

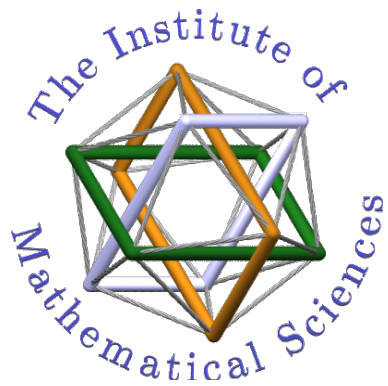
QCD RADIATIVE CORRECTIONS TO HIGGS PHYSICS

Taushif Ahmed

Feb 21, 2017

Talk to Defend My Thesis

Thesis Advisor: Prof. V. Ravindran



MOTIVATIONS

- It is an interesting era for High energy physics

2012's Discovery of SM-Higgs-like particle

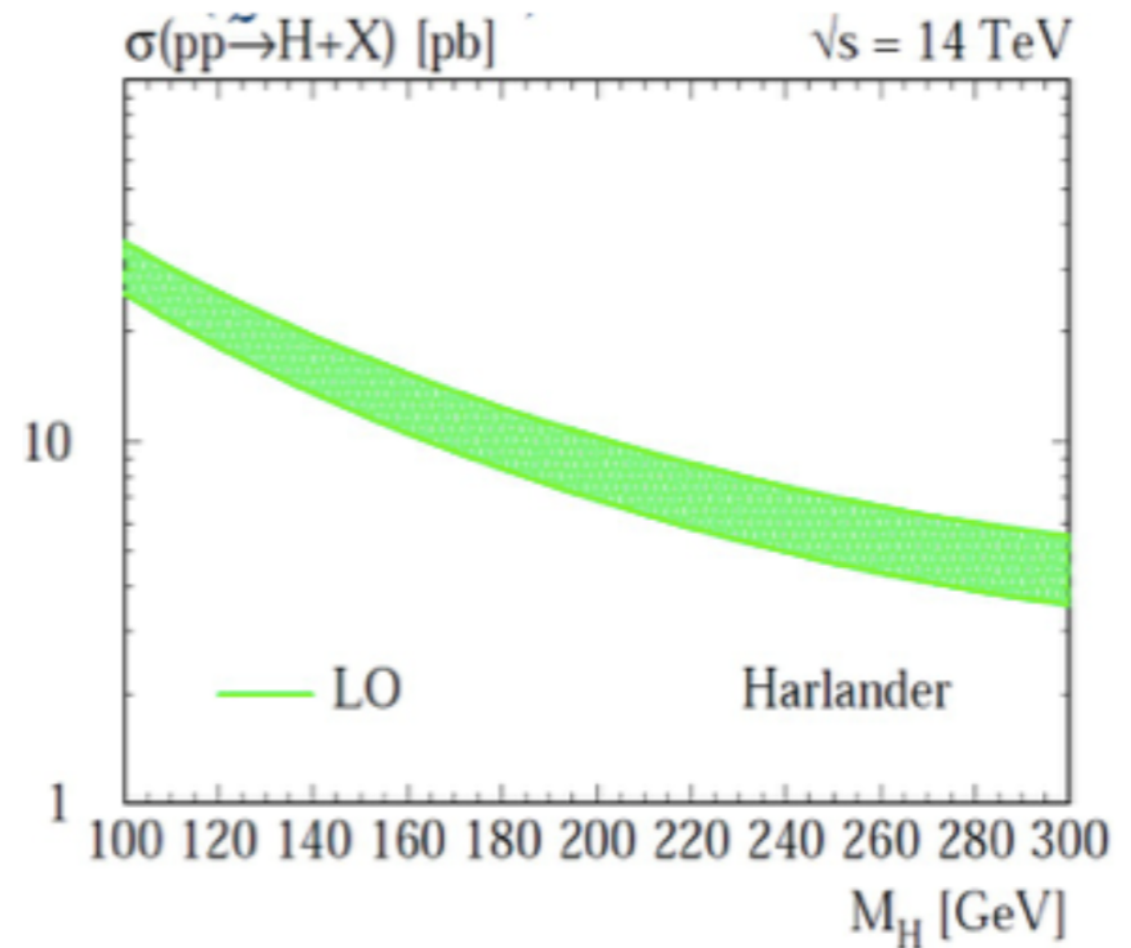
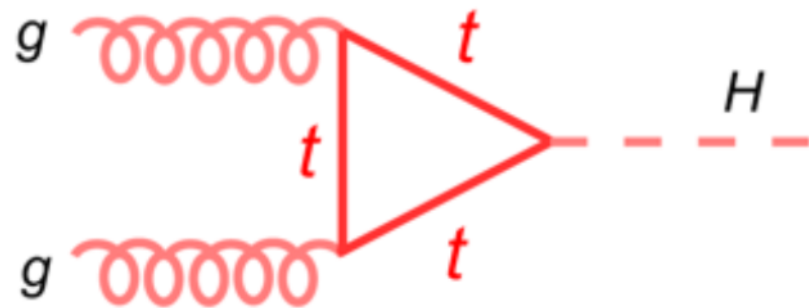
~~Excess in 750 GeV~~

- Is it new physics or the SM?
- Confirming these demand more data at LHC and precise theoretical predictions
- QCD radiative corrections are crucial

MOTIVATIONS

LO is a crude approximation

$$2S\sigma^H(x, m_H) = \int_x^1 \frac{dz}{z} \Phi_{gg}^{(0)}(z, \mu_F) 2\hat{s}\hat{\sigma}_{gg}^{(0)}\left(\frac{x}{z}, m_H^2, \mu_R\right) + \dots$$

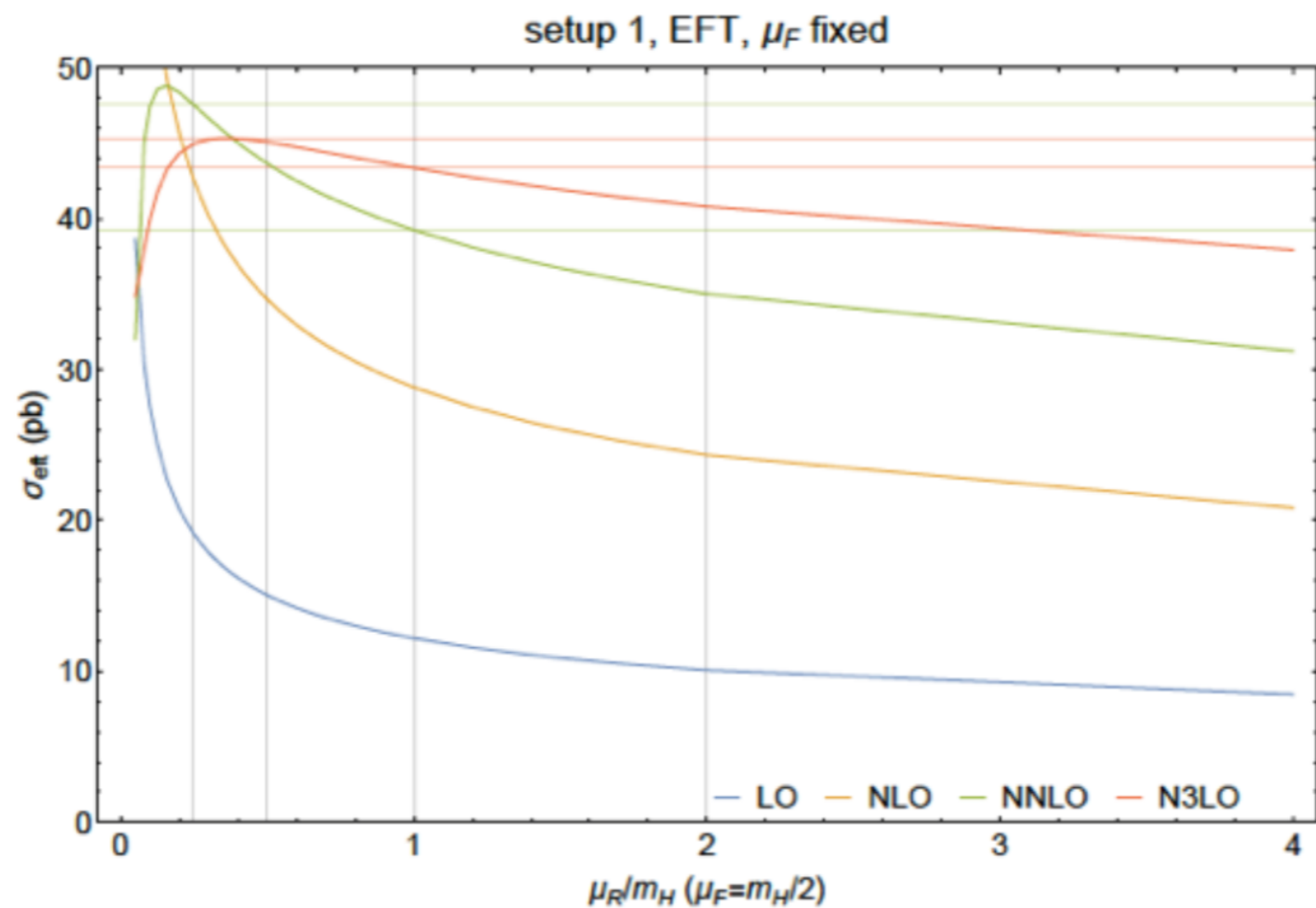
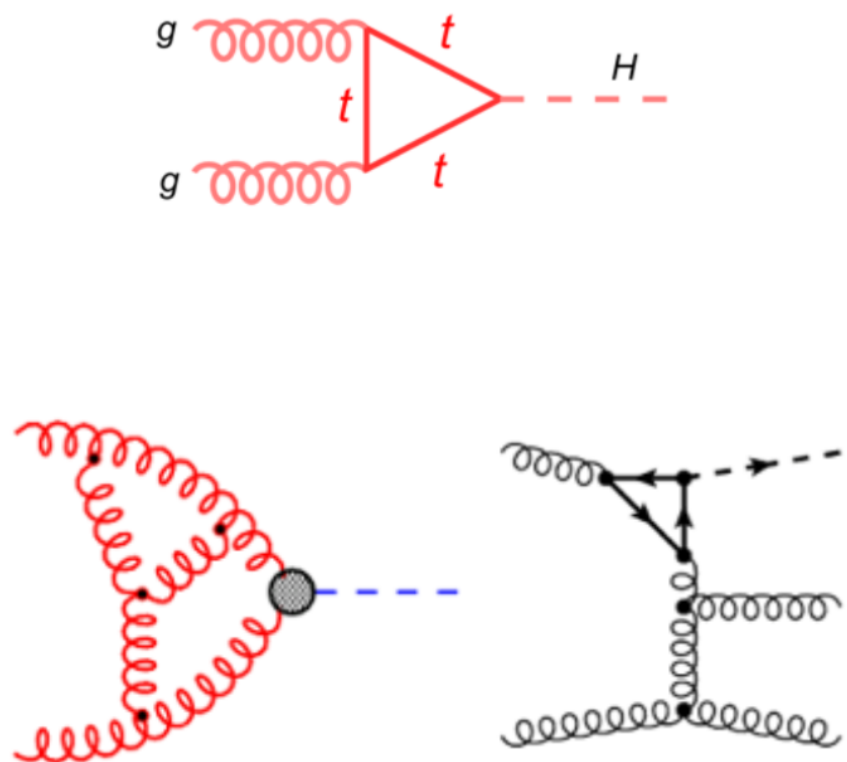


$$2\hat{s}\hat{\sigma}_{gg}^{(0)}\left(\frac{x}{z}, m_H^2, \mu_R\right) = \alpha_s^2(\mu_R) G_F F(m_t, m_H)$$

