Electric Dipole Moments as Probes of $B$ Anomaly

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The measurements of the lepton flavor universality (LFU) in $B(\bar{B} \to D^{(*)} l \nu)$ indicate a significant deviation from the standard model prediction at a 3–4 $\sigma$ level, revealing a violation of the LFU ($R_{D^{(*)}}$ anomaly). It is known that the $R_{D^{(*)}}$ anomaly can be easily accommodated by an $SU(2)_L$-singlet vector leptoquark (LQ) coupled primarily to third-generation fermions, whose existence is further motivated by a partial gauge unification. In general, such a LQ naturally leads to additional $CP$-violating phases in the LQ interactions. In this Letter, we point out that the current $R_{D^{(*)}}$ anomaly prefers the $CP$-violating interaction although $B(\bar{B} \to D^{(*)} l \nu)$ is a $CP$-conserving observable. The $CP$-violating LQ predicts a substantial size of the bottom-quark electric dipole moment (EDM), the chromo-EDM, and also the tau-lepton EDM. Eventually, at low energy, the nucleon and electron EDMs are induced. Therefore, we conclude that the $R_{D^{(*)}}$ anomaly with the $SU(2)_L$-singlet vector LQ provides unique predictions: neutron and proton EDMs with opposite signs and a magnitude of $O(10^{-27})$ e cm, with a null electron EDM signal. These EDMs could serve as crucial indicators in future experiments.

I. INTRODUCTION

In the near future, the sensitivities of precision measurements for the elementary particles, particularly $B$ physics and the electric dipole moments (EDMs), are expected to be improved by an order of magnitude. Many kinds of new physics models will undoubtedly be probed through these improvements.

Currently, a significant deviation from the standard model (SM) prediction has been reported by the BaBar, LHCb, Belle, and Belle II experiments [1–13], in measurements of the lepton flavor universality (LFU) in $\bar{B} \to D^{(*)} l \nu$. Violation of the LFU is represented by

$$R_{D^{(*)}} = \frac{B(\bar{B} \to D^{(*)} l \nu)}{B(\bar{B} \to D^{(*)} l \overline{\nu})},$$

where $l$ represents an average of the leptons. The up-to-date world average of the data [14, 15] is

$$R_D^{\exp} = 0.357 \pm 0.029, \quad R_{D^{*}}^{\exp} = 0.284 \pm 0.012,$$

while an up-to-date SM prediction [16–19] is

$$R_D^{SM} = 0.290 \pm 0.003, \quad R_{D^{*}}^{SM} = 0.248 \pm 0.001,$$

which implies more than 4$\sigma$ level tension.

This $R_{D^{(*)}}$ anomaly naively suggests the existence of $O(1)$ TeV new physics in the $b \to c \ell \nu$ process, and various kinds of models have been proposed [19, 20]. A new physics candidate is an $SU(2)_L$-singlet vector leptoquark (LQ), dubbed as $U_1$ LQ. The $U_1$ LQ hypothesis has been widely discussed in connection with a partial gauge unification [21–23] as well as the related flavor processes and the LHC phenomenology have been studied [24, 25]. These new physics predictions will be tested in the ongoing Belle II [26] and LHCb experiments [27]. One should note that to avoid the strict constraint from $K_L \to \mu e$ measurements [28, 29], (elaborate) $U(2)$ flavor symmetries have been considered for a successful interpretation of the $R_{D^{(*)}}$ anomaly [30–33]. In that case, the $U_1$ LQ couples primarily to third-generation fermions.

