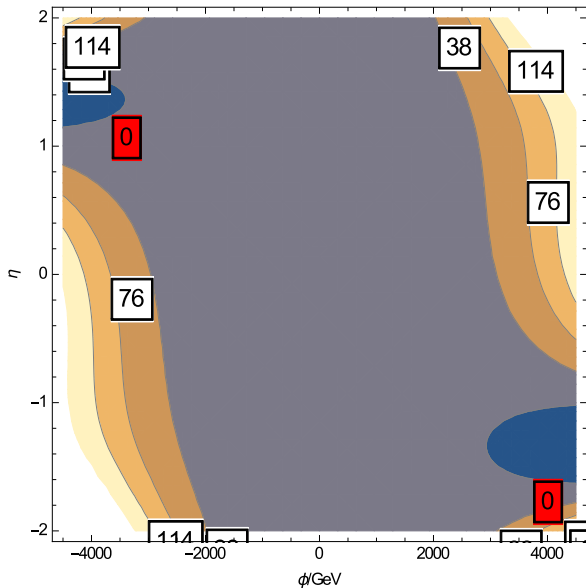
$$\tilde{b} = 0.7h_u, h_d = \eta h_u$$

Tomography of the scalar potential—sBottom direction



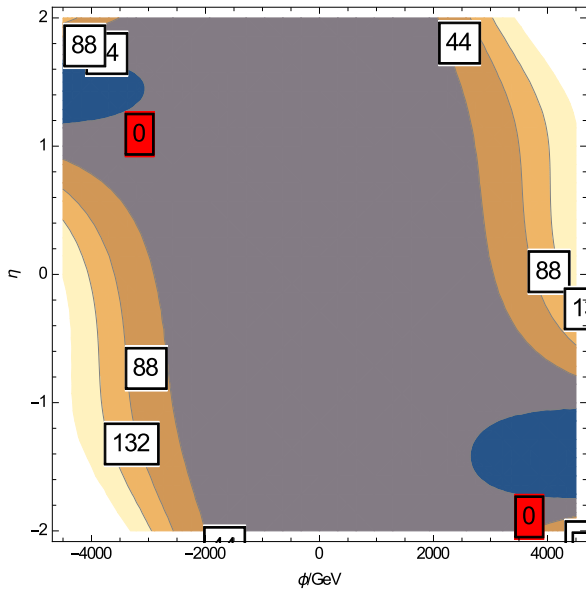
$$\tilde{b} = 0.8h_u, h_d = \eta h_u$$

Tomography of the scalar potential—sBottom direction



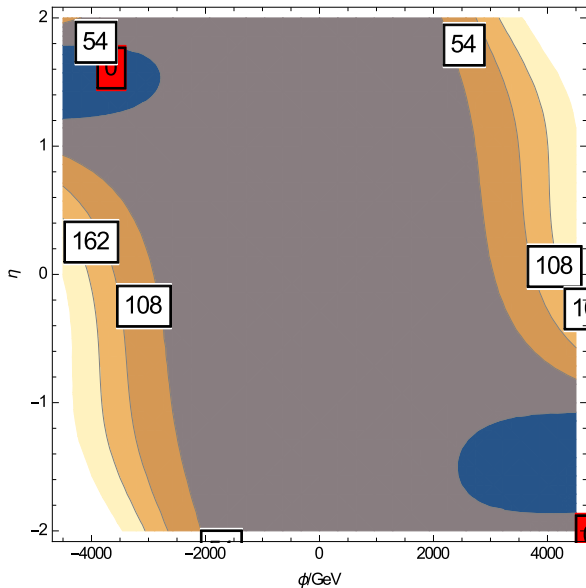
$$\tilde{b} = 0.9h_u, h_d = \eta h_u$$

Tomography of the scalar potential—sBottom direction



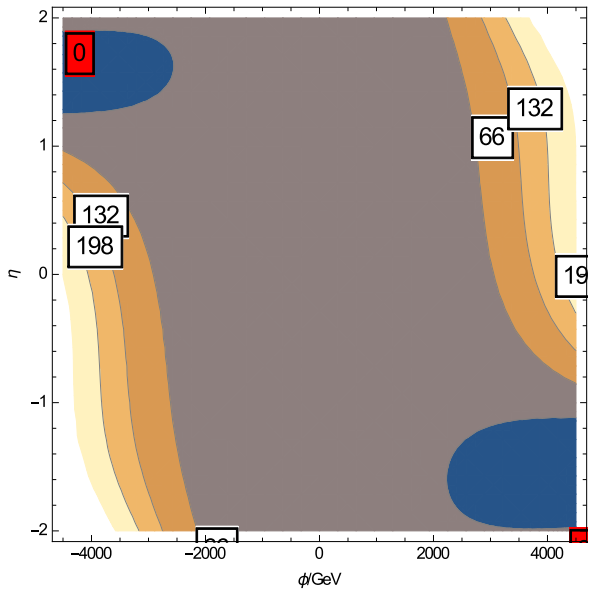
$$\tilde{b} = 1.0h_u, h_d = \eta h_u$$

Tomography of the scalar potential—sBottom direction



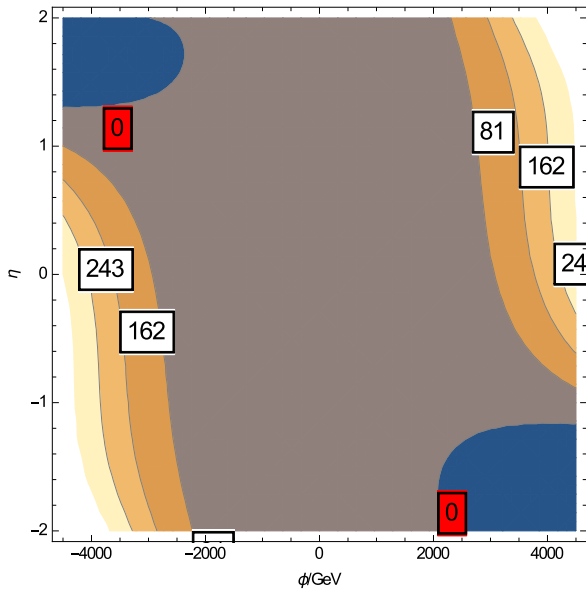
$$\tilde{b} = 1.1h_u, h_d = \eta h_u$$

Tomography of the scalar potential—sBottom direction



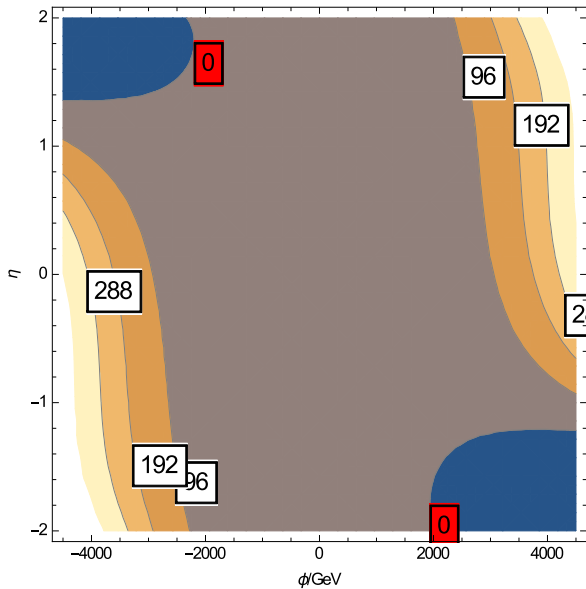
$$\tilde{b} = 1.2h_u, h_d = \eta h_u$$

Tomography of the scalar potential—sBottom direction



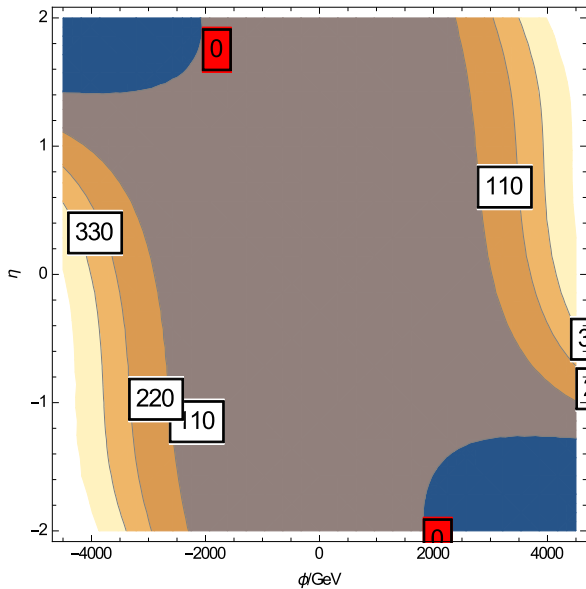