LO prediction is unreliable: **Huge** scale uncertainty

MOTIVATIONS

Reliable Result at N^3LO



$\Delta_{\text{EFT},k}^{\text{scale}} (\mu_F = m_H/2)$		
LO	($k = 0$)	$\pm 22.0\%$
NLO	($k = 1$)	$\pm 19.2\%$
NNLO	($k = 2$)	$\pm 9.5\%$
N ³ LO	($k = 3$)	$\pm 2.2\%$

$\Delta_{\text{EFT},k}^{\text{scale}}$		
LO	($k = 0$)	$\pm 14.8\%$
NLO	($k = 1$)	$\pm 16.6\%$
NNLO	($k = 2$)	$\pm 8.8\%$
N ³ LO	($k = 3$)	$\pm 1.9\%$

WHAT IS NEXT?

This thesis arises in this context



Precise predictions in Higgs, pseudo-Higgs & DY
production channels

1. Higgs Boson Production Through $b\bar{b}$ Annihilation At Threshold N^3LO QCD

TA, Rana & Ravindran
JHEP 1410, 139 (2014)

2. Rapidity Distribution In Drell-Yan & Higgs Productions at Threshold N^3LO QCD

TA, Mandal, Rana & Ravindran
Phys.Rev.Lett. 113, 212003 (2014)

3. Pseudo Scalar Form Factors At 3-Loop QCD

TA, Gehrmann, Mathews, Rana & Ravindran
JHEP 1511, 169 (2015)

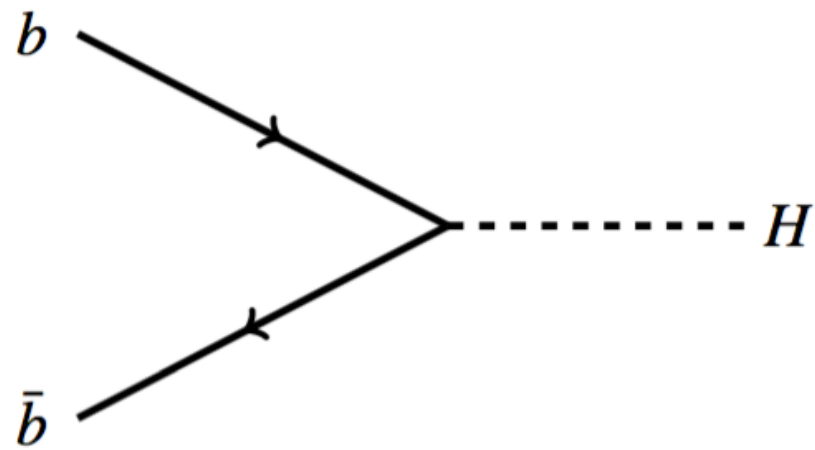
4. Pseudo-scalar Higgs Boson Production at Threshold N^3LO and N^3LL QCD

TA, Kumar, Mathews, Rana & Ravindran
Eur. Phys. J. C (2016) 76:355

PUBLICATIONS (NOT INCLUDED IN THESIS)

5. **Two-Loop QCD Correction to massive spin-2 resonance $\rightarrow$ 3-gluons**
JHEP 1405, 107 (2014) TA, Mahakhud, Mathews, Rana & Ravindran
6. **Drell-Yan Production at Threshold to Third Order in QCD**
Phys.Rev.Lett. 113, 112002 (2014) TA, Mahakhud, Rana & Ravindran
7. **Two-loop QCD corrections to Higgs $\rightarrow b + \bar{b} + g$ amplitude**
JHEP 1408, 075 (2014) TA, Mahakhud, Mathews, Rana & Ravindran
8. **Higgs Rapidity Distribution in $b\bar{b}$ Annihilation at Threshold in N^3LO QCD**
JHEP 1502, 131 (2015) TA, Mandal, Rana & Ravindran
9. **Spin-2 Form Factors at Three Loop in QCD**
JHEP 1512, 084 (2015) TA, Das, Mathews, Rana & Ravindran
10. **Pseudo-scalar Higgs boson production at $N^3LO_A + N^3LL'$**
Eur.Phys.J. C76 (2016) no.12, 663 TA, Bonvini, Kumar, Mathews, Rottoli, Rana & Ravindran
11. **NNLO QCD Corrections to the Drell-Yan Cross Section in Models of TeV- Scale Gravity**
Eur.Phys.J. C77 (2017) no.1, 22 TA, Banerjee, Dhani, Kumar, Mathews, Rana & Ravindran
12. **The two-loop QCD correction to massive spin-2 resonance $\rightarrow q\bar{q}g$**
Eur.Phys.J. C76 (2016) no.12, 667 TA, Das, Mathews, Rana & Ravindran
13. **Konishi Form Factor at Three Loop in $\mathcal{N} = 4$ SYM**
arXiv:1610.05317 [hep-th] (Under consideration in PRL) TA, Banerjee, Dhani, Rana, Ravindran & Seth
14. **Three loop form factors of a massive spin-2 with non-universal coupling**
arXiv:1612.00024 [hep-ph] (Appeared to be in PRD) TA, Banerjee, Dhani, Mathews, Rana & Ravindran
15. **RG improved Higgs boson production to N_3LO in QCD**
arXiv:1505.07422 [hep-ph] TA, Das, Kumar, Mathews, Rana & Ravindran

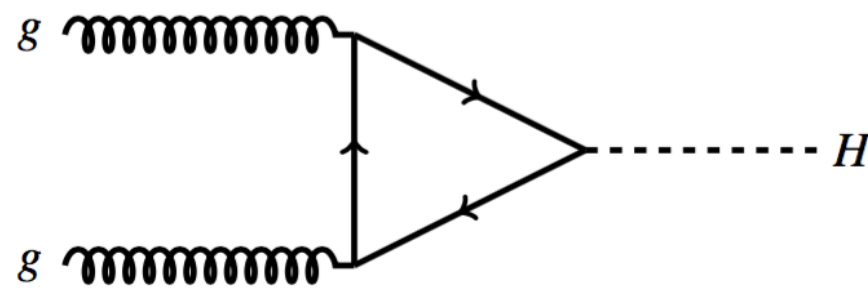
HIGGS BOSON PRODUCTION THROUGH $b\bar{b}$ ANNIHILATION AT THRESHOLD N³LO QCD



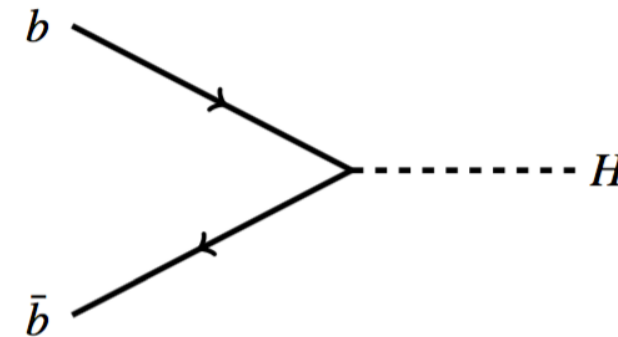
TA, Rana & Ravindran
JHEP 1410, 139 (2014)

Higgs boson production

Dominant



Sub-dominant



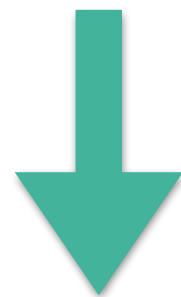
- Yukawa coupling: small in SM, can be enhanced in MSSM
- Measurements of Higgs couplings are underway at LHC
- In precision studies nothing is unimportant

QCD RADIATIVE CORRECTIONS ARE CRUCIAL

MOTIVATIONS: SV

- Going beyond LO: **challenging**
 - large no of diagrams
 - Loop integrals
 - Phase space integrals
- Often **fail** to compute **complete fixed order** result
- Alternative approach to **catch dominant contributions**

virtual & soft gluons



Soft-virtual corrections

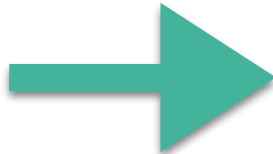
Partonic X-section

$$\Delta(z) = \Delta^{\text{sing}}(z) + \Delta^{\text{hard}}(z)$$

$$z = \frac{q^2}{\hat{s}}$$
$$\mathcal{D}_j \equiv \left(\frac{\ln^j(1-z)}{1-z} \right)_+$$

$$\Delta^{\text{sing}}(z) \equiv \Delta^{\text{SV}}(z) = \Delta_{\delta}^{\text{SV}} \delta(1-z) + \sum_{j=0}^{\infty} \Delta_j^{\text{SV}} \mathcal{D}_j$$

 **Leading in $z \rightarrow 1$** (threshold limit)

$\Delta^{\text{hard}}(z)$: polynomial in $\ln(1-z)$  **sub-leading**

MOTIVATIONS: SV

Partonic X-section: expand around $z \rightarrow 1$ (threshold limit)

$$\Delta(z) = \Delta^{\text{sing}}(z) + \Delta^{\text{hard}}(z)$$

$$z = \frac{q^2}{\hat{s}}$$
$$\mathcal{D}_j \equiv \left(\frac{\ln^j(1-z)}{1-z} \right)_+$$