The LQ model naturally brings a $CP$-violating (CPV) phase, which comes from the rotation matrices to the mass bases of the left- and right-handed quark and lepton fields that are not aligned in general. In this Letter, it will be clarified that the CPV phase is necessary to accommodate the $R_{D^{(*)}}$ anomaly, and this phase also induces the sizable nucleon EDMs at the low energy, which will be testable in the near future (see Fig. 1 for the Feynman diagrams). Although Refs. [34, 35] investigated the EDMs in the vector-LQ model in light of the $R_{D^{(*)}}$ anomaly, they focused on the parameter benchmark points and the necessity of the CPV phase was unclear. On the other hand, it is known that there is no robust correlation be-

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FIG. 1. The vector-LQ ($U_1$) contributions to $R_{D^{(*)}}$ (left diagram) and the (chromo-) EDMs for the bottom-quark and tau-lepton (right diagram).
between the $R_{D(c)}$ anomaly and EDMs in scalar LQ models [34, 36–39].

II. LQ MODEL

We consider a simplified $U_1$ LQ scenario with a $U(2)$ flavor symmetry. The relevant fermion interactions are described by

$$\mathcal{L} = \left(\beta_L^{ij}\bar{d}_i\gamma_\mu P_L j_j + \beta_R^{ij}\bar{d}_i\gamma_\mu P_R e_j\right)U^\dagger_4 + \text{h.c.},$$

(4)

with $P_{L/R} = (1 \pm \gamma_5)/2$ in the fermion mass eigenbasis. Although additional vector-like fermions are needed in Eq. (4) to obtain the ideal flavor structure in the UV complete model [40], we focus on the $3 \times 3$ flavor structures. This simplification is valid to consider the EDMs, and we will discuss this point in Sec. III D.

We consider the following flavor texture [23, 40]

$$\beta_L^{ij} \simeq \beta_L^{33} \begin{pmatrix} 0 & 0 & -c_d s_e s_x \sqrt{\frac{V_{te}}{V_{tr}}} \\ 0 & 0 & c_d s_q s_x \\ 0 & 0 & c_x \end{pmatrix},$$

$$\beta_R^{ij} \simeq \beta_R^{33} e^{i\phi_R} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{pmatrix},$$

(5)

where $c_d \approx 0.98$, corresponding to a case of $s_{l_2} \simeq s_\tau \simeq 0$ in the literature. Here, $s_\tau$ and $c_\tau$ represent flavor rotations $\sin \theta_\tau$ and $\cos \theta_\tau$ to bring the SM fermions to their mass eigenbasis. Note that $|\beta_L^{33}| \approx |\beta_R^{33}|$ results from the gauge symmetry in the UV complete model. In this setup, $\phi_d$ is an arbitrary CPV phase; the other CPV phases can be absorbed by a redefinition of $\phi_d$ [41]. Therefore, the relative phase between $\beta_L$ and $\beta_R$ interactions plays an important role in the CPV observables.

In our analysis, only three parameters are relevant to the phenomenology: $\beta_L^{33}/m_{U_1}$, $\beta_R^{32}/\beta_L^{33} (= c_d s_q s_x/c_x)$, and $\phi_R$.

III. EDMS AND OTHER OBSERVABLES

In this section, we concisely summarize the phenomenological effects of the $U_1$ LQ.

First, we focus on the LQ contributions to EDMs. The effective Lagrangian for the EDM ($d_f$) and chromo-EDM interactions ($\tilde{d}_f$) are expressed as

$$\mathcal{L}_{\text{eff}} = -\frac{i}{2} \sum_f \left( d_f \mathcal{J}_{\mu \nu} \gamma_5 f F_{\mu \nu} + g_s \tilde{d}_f \mathcal{J}_{\mu \nu} T^a \gamma_5 f G_{\mu \nu}^a \right),$$

(6)

with $\mathcal{J}_{\mu \nu} = \frac{i}{2} \mathcal{J}[\gamma_\mu, \gamma_\nu]$. Based on Refs. [35, 42, 43], the $U_1$ LQ contributions to the tau-lepton and bottom-quark (chromo-) EDMs are (see Fig. 1 right diagram)

$$d_\tau = -\frac{3e}{8\pi^2 m_{U_1}} m_b \text{Im} \left[ \beta_L^{33} (\beta_R^{33})^* \right],$$

$$d_b(\Lambda_{\text{LQ}}) = -\frac{5e}{24\pi^2 m_{U_1}} m_\tau \text{Im} \left[ \beta_L^{33} (\beta_R^{33})^* \right],$$

$$\tilde{d}_\tau(\Lambda_{\text{LQ}}) = -\frac{1}{8\pi^2 m_{U_1}} m_\tau \text{Im} \left[ \beta_L^{33} (\beta_R^{33})^* \right],$$