$$\tilde{b} = 1.3h_u, h_d = \eta h_u$$

Tomography of the scalar potential—sBottom direction



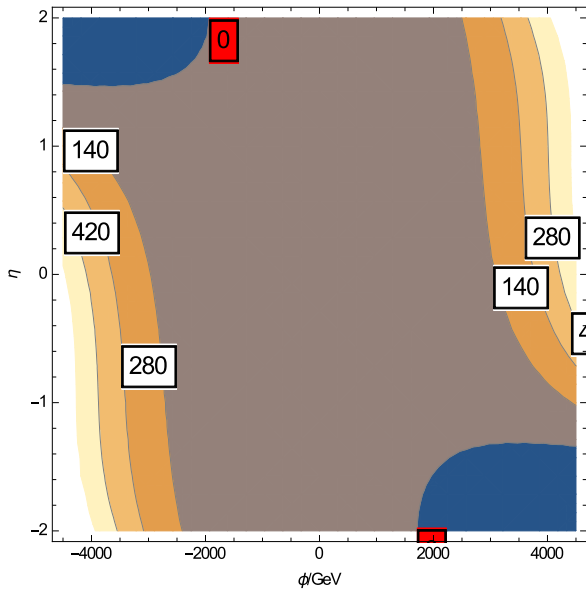
$$\tilde{b} = 1.4h_u, h_d = \eta h_u$$

Tomography of the scalar potential—sBottom direction



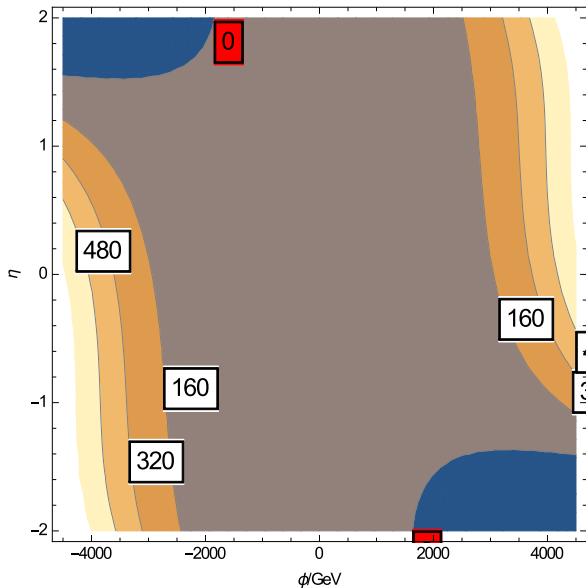
$$\tilde{b} = 1.5h_u, h_d = \eta h_u$$

Tomography of the scalar potential—sBottom direction



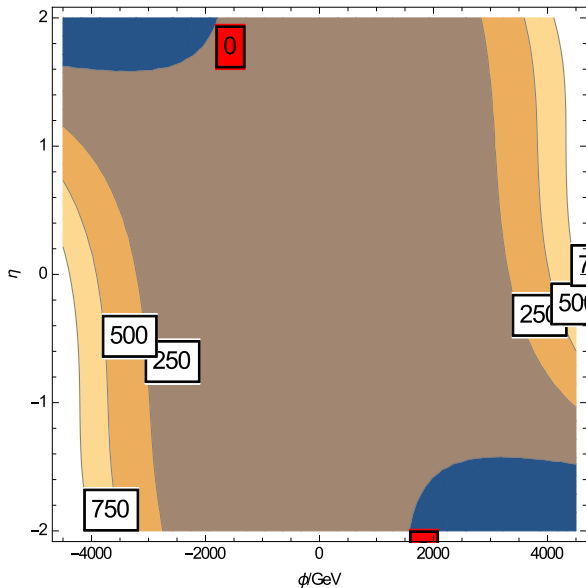
$$\tilde{b} = 1.6h_u, h_d = \eta h_u$$

Tomography of the scalar potential—sBottom direction



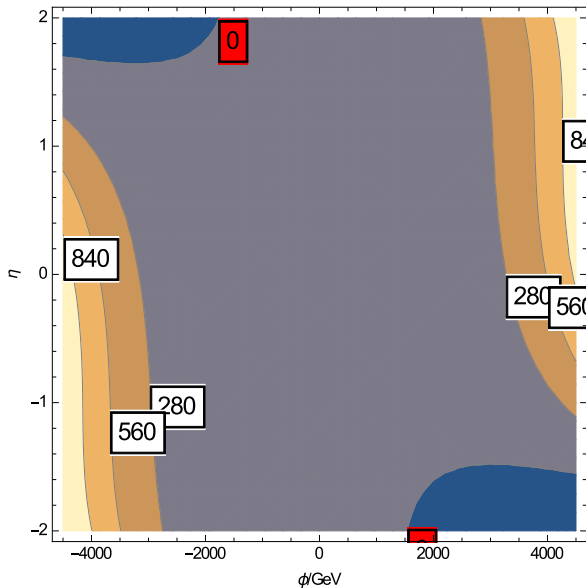
$$\tilde{b} = 1.7h_u, h_d = \eta h_u$$

Tomography of the scalar potential—sBottom direction



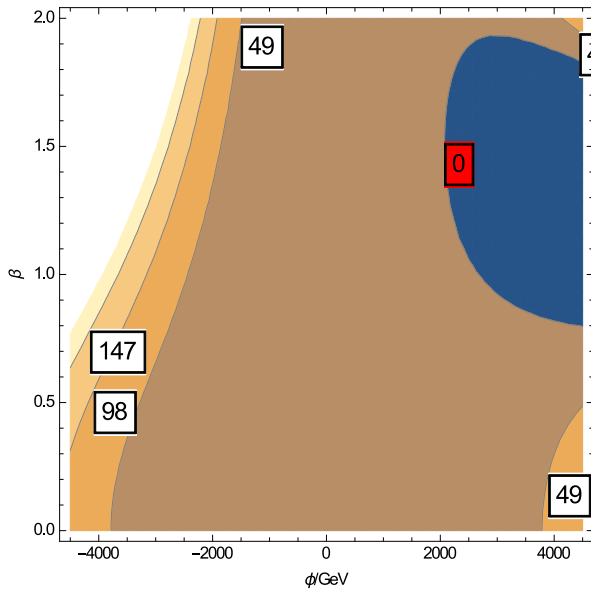
$$\tilde{b} = 1.8h_u, h_d = \eta h_u$$

Tomography of the scalar potential—sBottom direction



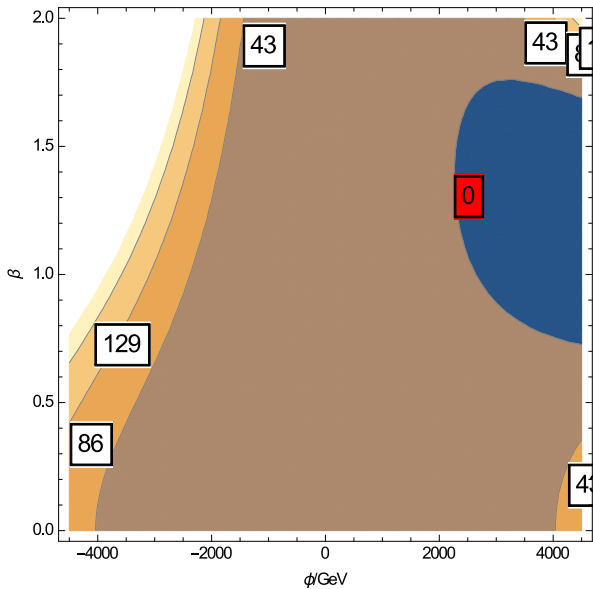
$$\tilde{b} = 1.9h_u, \quad h_d = \eta h_u$$