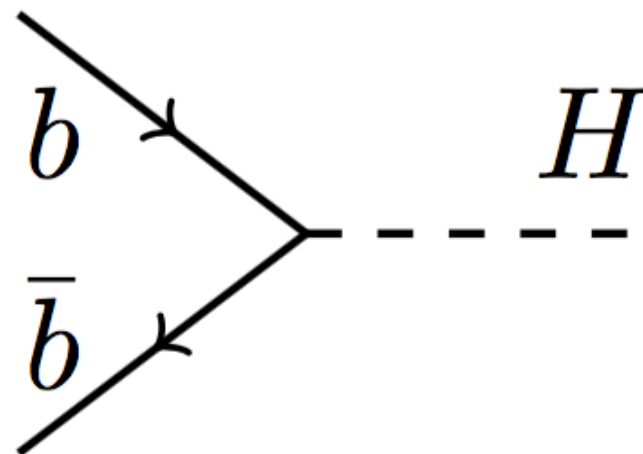
$$\Delta^{\text{sing}}(z) \equiv \Delta^{\text{SV}}(z) = \Delta_{\delta}^{\text{SV}} \delta(1-z) + \sum_{j=0}^{\infty} \Delta_j^{\text{SV}} \mathcal{D}_j$$

Leading in $z \rightarrow 1$

$\Delta^{\text{hard}}(z)$: polynomial in $\ln(1-z)$ $\longrightarrow$ sub-leading

Our focus

GOAL



Existing result: NNLO and partial SV N³LO ['03, '06]



Next obvious and necessary extension

SV corrections to $b\bar{b} \rightarrow H$ cross section
at N³LO QCD

THE PRESCRIPTION

Many methods

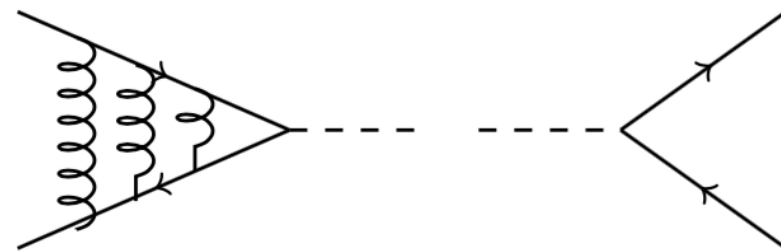
I. Direct evaluation of diagrams

THE PRESCRIPTION

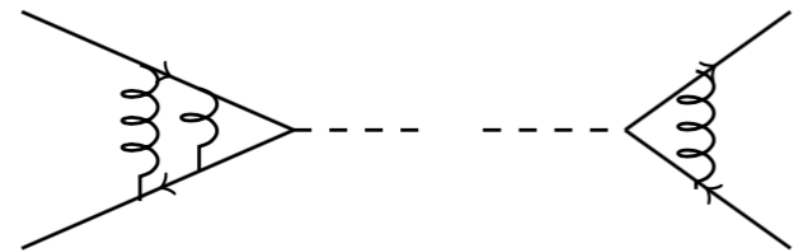
Many methods

I. Direct evaluation of diagrams

virtual {

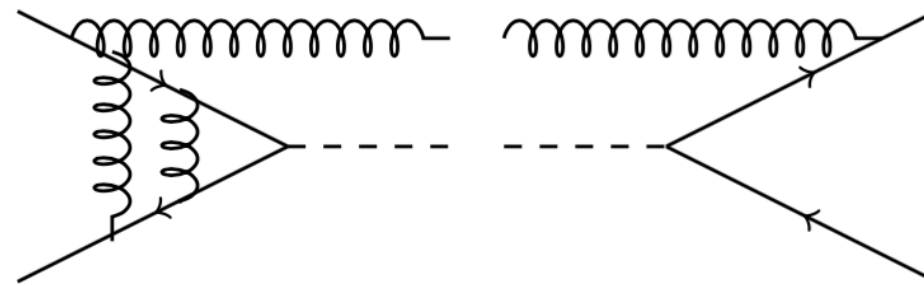


Triple virtual

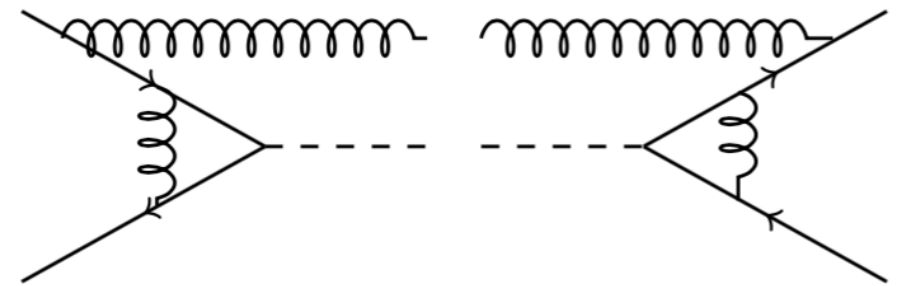


Double virtual

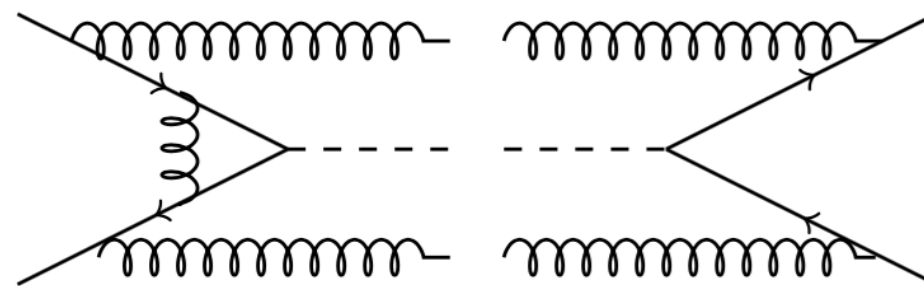
real
emission {



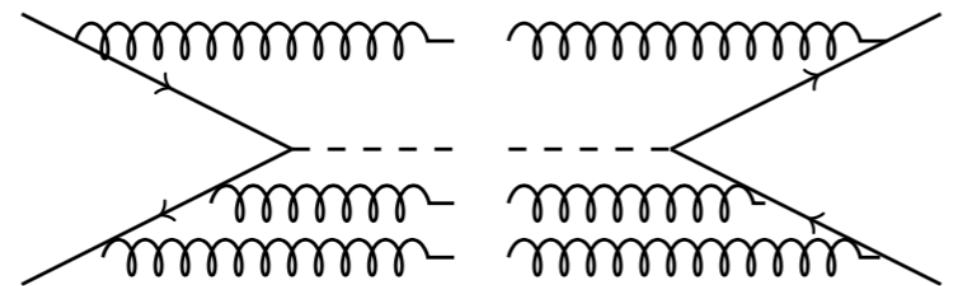
Double virtual real



Real virtual squared



Double real virtual



Triple real squared

THE PRESCRIPTION

Many methods

1. Direct evaluation of diagrams
2. Use factorisation, RGE & Sudakov resum

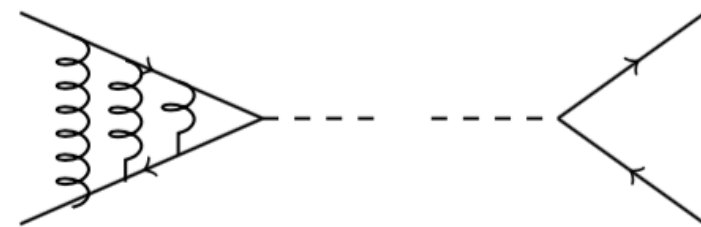
THE PRESCRIPTION

Many methods

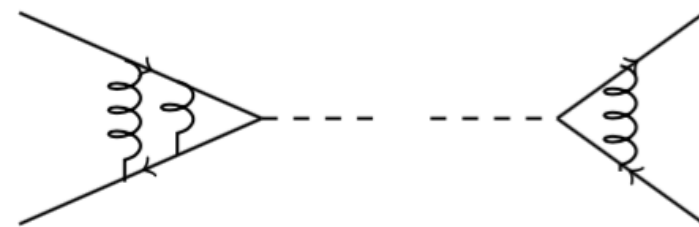
1. Direct evaluation of diagrams

✓ 2. Use factorisation, RGE & Sudakov resum

virtual



Triple virtual



Double virtual

real
emission



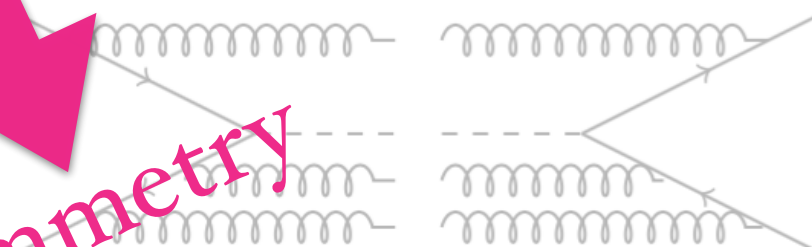
Double virtual real



Real virtual squared



Double real virtual



Triple real squared

Will not compute these!!
Symmetry

MASTER FORMULA

$$\Delta^{\text{SV},I}(z, q^2, \mu_R^2, \mu_F^2) = \mathcal{C} \exp(\Psi^I(z, q^2, \mu_R^2, \mu_F^2, \epsilon)) \big|_{\epsilon=0}$$

[Ravindran]

with

$$\begin{aligned} \Psi^I = & \left(\ln \left[Z^I(\hat{a}_s, \mu_R^2, \mu^2, \epsilon) \right]^2 + \ln \left| \hat{F}^I(\hat{a}_s, Q^2, \mu^2, \epsilon) \right|^2 \right) \delta(1-z) \\ & + 2\Phi^I(\hat{a}_s, q^2, \mu^2, z, \epsilon) - 2\mathcal{C} \ln \Gamma_{II}(\hat{a}_s, \mu^2, \mu_F^2, z, \epsilon) \end{aligned}$$

Required up to N³LO

- Operator renormalisation
- Form factors
- Soft-collinear distribution
- Mass factorisation kernel