(7)

(8)

(9)

and there is no contribution to the other EDMs at the LQ mass scale, $\mu = \Lambda_{\text{LQ}}$. Note that the Weinberg operator $(GG\bar{G})$ would be induced at two-loop level, but it is suppressed by $m_\mu m_\tau/m_{U_1}^2$, and we discarded it [37]. While there is no QCD renormalization-group (RG) evolution for $d_\tau$, we have taken into account the RG evolutions from $\Lambda_{\text{LQ}}$ to $m_b$ [38, 44], which are known to relax the EDM bound [45]. For example, the RG evolutions provide the following corrections:

$$d_b(\mu_b) = 0.84 d_b(\Lambda_{\text{LQ}}) - 0.42 e \tilde{d}_b(\Lambda_{\text{LQ}}),$$

$$\tilde{d}_b(\mu_b) = 0.91 \tilde{d}_b(\Lambda_{\text{LQ}}),$$

(10)

(11)

with $\Lambda_{\text{LQ}} = 2 \text{TeV}$.

After integrating out the tau and bottom quark at low energy, the electron EDM is induced by the tau and bottom-quark EDMs from QED three-loop radiative corrections [46]. Furthermore, a semi-leptonic $CP$-odd operator, $(\bar{e}_l \gamma_5 e)(\bar{p} p + \bar{m} m)$, is also induced by them from QED two-loop diagrams [47, 48], which eventually mimics the electron EDM (called an equivalent electron EDM) in the experiments [49, 50]. By using a result of the improved analysis for the QED three-loop calculation [51], we obtain

$$d_e = [4.7 \times 10^{-13} + 8.8 (1 \pm 0.1) \times 10^{-12}] d_b(\mu_b) + [9.9 \times 10^{-12} + 9.2 \times 10^{-14}] d_\tau.$$  

(12)

Here, the first terms in each parenthesis come from the QED three-loop contribution, while the second terms come from the semi-leptonic $CP$-odd operator [48]. Note that the latter calculation is a result in the case of the HF$^+$ molecule system [52] (see Refs. [49, 50] for the other molecules). The dominant theoretical uncertainty comes from the semi-leptonic $CP$-odd operator induced by the bottom-quark EDM, which is estimated as 10\% [48].

By a similar but more involved process, the nucleon (neutron and proton) EDMs are induced from the bottom-quark EDM and chromo-EDM. Short-distance contributions come from the light-quark EDM and chromo-EDMs, $d_{\text{light}}^N$ and the Weinberg operator, $d_{\text{N}}^N$ [53–55], while a long-distance contribution arises from a $CP$-odd photon-gluon operator $(GG\bar{G})$, $d_{\text{N}}^{\text{FC}}$ [48]. For
After integrating out the LQ and the weak bosons, the electron, neutron, and proton EDMs are summarized in Table I. The current 90% confidence level (CL) upper limits and future prospects for electron, neutron, and proton EDMs.

For the neutron and proton EDMs, numerically we have

\[
d_N = d_N^{\text{light}} + d_N^W + d_N^{\beta_3^G^3} \quad \text{(for } N = n, p\),
\]

\[
d_n^{\text{light}} = 4.3 \times 10^{-7} d_N(\mu_b) + 4.2 \times 10^{-8} d_N(\mu_b),
\]

\[
d_p^{\text{light}} = -3.6 \times 10^{-7} e \tilde{d}_N(\mu_b) + 9.5 \times 10^{-9} d_N(\mu_b),
\]

\[
d_n^W = -5.9 \left(1 \pm 0.5\right) \times 10^{-5} e \tilde{d}_N(\mu_b),
\]

\[
d_p^W = 8.5 \left(1 \pm 0.5\right) \times 10^{-5} e \tilde{d}_N(\mu_b),
\]

\[
d_N^{\beta_3^G^3} = 7 \times 10^{-7} d_N(\mu_b) \quad \text{(for } N = n, p\).
\]