Tomography of the scalar potential— h_d direction



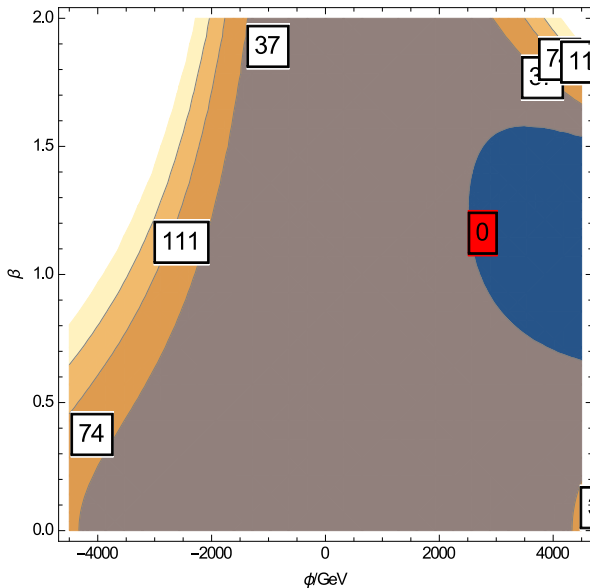
$$\tilde{h}_d = -1.5h_u, \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



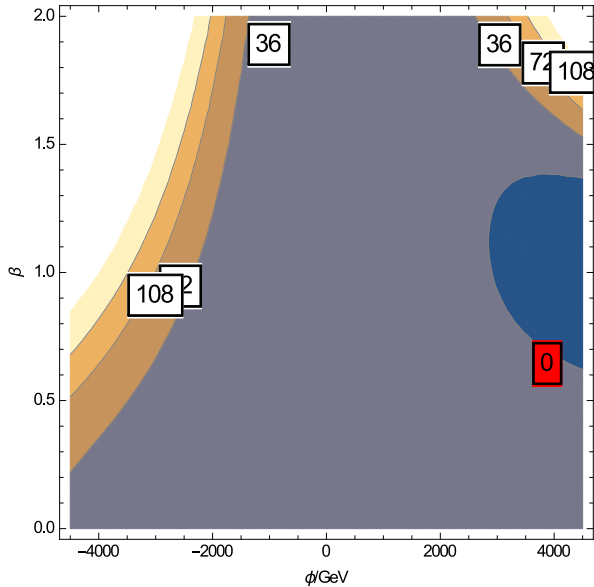
$$\tilde{h}_d = -1.4h_u, \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



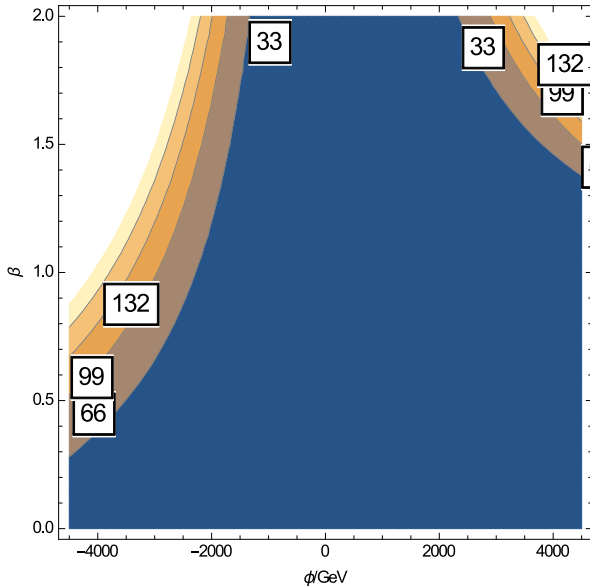
$$\tilde{h}_d = -1.3h_u, \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



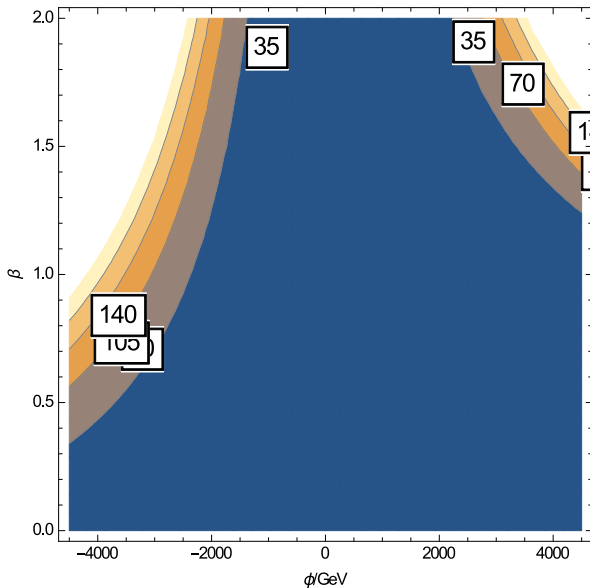
$$\tilde{h}_d = -1.2h_u, \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



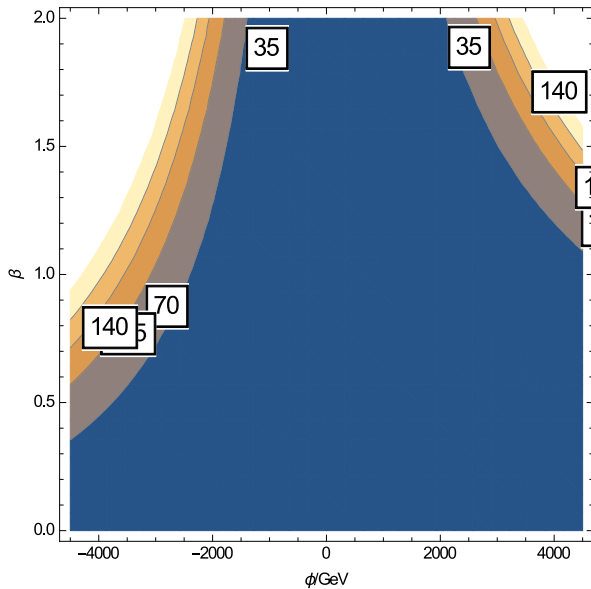
$$\tilde{h}_d = -1.1h_u, \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



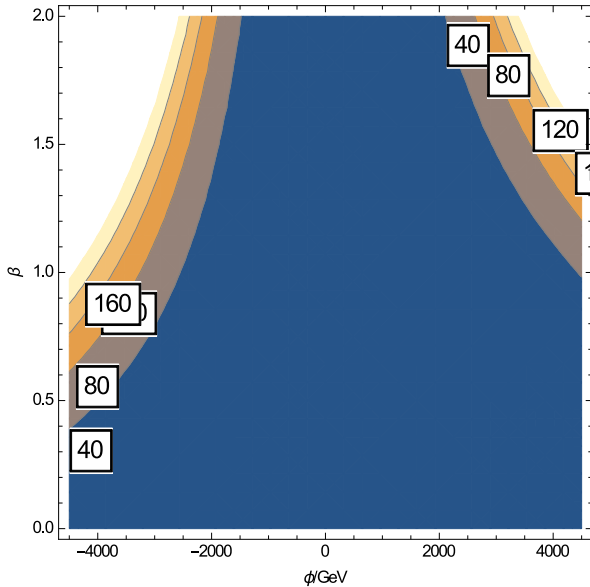
$$\tilde{h}_d = -1.0h_u, \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