MASTER FORMULA

$$\Delta^{\text{SV},I}(z, q^2, \mu_R^2, \mu_F^2) = \mathcal{C} \exp(\Psi^I(z, q^2, \mu_R^2, \mu_F^2, \epsilon)) \big|_{\epsilon=0}$$

[Ravindran]

with

$$\begin{aligned} \Psi^I = & \left(\ln \left[Z^I(\hat{a}_s, \mu_R^2, \mu^2, \epsilon) \right]^2 + \ln \left| \hat{F}^I(\hat{a}_s, Q^2, \mu^2, \epsilon) \right|^2 \right) \delta(1-z) \\ & + 2\Phi^I(\hat{a}_s, q^2, \mu^2, z, \epsilon) - 2\mathcal{C} \ln \Gamma_{II}(\hat{a}_s, \mu^2, \mu_F^2, z, \epsilon) \end{aligned}$$

Recently computed

[Gehrmann, Kara '14]

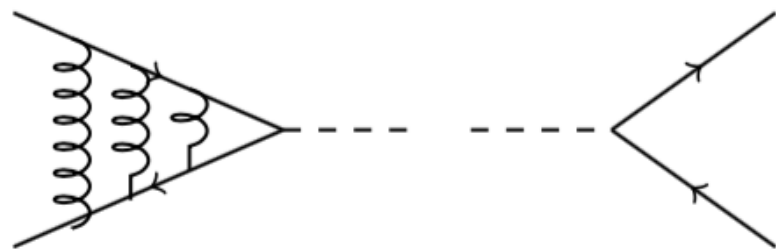
Recently computed

[TA, Mahakhud, Rana, Ravindran '14]

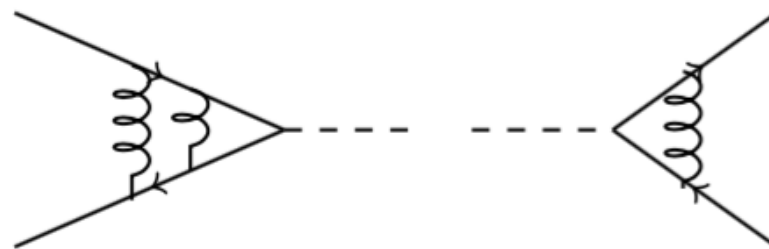
- ✓ Operator renormalisation
- ✓ Form factors
- ✓ Soft-collinear distribution
- ✓ Mass factorisation kernel

FORM FACTORS & SOFT-COLLINEAR DISTR

Form Factors



Triple virtual



Double virtual

[Gehrmann, Kara '14]

Soft-Collinear Distr

Real emission diagrams $|_{gg \rightarrow H} \Leftrightarrow$ Real emission diagrams $|_{b\bar{b} \rightarrow H}$



$$\Phi|_{gg \rightarrow H} = \frac{C_A}{C_F} \Phi|_{b\bar{b} \rightarrow H}$$

- Established up to NNLO

[Ravindran '06]

- We **postulated** the relation even at **N³LO**

[TA, Mahakhud, Rana, Ravindran '14]

- Verified in case of Drell-Yan

[Catani et. al., von Monteuffel et. al. '14]

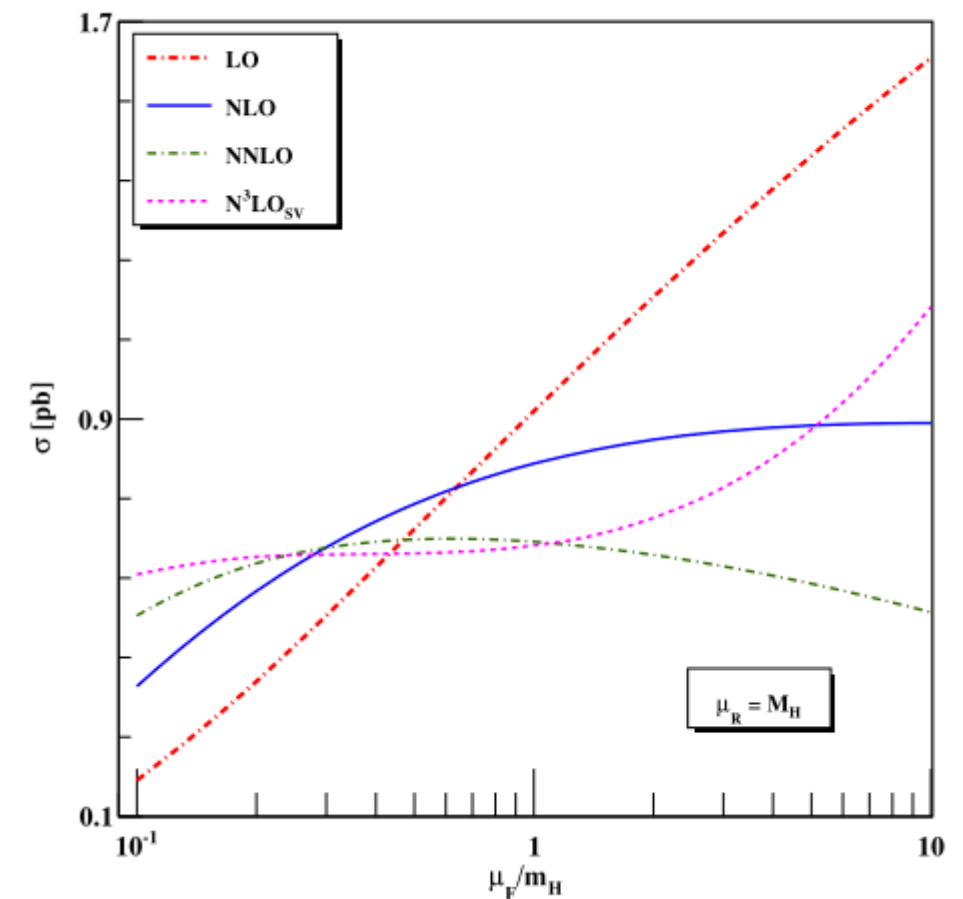
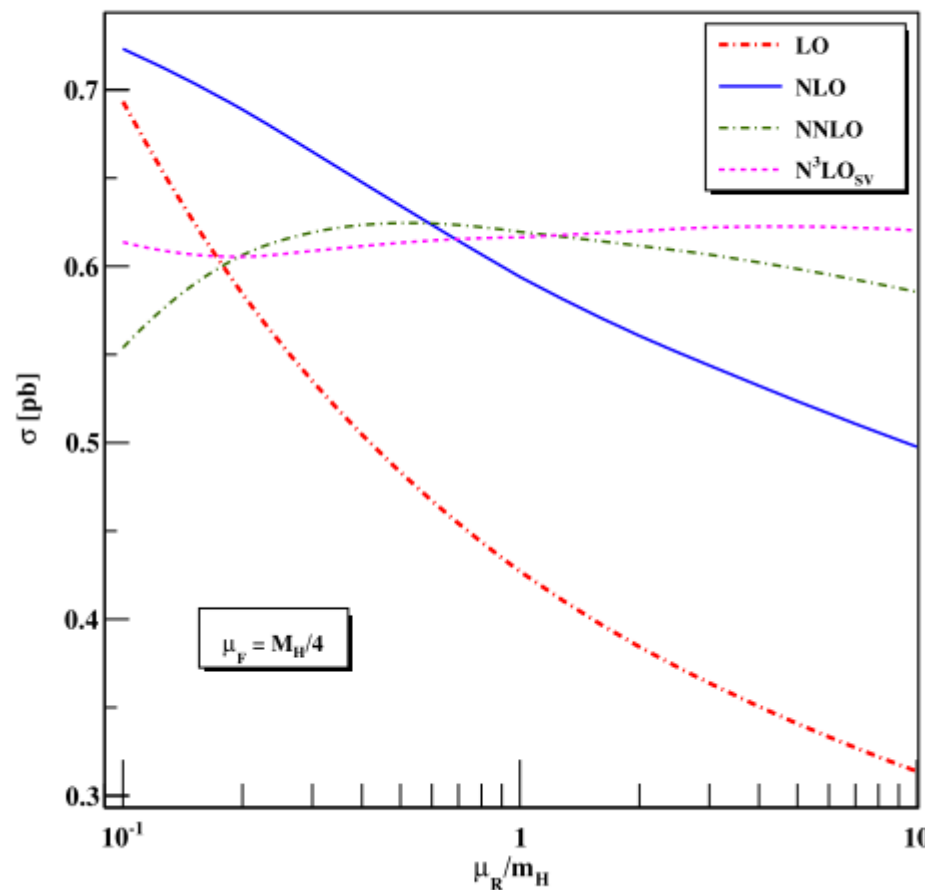
RESULTS

Analytical results at N³LO

- $\Delta^{SV}|_{\delta}$ is the new result
- Uplift the theoretical precision
- Reduces scale uncertainties

$$\Delta_b^{sv,(3)} = \delta(1-z) \left\{ C_A^2 C_F \left(\frac{13264}{315} \zeta_2^3 + \frac{2528}{27} \zeta_2^2 - \frac{1064}{3} \zeta_2 \zeta_3 - 272 \zeta_2 - \frac{400}{3} \zeta_3^2 - \frac{14212}{81} \zeta_3 \right. \right. \\ \left. \left. - 84 \zeta_5 + \frac{68990}{81} \right) + C_A C_F^2 \left(-\frac{20816}{315} \zeta_2^3 - \frac{62468}{135} \zeta_2^2 + \frac{27872}{9} \zeta_2 \zeta_3 + \frac{22106}{27} \zeta_2 \right. \right. \\ \left. \left. + \frac{3280}{3} \zeta_3^2 - \frac{10940}{9} \zeta_3 - \frac{37144}{9} \zeta_5 - \frac{982}{3} \right) + C_A C_F n_f \left(-\frac{6728}{135} \zeta_2^2 + \frac{208}{3} \zeta_2 \zeta_3 \right. \right. \\ \left. \left. + \frac{3368}{81} \zeta_2 + \frac{2552}{81} \zeta_3 - 8 \zeta_5 - \frac{11540}{81} \right) + C_F^3 \left(-\frac{184736}{315} \zeta_2^3 + \frac{152}{5} \zeta_2^2 - 64 \zeta_2 \zeta_3 \right. \right. \\ \left. \left. - \frac{550}{3} \zeta_2 + \frac{10336}{3} \zeta_3^2 - 1188 \zeta_3 + 848 \zeta_5 + \frac{1078}{3} \right) + C_F^2 n_f \left(\frac{12152}{135} \zeta_2^2 - \frac{5504}{9} \zeta_2 \zeta_3 \right. \right. \\ \left. \left. - \frac{2600}{27} \zeta_2 + \frac{4088}{9} \zeta_3 + \frac{5536}{9} \zeta_5 - \frac{70}{9} \right) + C_F n_f^2 \left(\frac{128}{27} \zeta_2^2 - \frac{32}{81} \zeta_2 - \frac{1120}{81} \zeta_3 + \frac{16}{27} \right) \right\} \\ + \mathcal{D}_0 \left\{ C_A^2 C_F \left(-\frac{2992}{15} \zeta_2^2 - \frac{352}{3} \zeta_2 \zeta_3 + \frac{98224}{81} \zeta_2 + \frac{40144}{27} \zeta_3 - 384 \zeta_5 - \frac{594058}{729} \right) \right. \\ \left. + C_A C_F^2 \left(\frac{1408}{3} \zeta_2^2 - 1472 \zeta_2 \zeta_3 + \frac{6592}{3} \zeta_2 + \frac{32288}{3} \zeta_3 + \frac{6464}{3} \right) + C_A C_F n_f \left(\frac{736}{3} \zeta_2^2 \right. \right.$$