For \(d_n^{\text{light}}\), the QCD sum-rule estimate is used [50, 56–59] (where the Peccci-Quinn mechanism is assumed to suppress a \(\tilde{\theta}\) term), whose overall normalization is determined by the lattice result [60]. The light-quark EDMs are induced by the bottom-quark EDM [48] and chromo-EDM [51], while the light-quark-EDM are induced from the bottom-quark chromo-EDM [44]. For \(d_N^W\), the QCD sum-rule estimates [50, 61, 62] (see also [63]) are used. Note that although all the above terms have 10%–30% theoretical uncertainties, we suppressed them except for the leading one. For \(d_N^{\beta_3^G^3}\), the QCD sum-rule technique is also used and the numerics should be understood as an order-of-magnitude estimation [48].

It is found that the overwhelmingly dominant contribution to the nuclear EDMs comes from the Weinberg operator. Also, the theoretical uncertainty is dominated by the Weinberg operator, which is estimated as 50% [62]. Although the accuracy of the lattice calculations is currently not competitive [64–70], they will provide complementary inputs in the future. We emphasize that the predicted neutron and proton EDMs must be the same size with opposite signs [62].

The current bounds and the future prospects for the electron, neutron, and proton EDMs are summarized in Table I.

### A. \(R_{D^(*)}\)

The \(U_1\) LQ can naturally explain the \(R_{D^(*)}\) anomalies. After integrating out the LQ and the weak bosons, the effective Lagrangian is given by

\[
L_{\text{eff}} = -2\sqrt{2} G_F V_{cb} \left[1 + C_{V_L} \right] O_{V_L} + C_{S_R} O_{S_R},
\]

with

\[
O_{V_L} = (\bar{\tau} c\gamma^\mu P_L b)(\tau c\gamma_\mu P_L \nu_\tau), \quad O_{S_R} = (\tau P_R b)(\tau P_L \nu_\tau).
\]

and the Wilson coefficients (WCs) at \(\mu = \mu_b\) are

\[
C_{V_L}(\mu_b) = \frac{\eta_{V_L}}{2\sqrt{2} G_F V_{cb}} \frac{\beta_{23}^V(\beta_{33}^V)^*}{m_{U_1}^2},
\]

\[
C_{S_R}(\mu_b) = -\frac{\eta_{S_R}}{2\sqrt{2} G_F V_{cb}} \frac{\beta_{23}^S(\beta_{33}^S)^*}{m_{U_1}^2},
\]

where \(\eta_{V_L}\), and \(\eta_{S_R}\), are coefficients of the QCD corrections [81–83]. For \(\Lambda_{QCD} \approx 2-4\text{ TeV}, \eta_{V_L} \approx 1.1\) and \(\eta_{S_R} \approx 2.0\) [19]. Furthermore, assuming the simplified flavor texture in Eq. (5), these two WC can be correlated with being

\[
C_{S_R}(\mu_b) \approx -3.6 e^{-i\phi_R} C_{V_L}(\mu_b).
\]

By using the numerical formulae for \(R_{D^(*)}\) in Ref. [19], based on the heavy quark effective theory form factors [17], we show a correlation between \(R_{D^(*)}\) and the CPV phase \(\phi_R\) in Fig. 2. Since \(R_{D^(*)}\) are the CP-conserving observables, they depend on only \(\cos \phi_R\) and are invariant under \(\phi_R \leftrightarrow -\phi_R\). The black contour denotes the values of \(\phi_R\) with varying \(\beta_{23}^V/m_{U_1}\). We use \(\beta_{23}^V/m_{U_1} \approx \lambda \approx 0.225\) as a typical reference value [40].