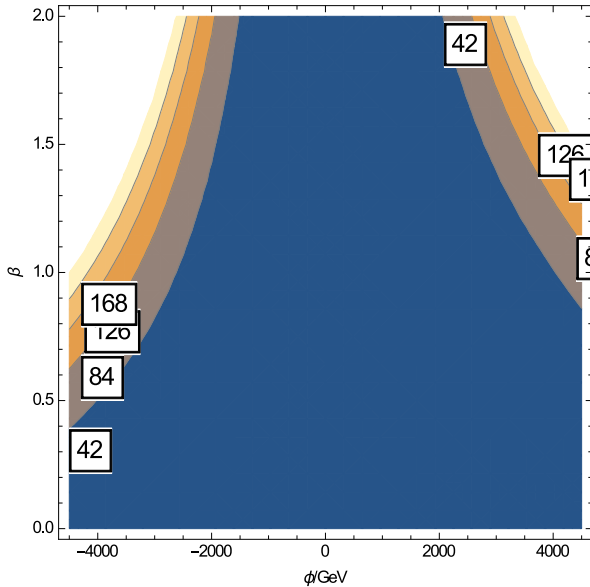
$$\tilde{h}_d = -0.9h_u, \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



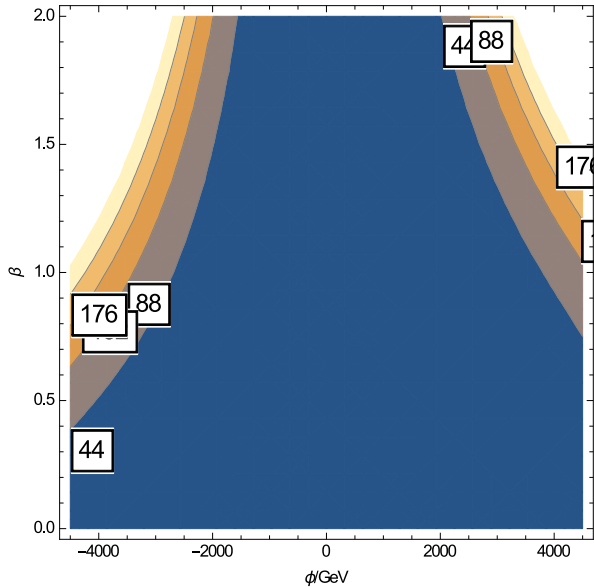
$$\tilde{h}_d = -0.8h_u, \quad \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



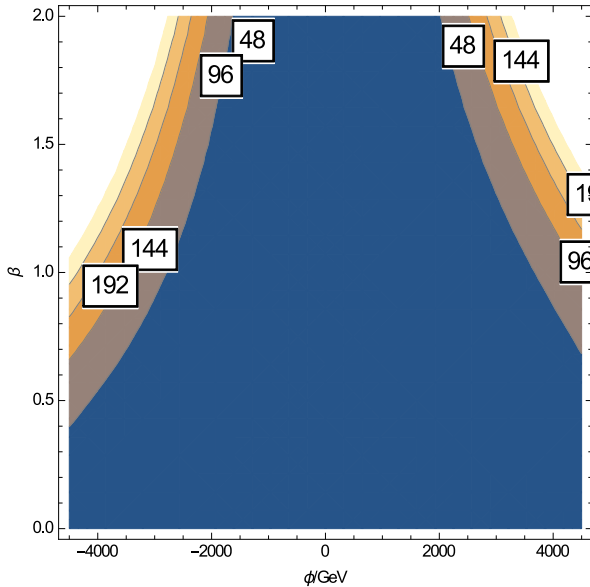
$$\tilde{h}_d = -0.7h_u, \quad \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



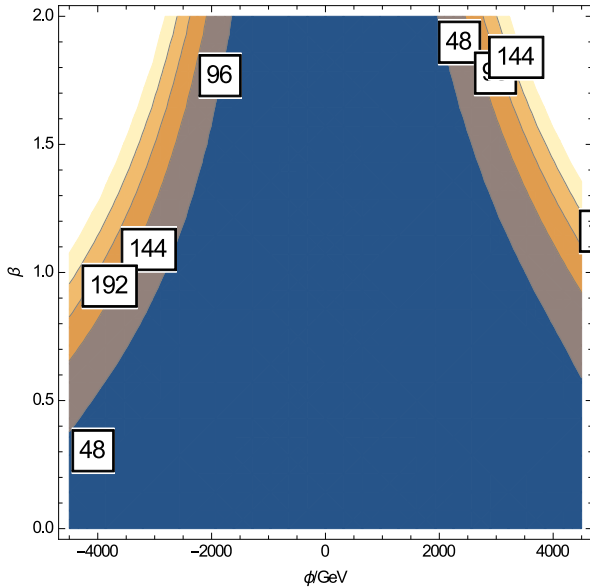
$$\tilde{h}_d = -0.6h_u, \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



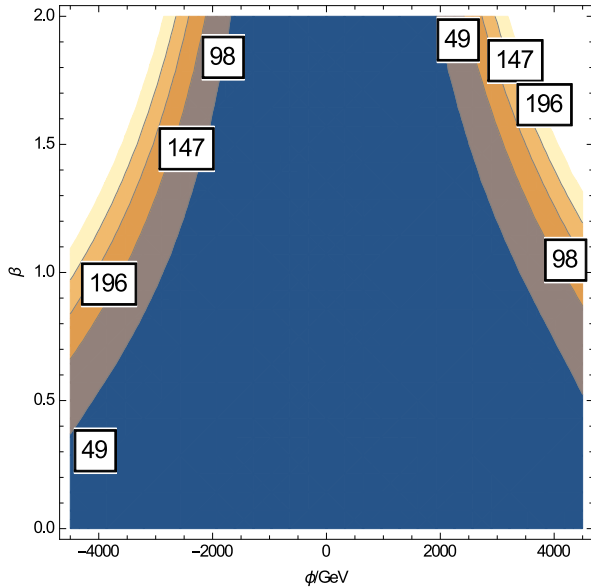
$$\tilde{h}_d = -0.5h_u, \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



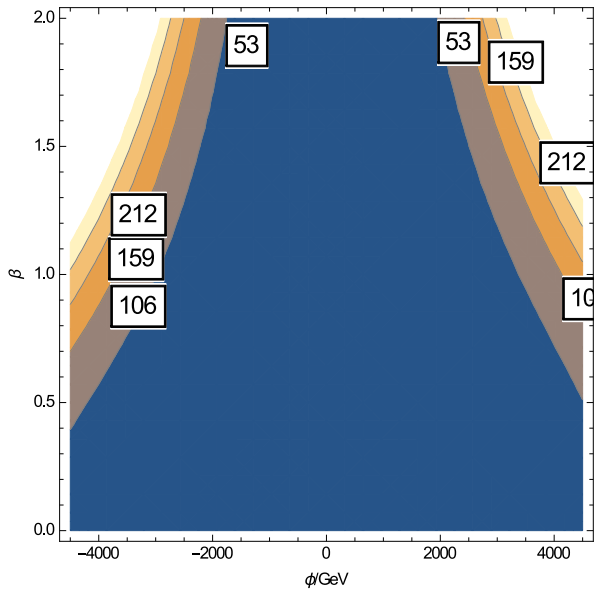
$$\tilde{h}_d = -0.4h_u, \quad \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