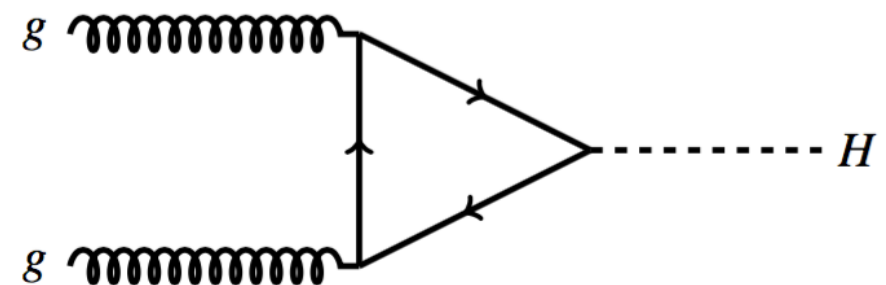
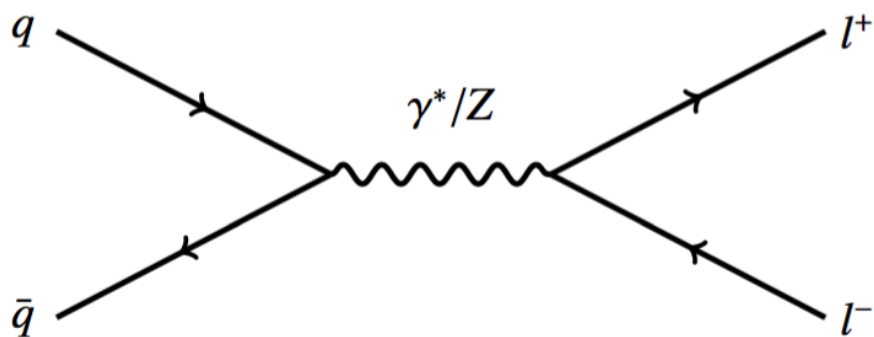
LHC13



Most accurate result till date!

RAPIDITY DISTRIBUTION IN DRELL-YAN & HIGGS PRODUCTIONS AT THRESHOLD N^3 LO QCD

TA, Mandal, Rana & Ravindran
Phys.Rev.Lett. 113, 212003 (2014)



MOTIVATIONS

- DY & Higgs: very important processes
- DY: 1. One of the cleanest processes
2. Crucial role in determining PDF
- Higgs: Yet to confirm the identities of 2012's particle

MOTIVATIONS

- DY & Higgs: very important processes
- DY: 1. One of the cleanest processes
2. Crucial role in determining PDF
- Higgs: Yet to confirm the identities of 2012's particle
 - Differential rapidity distributions: important observable
 - Will be measured at the LHC

MOTIVATIONS

- DY & Higgs: very important processes
- DY: 1. One of the cleanest processes
2. Crucial role in determining PDF
- Higgs: Yet to confirm the identities of 2012's particle
 - Differential rapidity distributions: important observable
 - Will be measured at the LHC
- Call for more precise theoretical results
- Going beyond LO: challenging
- Often fail to compute complete fixed order result

MOTIVATIONS

- DY & Higgs: very important processes
- DY: 1. One of the cleanest processes
2. Crucial role in determining PDF
- Higgs: Yet to confirm the identities of 2012's particle
 - Differential rapidity distributions: important observable
 - Will be measured at the LHC
- Call for more precise theoretical results
- Going beyond LO: challenging
- Often fail to compute complete fixed order result

Catch dominant contributions through SV approx

Rapidity Distribution

$$\Delta_Y(z_1, z_2) = \Delta_Y^{\text{sing}}(z_1, z_2) + \Delta_Y^{\text{hard}}(z_1, z_2)$$

$$Y \equiv \frac{1}{2} \log \left(\frac{x_1^0}{x_2^0} \right) \quad \tau \equiv x_1^0 x_2^0$$

$$z_i = \frac{x_i^0}{x_i}$$

$$\begin{aligned} \Delta_Y^{\text{SV}} = & \Delta_Y^{\text{SV}}|_{\delta\delta} \delta(1-z_1)\delta(1-z_2) + \sum_{j=0}^{2j-1} \Delta_Y^{\text{SV}}|_{\delta\mathcal{D}_j} \delta(1-z_2)\mathcal{D}_j \\ & + \sum_{j=0}^{2j-1} \Delta_Y^{\text{SV}}|_{\delta\overline{\mathcal{D}}_j} \delta(1-z_2)\overline{\mathcal{D}}_j + \sum_{j,l} \Delta_Y^{\text{SV}}|_{\mathcal{D}_j\overline{\mathcal{D}}_l} \mathcal{D}_j\overline{\mathcal{D}}_l. \end{aligned}$$

 **Leading in** $z_1 \rightarrow 1, z_2 \rightarrow 1$ (threshold limit)

$\Delta_Y^{\text{hard}}(z_1, z_2)$: polynomial in $\ln(1-z_i)$  **sub-leading**

GOAL

Existing result: NNLO and partial SV N³LO ['03, '07]