The gray-shaded region cannot be predicted within the \(U_1\) LQ model. It is found that large \(\phi_R\) (\(\pi/3 < |\phi_R|\)) is favored to accommodate the anomalies. A CP-conserving scenario of \(\phi_R = 0\) can be excluded by the current data. One should note that the \(U_1\) LQ model also leads to deviations from the SM predictions in other \(b \to c\tau\nu\) observables, \(\tau\) polarization asymmetry and the LFU violation in \(\Lambda_b \to \Lambda_c\ell\nu\), which will be shown in Appendix A.

### B. \(B_s \to \tau^+\tau^-\)

Within the SM, \(B_s \to \tau^+\tau^-\) is suppressed by the one-loop factor and also the chirality factor, \(m_\tau^2/m_\tau^2\). On the other hand, the \(U_1\) LQ contributions are induced at
FIG. 3. The predicted neutron and proton EDMs are shown by the black contours in the left and right panels, respectively, where the solid (dashed) lines represent positive (negative) EDMs. The red (light red) region can explain the \(R_D\) anomaly at 1\(\sigma\) (2\(\sigma\)) level. The blue and green regions are excluded by the high-\(p_T\) bound and \(B_s \to \tau^+\tau^-\), respectively. The estimated sensitivities based on upcoming Run 3 data are shown by the dashed blue and green lines. We set \(m_{U_1} = 2\) TeV and \(\beta_{23}^{-\ast} = \beta_{33}^{\ast} = \lambda\).

the tree level and further the chirality suppression can be avoided. Therefore, \(B_s \to \tau^+\tau^-\) is significantly affected by the LQ. Currently, the LHCb with Run 1 data sets the upper limit on the branching ratio at 95 % CL as \([84]\)

\[
B(B_s \to \tau^+\tau^-) \leq 6.8 \times 10^{-3}.
\] (24)

The future prospect of the LHCb Run 3 has been estimated to improve the sensitivity by a factor of five \([85]\).

The \(U_1\) LQ contribution to \(B_s \to \tau^+\tau^-\) including the QCD corrections is given by \([40]\)

\[
\frac{B(B_s \to \tau^+\tau^-)}{B(B_s \to \tau^+\tau^-)_{\text{SM}}} \simeq 1 + \frac{\pi}{\sqrt{2} \alpha_G V_{tb} V_{ts}^\ast m_{U_1}^2} \beta_{L}^{33} (-0.26 \beta_{L}^{33} + 1.8 \beta_{R}^{33})^\ast + \left(1 - \frac{4m_{B_s}^2}{m_{B_s}^2} \right) \frac{1.8 \pi}{\sqrt{2} \alpha_G V_{tb} V_{ts}^\ast m_{U_1}^2} \beta_{L}^{33} (\beta_{R}^{33})^\ast.
\] (25)

It is noted that the effect from the CPV phase \(\phi_R\) is mild due to the smallness of the SM contribution.

C. LHC high-\(p_T\) bound

We employed a public tool \textsc{HighPT} \([86]\) to derive the collider constraint from \(pp \to \tau^+\tau^-\) and \(pp \to \tau\nu\) data. Currently, the dominant constraint comes from the high-\(p_T\) \(\tau\tau\) search from the ATLAS collaboration \([87]\) (see also Refs. \([88, 89]\) for the relevant study). At the CMS, an excess has been found in the high-\(p_T\) tail region \([90, 91]\). However, the ATLAS does not find excess in the region.\(^1\) On the other hand, the constraint from high-\(p_T\) mono-\(\tau\) search is currently less constraining \([93, 94]\). However, it has been pointed out that requiring an additional \(b\)-tagged jet can improve the sensitivity so that this channel is competitive with the \(\tau\tau\) channel \([95, 96]\).

D. Comment on other constraints

It is known that although loop-induced LQ contributions to \(B_s \to B_s^\ast\) mixing mixing give a severe constraint, once additional vector-like fermions are introduced in the UV complete model the constraint can be naturally avoided thanks to the GIM-like mechanism \([24, 40, 97\text{-}101]\). We emphasize that the vector-like fermions do not mix the SM right-handed fermions in the UV complete model, and the EDMs are not induced from the vector-like fermion loops \([40]\). Therefore, the EDMs provide a unique prediction of the model.