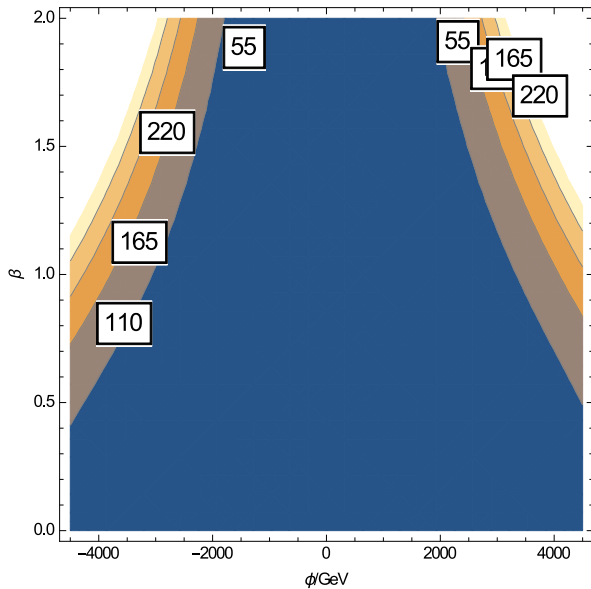
$$\tilde{h}_d = -0.3h_u, \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



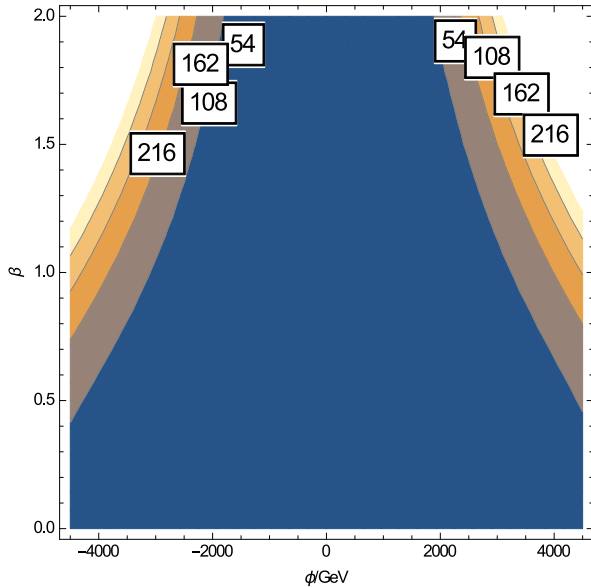
$$\tilde{h}_d = -0.2h_u, \quad \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



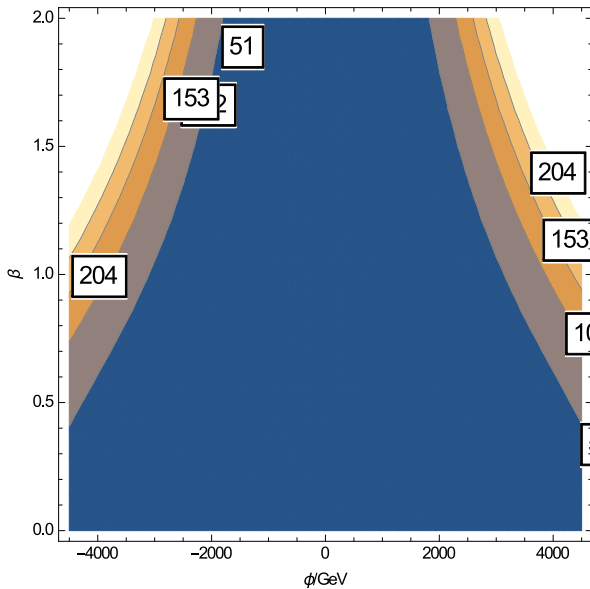
$$\tilde{h}_d = -0.1h_u, \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



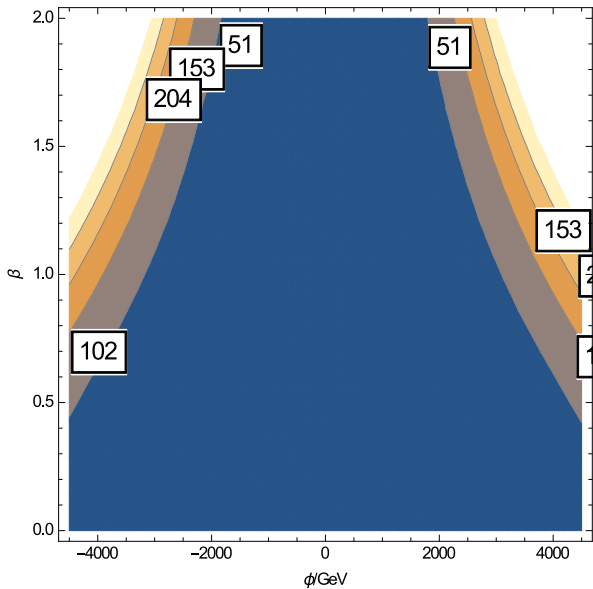
$$\tilde{h}_d = 0h_u, \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



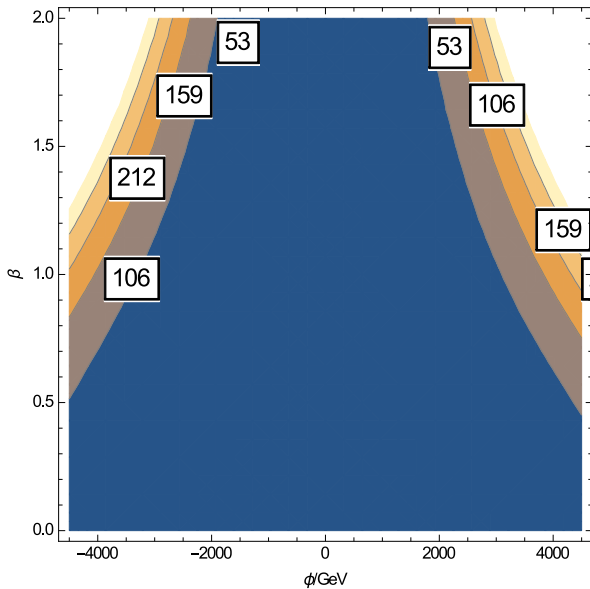
$$\tilde{h}_d = 0.1h_u, \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



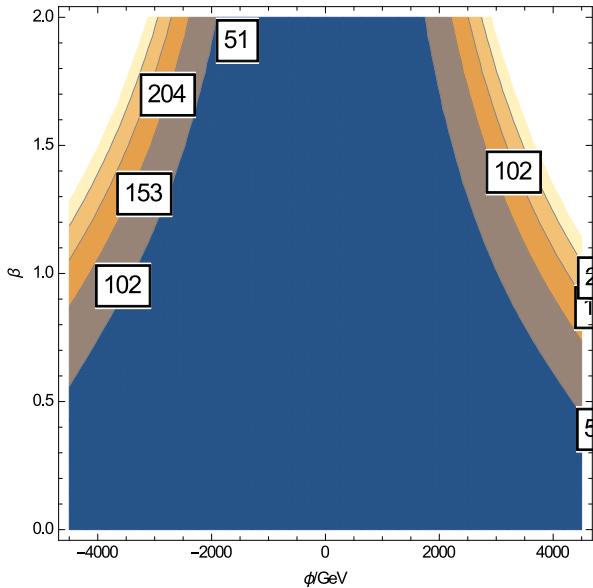
$$\tilde{h}_d = 0.2h_u, \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



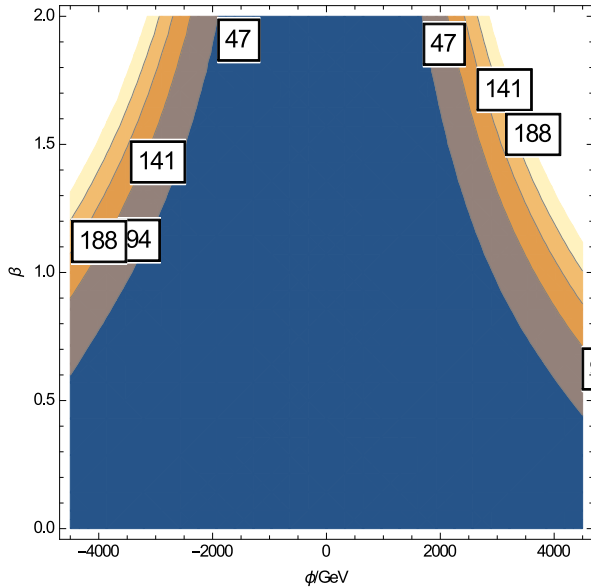
$$\tilde{h}_d = 0.3h_u, \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