Next obvious and necessary extension

SV corrections to rapidity for

1. Higgs in $gg \rightarrow H$

2. Leptonic pair in DY

at N³LO QCD

THE PRESCRIPTION

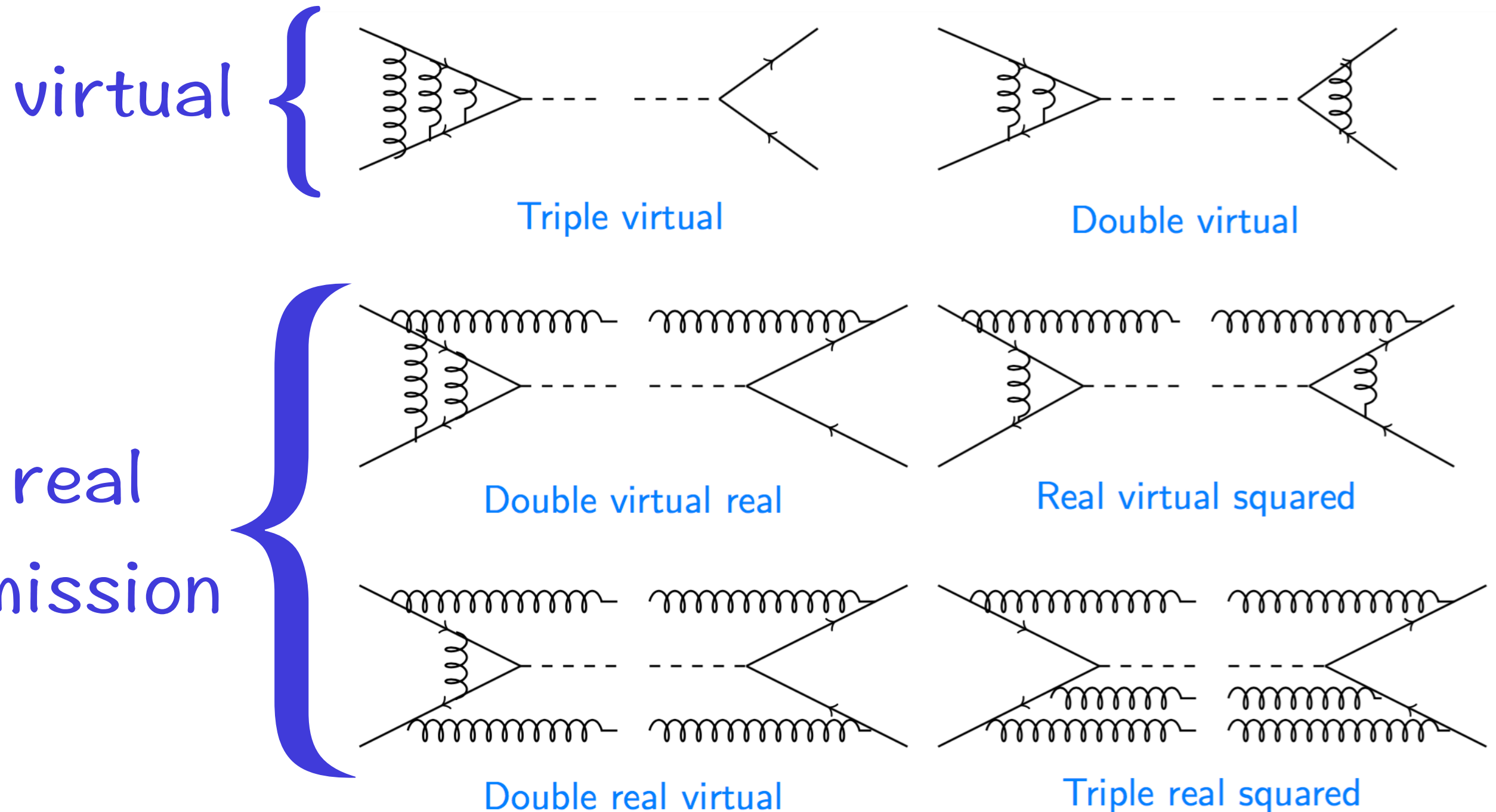
Many methods

I. Direct evaluation of diagrams

THE PRESCRIPTION

Many methods

I. Direct evaluation of diagrams



THE PRESCRIPTION

Many methods

1. Direct evaluation of diagrams
2. Use factorisation, RGE & Sudakov resum

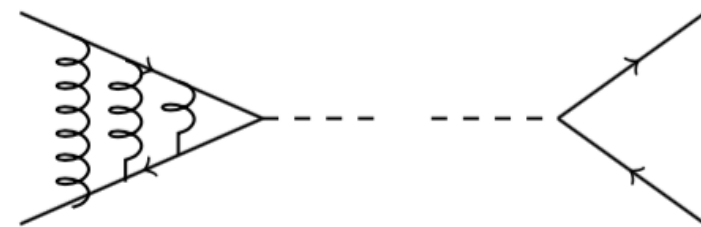
THE PRESCRIPTION

Many methods

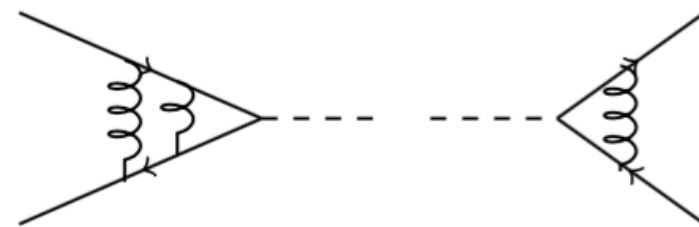
1. Direct evaluation of diagrams

✓ 2. Use factorisation, RGE & Sudakov resum

virtual



Triple virtual



Double virtual

real
emission



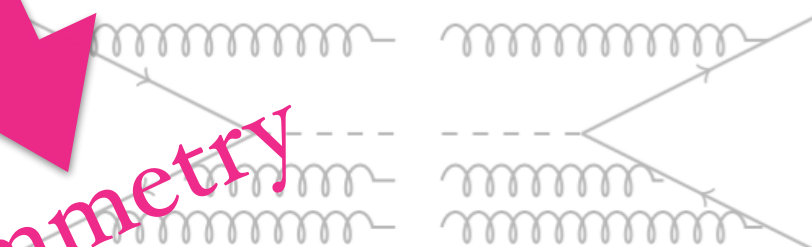
Double virtual real



Real virtual squared



Double real virtual



Triple real squared

Will not compute these!!
Symmetry

MASTER FORMULA

$$\Delta_Y^{\text{SM}}(z_1, z_2, q^2, \mu_R^2, \mu_F^2) = \mathcal{C} \exp \left(\Psi_Y(z_1, z_2, q^2, \mu_R^2, \mu_F^2, \epsilon) \right) \Big|_{\epsilon=0}$$

[Ravindran]

$$\begin{aligned} \Psi_Y = & \left(\ln \left[Z(\hat{a}_s, \mu_R^2, \mu^2, \epsilon) \right]^2 + \ln \left| \mathcal{F}(\hat{a}_s, Q^2, \mu^2, \epsilon) \right|^2 \right) \delta(1 - z_1) \delta(1 - z_2) \\ & + 2\Phi_Y(\hat{a}_s, q^2, \mu^2, z_1, z_2, \epsilon) - \mathcal{C} \ln \Gamma(\hat{a}_s, \mu^2, \mu_F^2, z_1, \epsilon) \delta(1 - z_2) \\ & - \mathcal{C} \ln \Gamma(\hat{a}_s, \mu^2, \mu_F^2, z_2, \epsilon) \delta(1 - z_1). \end{aligned}$$

Required up to N³LO

- Operator renormalisation
- Form factors
- Soft-collinear distribution
- Mass factorisation kernel

MASTER FORMULA

$$\Delta_Y^{\text{SM}}(z_1, z_2, q^2, \mu_R^2, \mu_F^2) = \mathcal{C} \exp \left(\Psi_Y(z_1, z_2, q^2, \mu_R^2, \mu_F^2, \epsilon) \right) \Big|_{\epsilon=0}$$

[Ravindran]

$$\begin{aligned} \Psi_Y = & \left(\ln \left[Z(\hat{a}_s, \mu_R^2, \mu^2, \epsilon) \right]^2 + \ln \left| \mathcal{F}(\hat{a}_s, Q^2, \mu^2, \epsilon) \right|^2 \right) \delta(1 - z_1) \delta(1 - z_2) \\ & + 2\Phi_Y(\hat{a}_s, q^2, \mu^2, z_1, z_2, \epsilon) - \mathcal{C} \ln \Gamma(\hat{a}_s, \mu^2, \mu_F^2, z_1, \epsilon) \delta(1 - z_2) \\ & - \mathcal{C} \ln \Gamma(\hat{a}_s, \mu^2, \mu_F^2, z_2, \epsilon) \delta(1 - z_1). \end{aligned}$$

Unavailable

- ✓ Operator renormalisation
- ✓ Form factors
- Soft-collinear distribution
- ✓ Mass factorisation kernel

SOFT-COLLINEAR DISTRIBUTION

- Demanding finiteness of rapidity & RG invariance

→ poles of SCD

- Determining finite part

→ requires explicit computations

- However, it has been found

$$\Phi_Y \Leftrightarrow \Phi_{X\text{section}}$$

[Ravindran, van Neerven, Smith]

- SCD for Xsection is used to obtain Φ_Y at $N^3\text{LO}$

[TA, Mandal, Rana, Ravindran]

RESULTS

Analytical results at N³LO

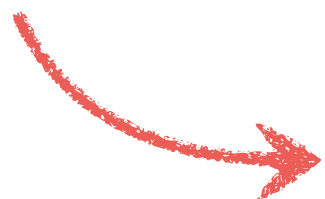
- $\Delta_Y^{\text{SV}}|_{\delta\delta}$ is the new result
- Uplift the theoretical precision
- Reduces scale uncertainties

$$\begin{aligned} \Delta_{Y,gg,3}^{H,\text{SV}} = & \delta(1-z_1)\delta(1-z_2) \left[C_A^3 \left\{ \frac{215131}{81} + \frac{1364}{9}\zeta_5 - \frac{54820}{27}\zeta_3 + \frac{1600}{3}\zeta_3^2 + \frac{41914}{27}\zeta_2 \right. \right. \\ & - 88\zeta_2\zeta_3 + \frac{40432}{135}\zeta_2^2 + \frac{12032}{105}\zeta_2^3 \Big\} + n_f C_A^2 \left\{ -\frac{98059}{81} + \frac{1192}{9}\zeta_5 + \frac{2536}{27}\zeta_3 \right. \\ & - \frac{7108}{27}\zeta_2 - 272\zeta_2\zeta_3 + \frac{1240}{27}\zeta_2^2 \Big\} + n_f C_F C_A \left\{ -\frac{63991}{81} + 160\zeta_5 + 400\zeta_3 - \frac{2270}{9}\zeta_2 \right. \\ & + 288\zeta_2\zeta_3 + \frac{176}{45}\zeta_2^2 \Big\} + n_f C_F^2 \left\{ \frac{608}{9} - 320\zeta_5 + \frac{592}{3}\zeta_3 \right\} + n_f^2 C_A \left\{ \frac{2515}{27} + \frac{112}{3}\zeta_3 \right. \\ & - \frac{64}{3}\zeta_2 - \frac{208}{15}\zeta_2^2 \Big\} + n_f^2 C_F \left\{ \frac{8962}{81} - \frac{224}{3}\zeta_3 - \frac{184}{9}\zeta_2 - \frac{32}{45}\zeta_2^2 \right\} \\ & + \log\left(\frac{q^2}{\mu_F^2}\right) C_A^3 \left\{ -\frac{8284}{9} + 224\zeta_5 + \frac{10408}{9}\zeta_3 - \frac{22528}{27}\zeta_2 - 224\zeta_2\zeta_3 - \frac{1276}{3}\zeta_2^2 \right\} \\ & + \log\left(\frac{q^2}{\mu_F^2}\right) n_f C_A^2 \left\{ \frac{4058}{9} - \frac{1120}{9}\zeta_3 + \frac{8488}{27}\zeta_2 + \frac{232}{3}\zeta_2^2 \right\} \\ & + \log\left(\frac{q^2}{\mu_F^2}\right) n_f C_F C_A \left\{ \frac{616}{9} - \frac{352}{9}\zeta_3 + 72\zeta_2 \right\} + \log\left(\frac{q^2}{\mu_F^2}\right) n_f C_F^2 \{-4\} \end{aligned}$$

Numerical Impacts for Higgs

	$\delta\delta$	$\delta\overline{\mathcal{D}}_0$	$\delta\overline{\mathcal{D}}_1$	$\delta\overline{\mathcal{D}}_2$	$\delta\overline{\mathcal{D}}_3$	$\delta\overline{\mathcal{D}}_4$	$\delta\overline{\mathcal{D}}_5$	$\mathcal{D}_0\overline{\mathcal{D}}_0$	$\mathcal{D}_0\overline{\mathcal{D}}_1$
%	73.3	16.0	9.1	31.4	1.0	-9.9	-23.1	-13.7	-10.7

	$\mathcal{D}_0\overline{\mathcal{D}}_2$	$\mathcal{D}_0\overline{\mathcal{D}}_3$	$\mathcal{D}_0\overline{\mathcal{D}}_4$	$\mathcal{D}_1\overline{\mathcal{D}}_1$	$\mathcal{D}_1\overline{\mathcal{D}}_2$	$\mathcal{D}_1\overline{\mathcal{D}}_3$	$\mathcal{D}_2\overline{\mathcal{D}}_2$
%	-0.3	3.1	7.3	-0.2	3.8	8.6	4.2