The similar sensitivity to \(B_s \to \tau^+\tau^-\) could be obtained from the measurement of \(B \to K\tau^+\tau^-\) at the Belle II \([25]\), while we omitted it since the current bound is much weaker. Although \(B^- \to \tau\nu\) is also modified in the simplified flavor texture, a moderate \(\beta_{13}^{-\ast}\) suppresses the constraint \([40]\).

\(^1\) More detailed experimental comparisons and/or statistics are necessary to conclude the difference between the CMS and ATLAS results \([92]\).
FIG. 4. The absolute values of the predicted neutron and proton EDMs are shown by the black contours in the left and right panels, respectively. Constraints from the high-$p_T$ search and $B_s \rightarrow \tau^+ \tau^-$ are represented by the blue and green regions, respectively. The gray-shaded regions are out of the model prediction. We set $m_{U_1} = 2$ TeV and $\beta_{33}^{23}/\beta_{33}^{33} = \lambda$.

IV. RESULT

In Figs. 3 and 4, we show the correlations between the predicted nucleon (neutron and proton) EDMs and the $R_{D^*}$ anomaly in the $U_1$ LQ model. Here, $m_{U_1} = 2$ TeV and $\beta_{33}^{23}/\beta_{33}^{33} = \lambda$ are taken as reference values. Black contours in Fig. 3 indicate the neutron and proton EDMs in the left and right panels, respectively, where the solid (dashed) lines represent positive (negative) EDMs. We used the central values of Eqs. (16) and (17) for the estimates of the nucleon EDMs. The blue and green regions are excluded by the high-$p_T$ bound and $B_s \rightarrow \tau^+ \tau^-$, respectively. The estimated sensitivities based on upcoming Run 3 data are shown by the dashed blue and green lines in Fig. 3. We also show the correlations on the $R_D-R_{D^*}$ plane in Fig. 4.

These figures show that some of the preferred areas are already excluded by both the high-$p_T$ bound and $B_s \rightarrow \tau^+ \tau^-$. In the allowed regions, the predicted magnitudes of the nucleon EDMs are $|d_n| < 7 \times 10^{-27}$ e cm and $|d_p| < 1 \times 10^{-26}$ e cm. Very excitingly, in the near future, several experiments will probe the neutron EDM at $O(10^{-27})$ e cm precision [73–76], and eventually $O(10^{-28})$ e cm [77]. Furthermore, two experiments are proposed that the proton EDM will be proved at $O(10^{-29})$ e cm precision [79, 80]. Therefore, we conclude that neutron and proton EDMs and their opposite signs will be a smoking-gun signal of the $U_1$ LQ model.

On the other hand, the induced electron EDM from Eq. (12) is $|d_e| < 10^{-32}$ e cm, which is a few orders away from the future prospect, but the suppressed electron EDM is also a unique prediction of this model.

V. SUMMARY AND DISCUSSION

In this Letter, we established a robust bridge between the electric dipole moments and the flavor anomaly in $B \rightarrow D^{(*)}\ell\bar{\nu}$ through the popular $SU(2)_L$-singlet vector LQ coupled primarily to third-generation fermions. In the LQ interactions, there is one $CP$-violating phase which is required to accommodate the $R_{D^*}$ anomaly, and hence $CP$-violating phenomena are inevitably predicted. We investigated various EDMs and found that neutron and proton EDMs are induced with opposite signs, and predicted magnitudes are within reach of the sensitivities of future experiments.

Correlations with other CPV phenomena, e.g., $\Delta A_{CP}(B \rightarrow X_s \gamma)$, will also be interesting and we leave them as a future work. It is known that the remaining discrepancies in $b \rightarrow s\ell^+\ell^-$ could also be solved by the $U_1$ LQ at one-loop level [100]. Going beyond the leading-log approximation is necessary for the presence of vector-like fermions, and it will also be a part of future work.