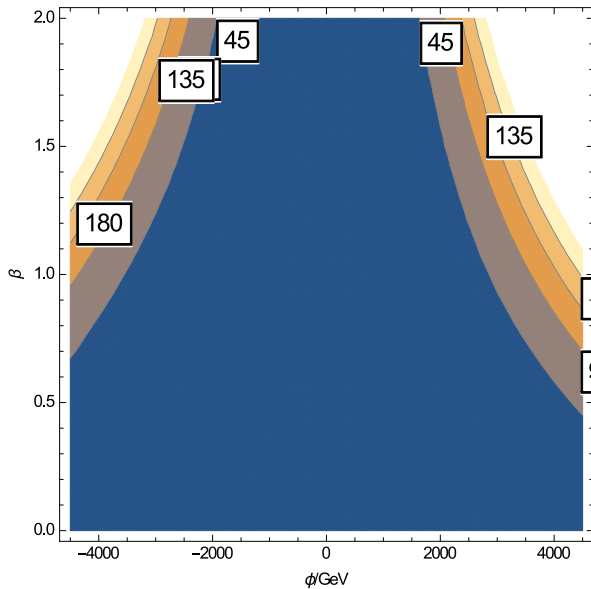
$$\tilde{h}_d = 0.4h_u, \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



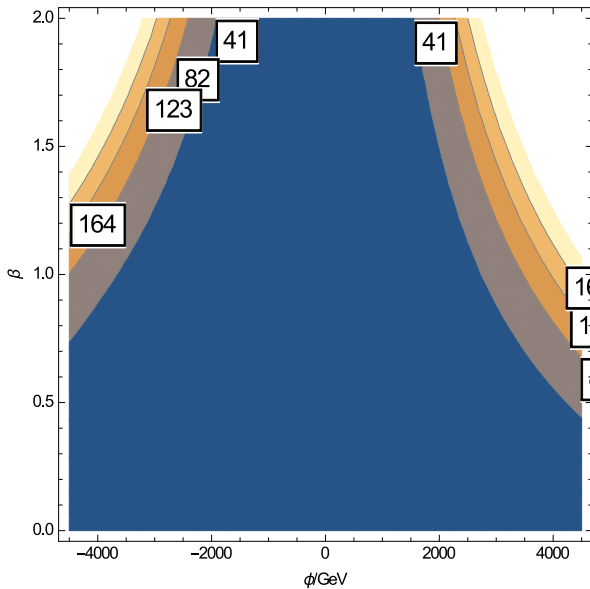
$$\tilde{h}_d = 0.5h_u, \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



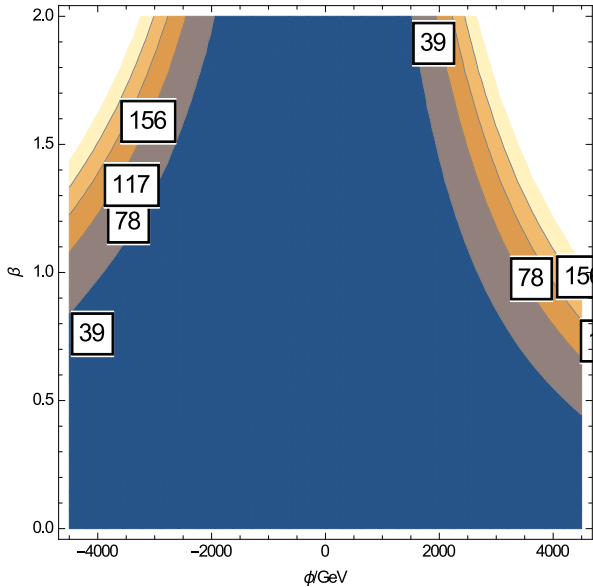
$$\tilde{h}_d = 0.6h_u, \quad \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



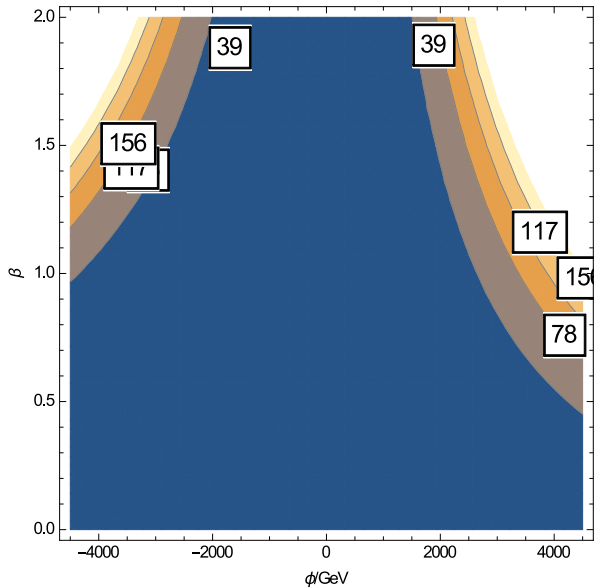
$$\tilde{h}_d = 0.7h_u, \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



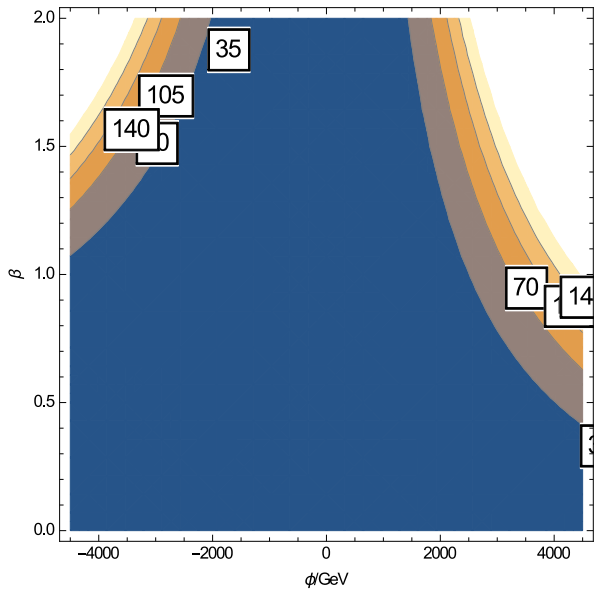
$$\tilde{h}_d = 0.8h_u, \quad \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



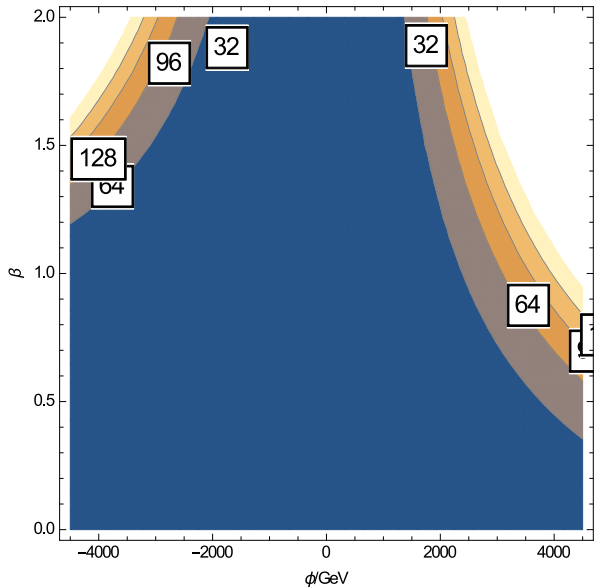
$$\tilde{h}_d = 0.9h_u, \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