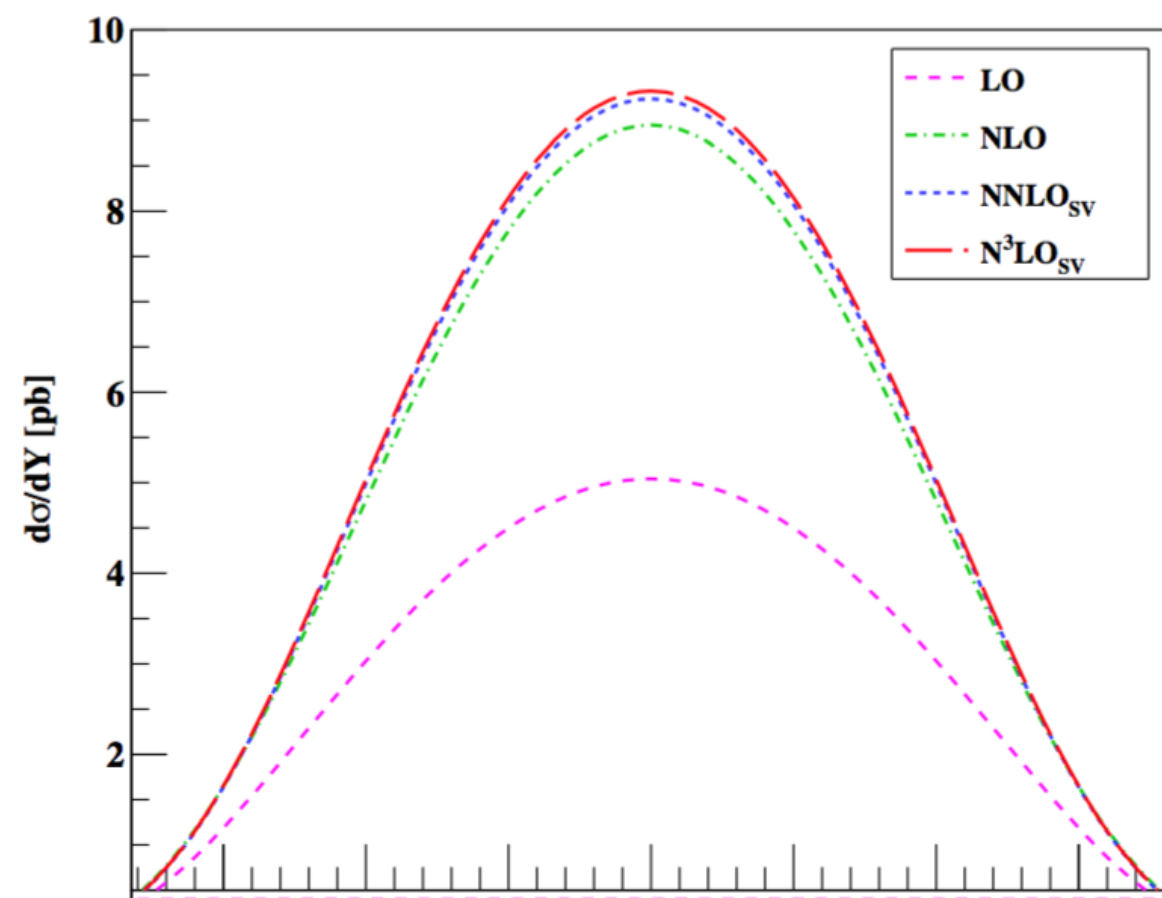


$\Delta_Y^{\text{SV}}|_{\delta\delta}$ has the largest contribution!

RESULTS

Y	0.0	0.4	0.8	1.2	1.6
NNLO	11.21	10.96	10.70	9.13	7.80
NNLO _{SV}	9.81	9.61	8.99	8.00	6.71
NNLO _{SV} (A)	10.67	10.46	9.84	8.82	7.48
N ³ LO _{SV}	11.62	11.36	11.07	9.44	8.04
N ³ LO _{SV} (A)	11.88	11.62	11.33	9.70	8.30
$K3$	2.31	2.29	2.36	2.21	2.17

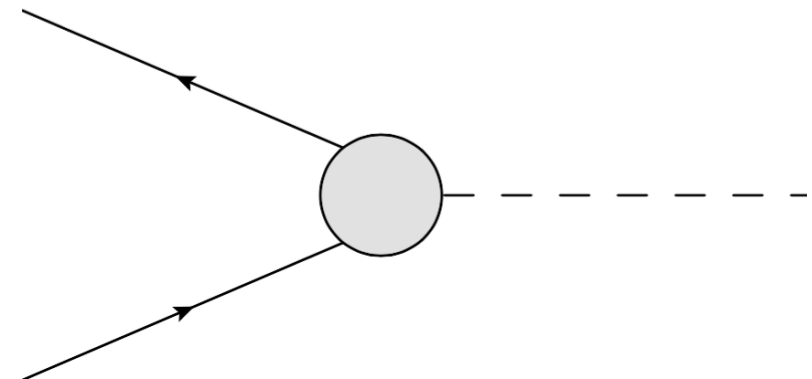
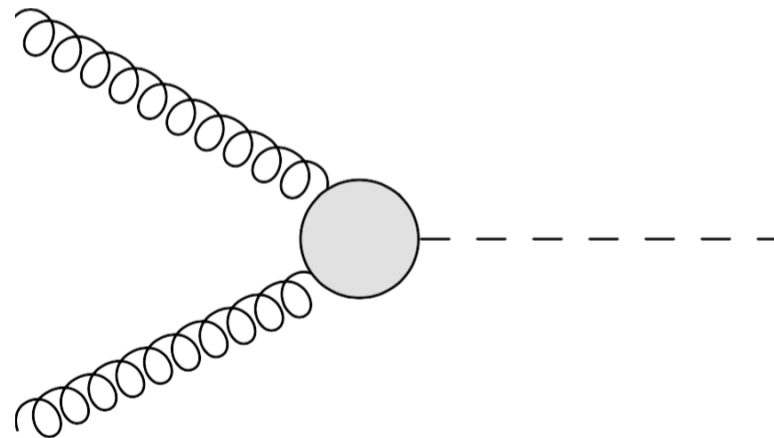
Most accurate results till date!



PSEUDO SCALAR FORM FACTORS AT 3-LOOP QCD

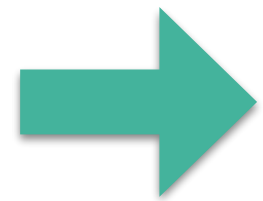
TA, Gehrmann, Mathews, Rana & Ravindran
JHEP 1511, 169 (2015)

TA, Kumar, Mathews, Rana & Ravindran
Eur. Phys. J. C (2016) 76:355



MOTIVATIONS

- **MSSM** has richer Higgs sector



5 physical Higgs bosons

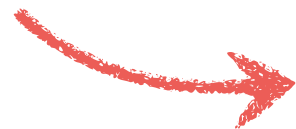


neutral h, H, A

charged $H^\pm$

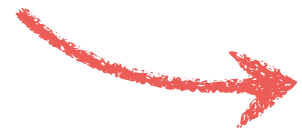
$$\begin{cases} h, H : \text{CP even} \\ A : \text{CP odd} \end{cases}$$

- Pseudo-scalar: **important at the LHC**



similar to scalar Higgs

- ~~New resonance at 750 GeV~~



~~New scalar / Spin-2 / Pseudo-scalar?~~

- Searches at the LHC **demands precise theoretical predictions**

MOTIVATIONS

CP even

Inclusive production cross section at N^3LO QCD

[Anastasiou, Duhr, Dulat, Furlan, Herzog, Mistlberger]

CP odd

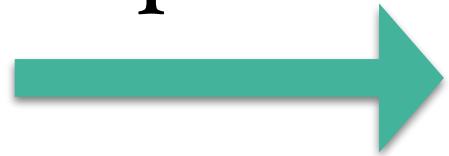
Inclusive production cross section at $NNLO$ QCD

[Harlander, Kilgore; Anastasiou, Melnikov]

What is next?

Go **beyond $NNLO$** for CP odd!

requires



1. Virtual correction at 3-loop
2. Real corrections at N^3LO

GOAL

CP even

Inclusive production cross section at N^3LO QCD

[Anastasiou, Duhr, Dulat, Furlan, Herzog, Mistlberger]

CP odd

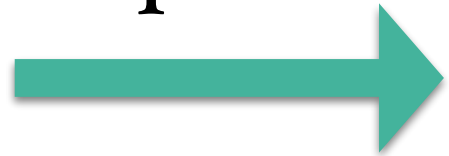
Inclusive production cross section at $NNLO$ QCD

[Harlander, Kilgore; Anastasiou, Melnikov]

What is next?

Go **beyond $NNLO$** for CP odd!

requires



1. Virtual correction at 3-loop
2. Real corrections at N^3LO

Our GOAL

EFFECTIVE LAGRANGIAN

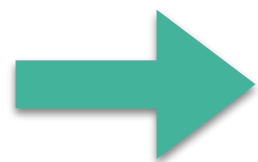
Original Theory

Pseudo scalar couples to quarks through **Yukawa**

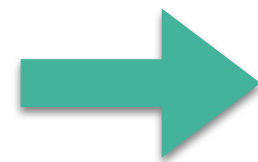
Effective Theory

[Chetyrkin, Kniehl, Steinhauser and Bardeen]

Simplifications occur if $m_A \ll 2m_t$



effective theory by **int out top loop**



massless QCD

$$\mathcal{L}_{\text{eff}}^A = \Phi^A \left[-\frac{1}{8} C_G O_G - \frac{1}{2} C_J O_J \right]$$

$$O_G(x) = G_a^{\mu\nu} \tilde{G}_{a,\mu\nu} \equiv \epsilon_{\mu\nu\rho\sigma} G_a^{\mu\nu} G_a^{\rho\sigma}$$

$$O_J(x) = \partial_\mu (\bar{\psi} \gamma^\mu \gamma_5 \psi)$$

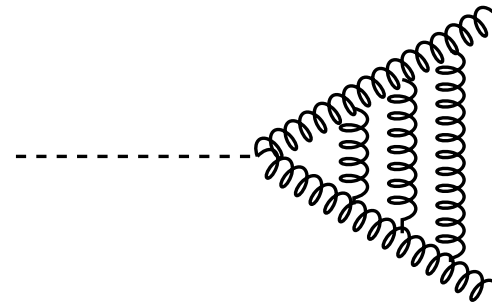
$$C_G = -a_s 2^{\frac{5}{4}} G_F^{\frac{1}{2}} \cot\beta$$

$$C_J = - \left[a_s C_F \left(\frac{3}{2} - 3 \ln \frac{\mu_R^2}{m_t^2} \right) + a_s^2 C_J^{(2)} + \dots \right] C_G$$