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shown on the plane of purple contours, respectively. 


LHCb Collaboration, *Test of lepton flavour universality using $B^0 \to D^{\ast-}\tau^{+}\nu_{\tau}$ decays with hadronic $\tau$ channels*, arXiv:2305.01463.


S. Iguro and R. Watanabe, *Bayesian fit analysis to full distribution data of $B \to D(\ast)\ell^\pm\nu\ell$: $|V_{cb}|$ determination and New Physics constraints*, JHEP 08 (2020) 006 [arXiv:2004.10208].


S. Iguro, T. Kitahara, and R. Watanabe, *Global fit to $b \to c\tau\bar{\nu}$ anomalies 2022 mid-autumn*, arXiv:2210.10751.

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**Appendix A: Other $b \to c\tau\bar{\nu}$ observables**

In this appendix, other related observables in $b \to c\tau\bar{\nu}$ are discussed in the simplified $U_1$ LQ model. In Fig. 5, the $\tau$ polarization asymmetries in $B \to D(\ast)\tau\bar{\nu}$, $P_D^\tau$ and $P_D^{D\ast}$ [102, 103], and the LFU violation in $\Lambda_b \to \Lambda_c\tau\bar{\nu}$, $R_{\Lambda_b} \equiv B(\Lambda_b \to \Lambda_c\tau\bar{\nu})/B(\Lambda_b \to \Lambda_c\bar{\nu})$, are shown by the green, magenta, and purple contours, respectively.

It is found that $P_D^{D\ast}$ cannot deviate from the SM prediction $P_D^{D\ast,\text{SM}} \simeq -0.50$, while $P_D^\tau$ can deviate from $P_D^{D\ast,\text{SM}} \simeq 0.33$ which will be probed by the Belle II with good accuracy [104]. On the other hand, a large value of $R_{\Lambda_b}$ is expected compared to the SM prediction, $R_{\Lambda_b,\text{SM}} \simeq 0.32$ [105]. This behavior is consistent with a sum rule prediction [106–108], and it should also be a smoking-gun signal in the LHCb [109]. Note that the $D^\ast$ longitudinal polarization ratio in $B \to D^\ast\tau\bar{\nu}$, $F_L^{D\ast}$ [102, 110], is also predicted. It is, however, found that the $U_1$ LQ effect is tiny, $\Delta F_L^{D\ast} = 0.01$ [41, 111], and it is smaller than the Belle II sensitivity [26].


[56] M. Pospelov and A. Ritz, *Neutron EDM from electric...


[90] CMS Collaboration, The search for a third-generation leptoquark coupling to a τ lepton and a b quark through single, pair and nonresonant production at √s = 13 TeV. https://cds.cern.ch/record/2815309.

[91] CMS Collaboration, Searches for additional Higgs
bosons and for vector leptoquarks in $\tau\tau$ final states in proton-proton collisions at $\sqrt{s} = 13$ TeV.


[106] M. Blanke, et al., Impact of polarization observables and $B_c \to \tau\nu$ on new physics explanations of the $b \to c\tau\nu$ anomaly, Phys. Rev. D 99 (2019) 075006 [arXiv:1811.09603].

[107] M. Blanke, et al., Addendum to “Impact of polarization observables and $B_c \to \tau\nu$ on new physics explanations of the $b \to c\tau\nu$ anomaly”, Phys. Rev. D 100 (2019) 035035 [arXiv:1905.08253].

[108] M. Fedele, et al., Impact of $\Lambda b \to \Lambda c\tau\nu$ measurement on new physics in $b \to c\nu\tau$ transitions, Phys. Rev. D 107 (2023) 055005 [arXiv:2211.14172].

[109] LHCb Collaboration, Observation of the decay $\Lambda_{b}^0 \to \Lambda_{c}^+ \tau^- \bar{\nu}_{\tau}$, Phys. Rev. Lett. 128 (2022) 191803 [arXiv:2201.03497].