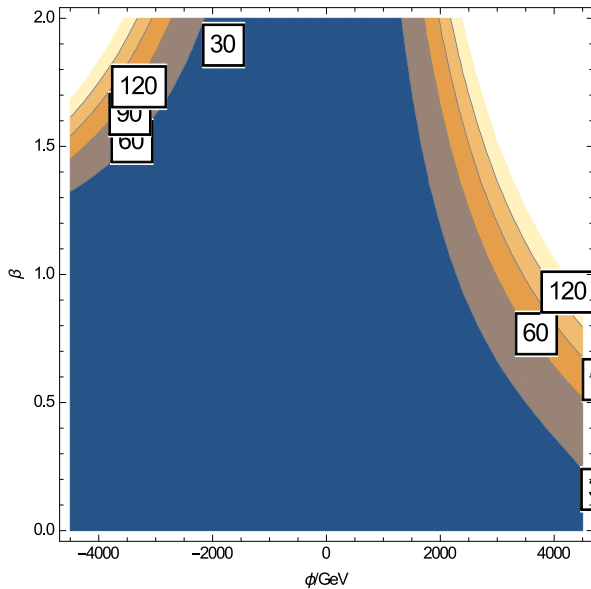
$$\tilde{h}_d = 1.0h_u, \tilde{b} = \beta h_u$$

Tomography of the scalar potential— h_d direction



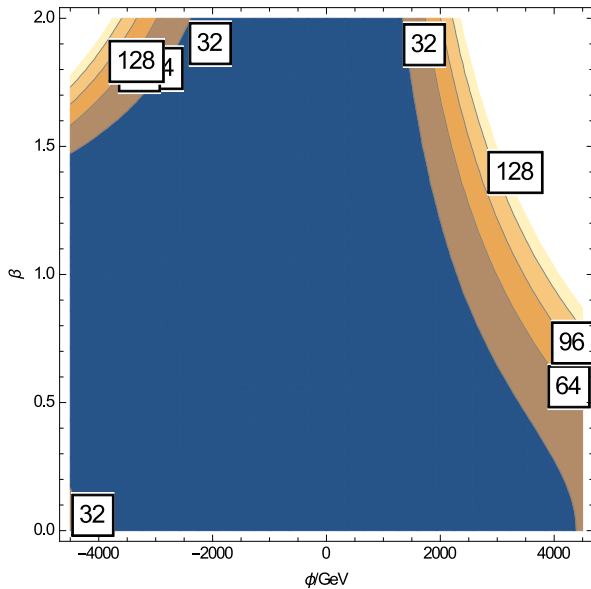
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Tomography of the scalar potential— h_d direction



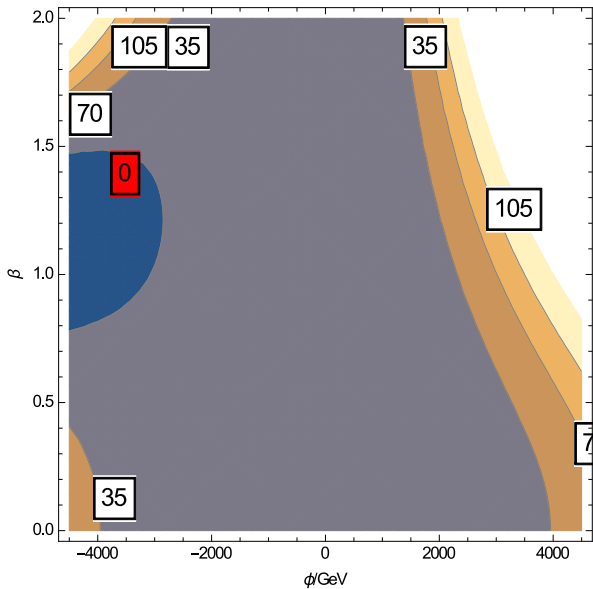
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Tomography of the scalar potential— h_d direction



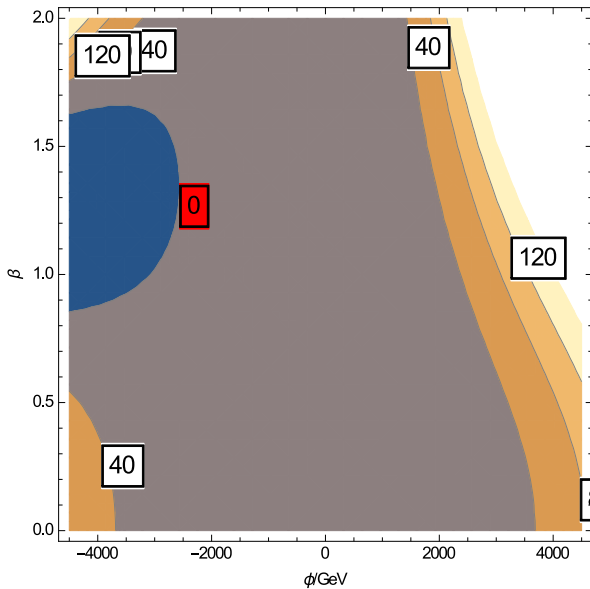
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Tomography of the scalar potential— h_d direction



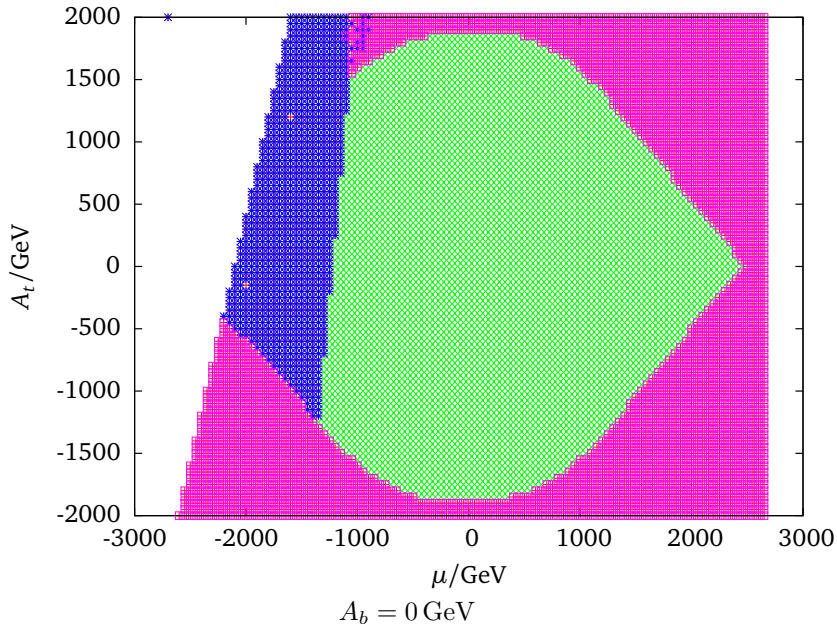
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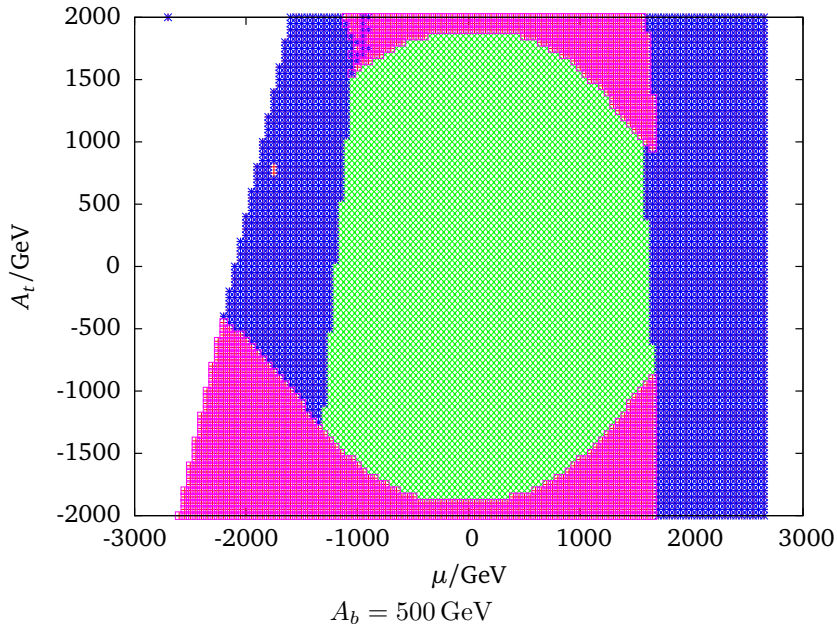
Tomography of the scalar potential— h_d direction