Qgraf

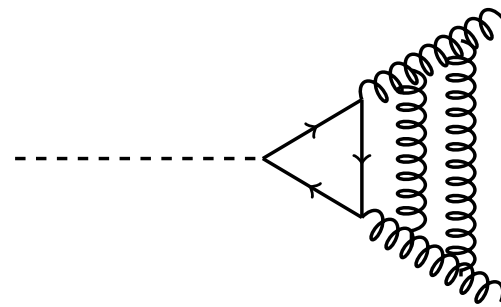
[P. Nogueira]

1586



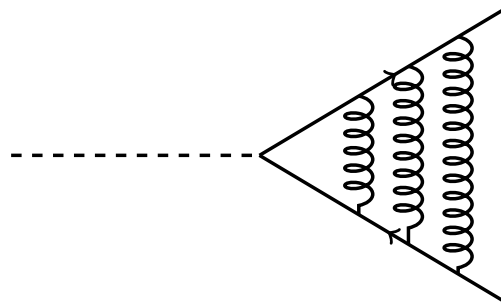
type

447



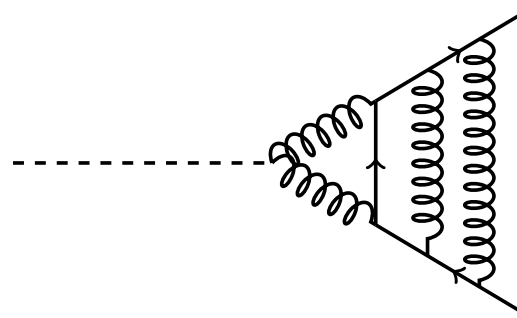
type

244



type

400



type

γ_5 PRESCRIPTION

- Color simplification in $SU(N)$ theory
 - Lorentz & Dirac algebra in d -dimensions
- } in-house codes
- What about γ_5 & $\varepsilon_{\mu\nu\rho\sigma}$?

➡ inherently 4-dimensional

➡ problem of defining in $d (\neq 4)$ dimensions

Prescription

$$\gamma_5 = i \frac{1}{4!} \varepsilon_{\nu_1 \nu_2 \nu_3 \nu_4} \gamma^{\nu_1} \gamma^{\nu_2} \gamma^{\nu_3} \gamma^{\nu_4}$$

$$\{\gamma_5, \gamma^\mu\} \neq 0$$

[t Hooft and Veltman]

$$\varepsilon_{\mu_1 \nu_1 \lambda_1 \sigma_1} \varepsilon^{\mu_2 \nu_2 \lambda_2 \sigma_2} = 4! \delta_{[\mu_1}^{\mu_2} \dots \delta_{\sigma_1]}^{\sigma_2}$$

Treat in d -dimensions

IBP & LI

- Removing unphysical DOF of gluons
 1. Internal: Ghost loops
 2. External: Polarization sum in axial gauge
- Results

Thousands of 3-loop scalar integrals!



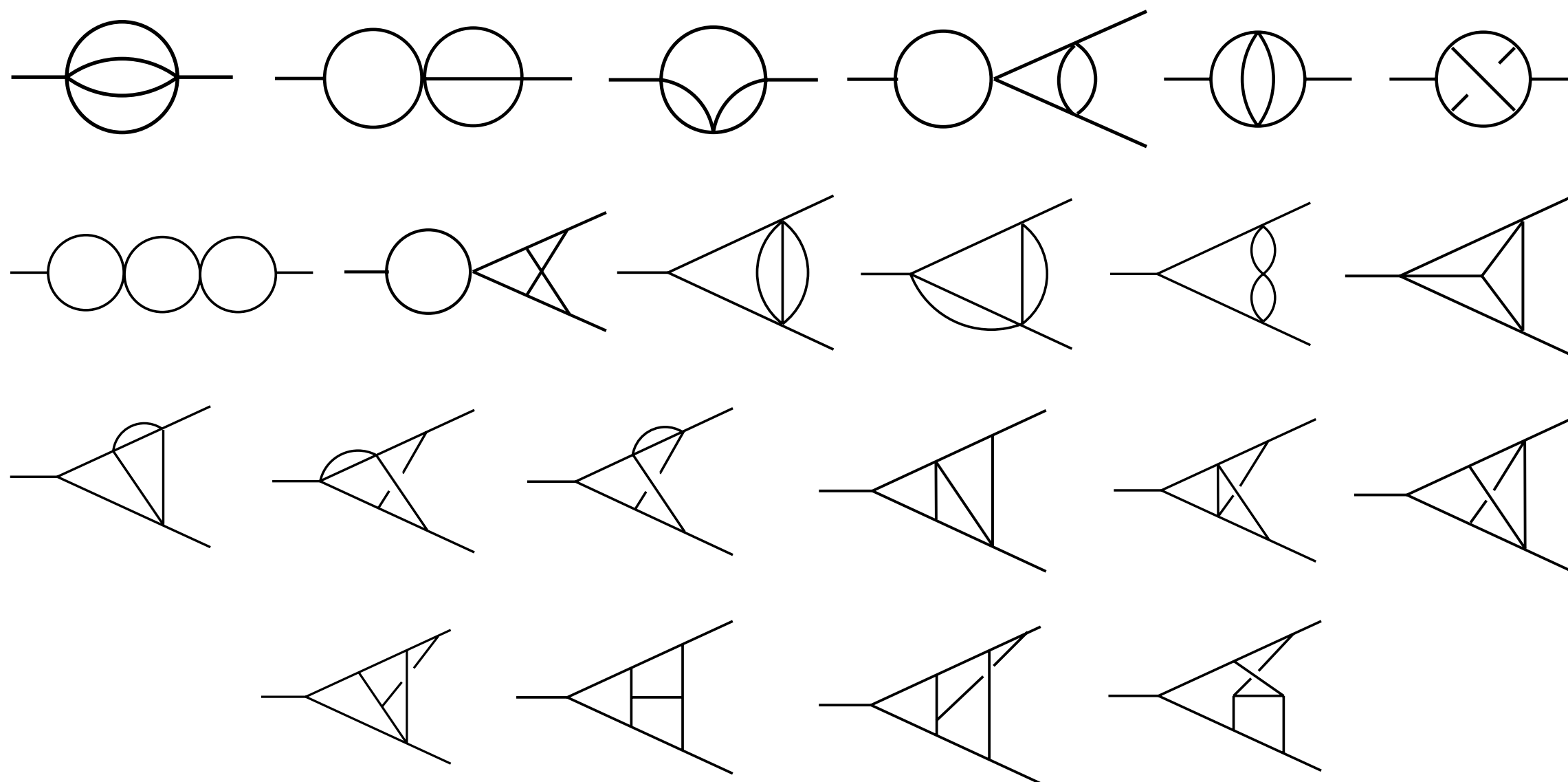
IBP & LI identities

[Chetyrkin, Tkachov; Gehrmann, Remeddy]

22 Master Integrals (topologically different)

Master Integrals

[Gehrmann, Huber & Maitre '05;
Gehrmann, Heinrich, Huber & Studerus '06;
Heinrich, Huber & Maitre '08;
Heinrich, Huber, Kosower & Smirnov '09;
Lee, Smirnov & Smirnov '10]



Results

Unrenormalized 3-loop FF in power series of ϵ ($d = 4 + \epsilon$)

COUPLING CONS RENORM

- Dimensional Regularization

$$d = 4 + \epsilon$$

- Coupling Constant Renorm

$$\hat{a}_s S_\epsilon = \left(\frac{\mu^2}{\mu_R^2} \right)^{\epsilon/2} Z_{a_s} a_s$$

$$Z_{a_s} = 1 + a_s \left[\frac{2}{\epsilon} \beta_0 \right] + a_s^2 \left[\frac{4}{\epsilon^2} \beta_0^2 + \frac{1}{\epsilon} \beta_1 \right] + a_s^3 \left[\frac{8}{\epsilon^3} \beta_0^3 + \frac{14}{3\epsilon^2} \beta_0 \beta_1 + \frac{2}{3\epsilon} \beta_2 \right] + \dots$$

β_i QCD beta functions

OPERATOR RENORM

- Overall Operator Renorm

O_G & O_J requires additional renorm



$$[O_G]_R = Z_{GG} [O_G]_B + Z_{GJ} [O_J]_B$$

$$[O_J]_R = Z_5^s Z_{\overline{MS}}^s [O_J]_B$$

- * O_G mixes under renorm
- * Finite renorm $Z_5^s \longleftrightarrow \gamma_5$ prescription
- * Universal IR pole structure $\longrightarrow Z_{ij}$
 $\longrightarrow$ New methodology

RESULTS

- 3-loop pseudo-scalar FF
- Operator renormalisation constants
- Corresponding anomalous dimensions

$$\mu_R^2 \frac{d}{d\mu_R^2} Z_{ij} \equiv \gamma_{ik} Z_{kj}$$

- Using these, we obtain renormalised FF

Most accurate results till date!

AXIAL ANOMALY RELATION

Axial Anomaly

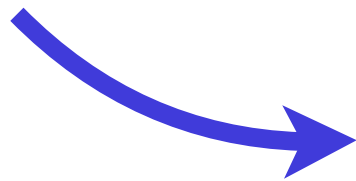
$$[O_J]_R = a_s \frac{n_f}{2} [O_G]_R$$



RG Invariance

$$\gamma_{JJ} = \frac{\beta}{a_s} + \gamma_{GG} + a_s \frac{n_f}{2} \gamma_{GJ}$$

Our results are in agreement with this in $\epsilon \rightarrow 0$



Crucial check

- Soft-virtual cross section at $N^3\text{LO}$
and

Threshold resum cross section at $N^3\text{LL}$

[TA, Kumar, Mathews, Rana & Ravindran]

- Approximate $N^3\text{LO} + N^3\text{LL}'$ cross section using SCET

[TA, Bonvini, Kumar, Mathews, Rottoli, Rana & Ravindran]

- For total inclusive production cross section, it is an important ingredient.

CONCLUSIONS

Most precise predictions for

1. Xsection of Higgs production in bottom annihilation
2. Rapidity of Higgs and DY pair
3. Pseudo-scalar Form Factors at 3-loop

Scale dependence is under control

These will play important role at the LHC

Thank you

ধন্যবাদ