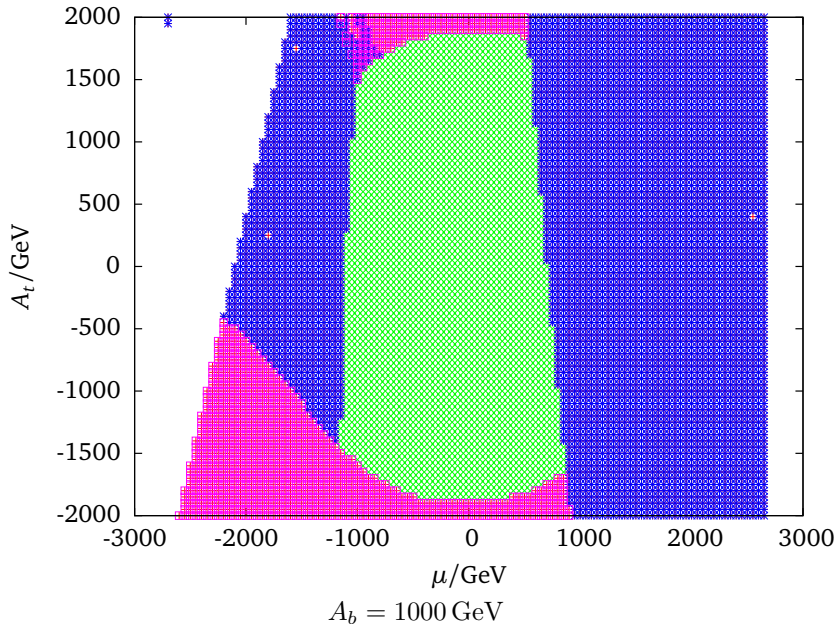


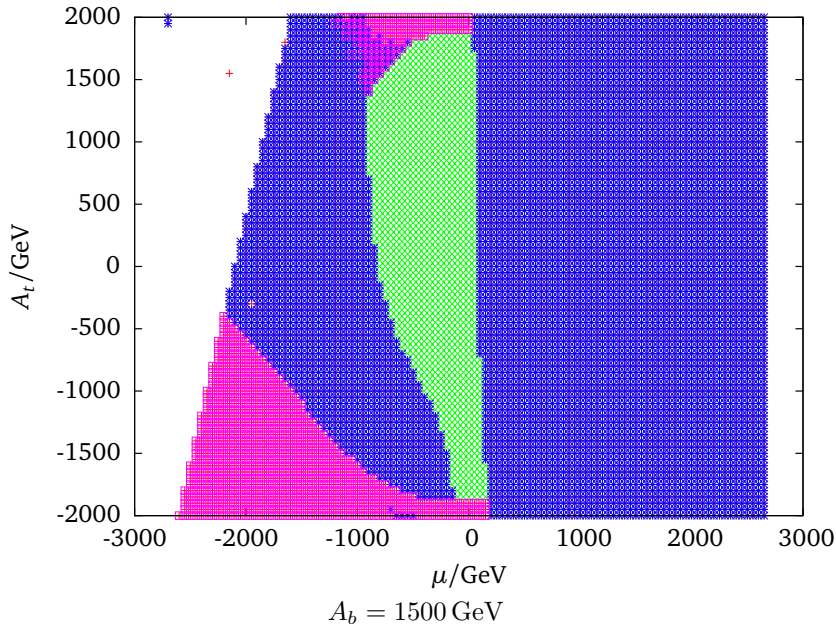
$$\tilde{h}_d = 1.5h_u, \tilde{b} = \beta h_u$$

- no pocket-calculator formula :-(
• numerical/graphical exclusion limits in μ - $\tan \beta$ - A_t - A_b











- charge and color breaking constraints complementary to direct searches
- check for theoretical consistency
- a closer view reveals very strong constraints

Simple analytic formulae — **by far not the strongest bounds**

- $|\tilde{t}_L| = |\tilde{t}_R| = |h_u|$

$$|A_t|^2 < 3y_t^2 (m_{h_2}^2 + |\mu|^2 + \tilde{m}_L^2 + \tilde{m}_t^2)$$

[Gunion, Haber, Sher '88]

- $|\tilde{b}_L| = |\tilde{b}_R| = |h_u|$

$$m_{H_u}^2 + \mu^2 + \tilde{m}_Q^2 + \tilde{m}_b^2 > \frac{(\mu y_b)^2}{y_b^2 + (g_1^2 + g_2^2)/2}$$

[WGH '15]

Actually more involved!



- charge and color breaking constraints complementary to direct searches
- check for theoretical consistency
- a closer view reveals very strong constraints

Simple analytic formulae — **by far not the strongest bounds**

- $|\tilde{t}_L| = |\tilde{t}_R| = |h_u|$

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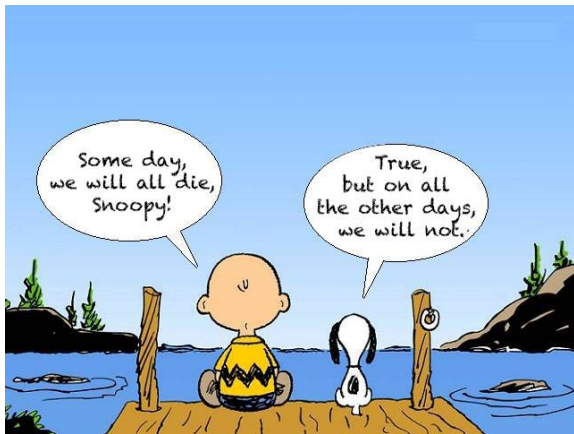
[Gunion, Haber, Sher '88]

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[WGH '15]

$$4\lambda(\eta, \alpha, \beta)M^2(\eta, \alpha, \beta) > (\mathcal{A}(\eta, \alpha, \beta))^2$$



All the details: [arXiv:1606.0xxxx](https://arxiv.org/abs/1606.0xxxx)

Backup

Slides

Yukawa coupling not directly proportional to mass (same for y_t)

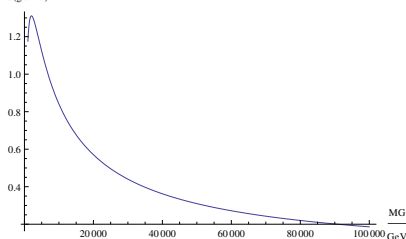
$$y_b = \frac{m_b}{v_d(1 + \Delta_b)}$$

[Hall, Rattazzi, Sarid '94; Carena, Garcia, Nierste, Wagner '99]

$$\Delta_b^{\text{gluino}} = \frac{2\alpha_s}{3\pi} \mu M_{\tilde{G}} \tan \beta C_0(\tilde{m}_{\tilde{b}_1}, \tilde{m}_{\tilde{b}_2}, M_{\tilde{G}}),$$

$$\Delta_b^{\text{higgsino}} = \frac{Y_t^2}{16\pi^2} \mu A_t \tan \beta C_0(\tilde{m}_{\tilde{t}_1}, \tilde{m}_{\tilde{t}_2}, \mu).$$

$\Delta_b(\text{gluino})$



$\Delta_b(\text{higgsino})$

