

Implications of an R-Scan for Charm Physics *

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The impact of improved measurements of the cross section for electron-positron annihilation into hadrons in the charm threshold region is discussed. Two aspects are studied in detail: i.) A significant reduction of the experimental error of the electronic width of the narrow resonances J/ψ and ψ' and of the continuum cross section from the open charm threshold up to 4.6 GeV will lead to a correspondingly improved determination of the charmed quark mass. ii) A high luminosity measurement with 24 pb^{-1} at three points and with a spacing of 2 MeV around $\sqrt{s} = 3511 \text{ MeV}$ may allow to observe the direct, resonant production of χ_{c1} .

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1. Introduction

Significant improvements in luminosity are anticipated for electron positron collisions in the low energy region, with the BES III experiment at the BEPC II collider in Beijing as characteristic example. BEPC II will cover the energy region between 2 and 4.6 GeV and is therefore specifically suited for the exploration of the charm system. Indeed, recently a lot of emphasis has been put on the study of the newly discovered charmonium resonances denoted X,Y and Z. (For discussions of recent theoretical and experimental developments see e.g. Refs. 1, 2). In this brief contribution two different aspects of charm physics will be investigated which could profit from a high luminosity scan in the charm threshold region:

i) When combined with increasingly precise measurements of the electronic widths of J/ψ and ψ' an R-scan with larger luminosity and reduced systematical error could lead to an improved determination of the charm quark mass.

ii.) Investing 24 pb^{-1} of integrated luminosity into the R-measurement at three points each, with a spacing of 2 MeV around 3.511 GeV, the direct resonant production of χ_{c1} (and perhaps even χ_{c2}), which can proceed through two virtual photons, seems within reach.

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Table 1. Experimental moments in $(\text{GeV})^{-2n}$ as defined in Eq. (1), separated according to the contributions from the narrow resonances, the charm threshold region and the continuum region above $\sqrt{s} = 4.8$ GeV. In the last column the NLO contribution from the gluon condensate is shown.

n	$\mathcal{M}_n^{\text{res}}$ $\times 10^{(n-1)}$	$\mathcal{M}_n^{\text{thresh}}$ $\times 10^{(n-1)}$	$\mathcal{M}_n^{\text{cont}}$ $\times 10^{(n-1)}$	$\mathcal{M}_n^{\text{exp}}$ $\times 10^{(n-1)}$	$\mathcal{M}_n^{\text{np(NLO)}}$ $\times 10^{(n-1)}$
1	0.1201(25)	0.0318(15)	0.0646(11)	0.2166(31)	-0.0002(5)
2	0.1176(25)	0.0178(8)	0.0144(3)	0.1497(27)	-0.0005(10)
3	0.1169(26)	0.0101(5)	0.0042(1)	0.1312(27)	-0.0008(16)
4	0.1177(27)	0.0058(3)	0.0014(0)	0.1249(27)	-0.0013(25)

Table 2. Results for $m_c(3 \text{ GeV})$ in GeV. The errors are from experiment, α_s , variation of μ and the gluon condensate.

n	$m_c(3 \text{ GeV})$	exp	α_s	μ	npNLO	total
1	0.986	0.009	0.009	0.002	0.001	0.013
2	0.975	0.006	0.014	0.005	0.002	0.016
3	0.975	0.005	0.015	0.007	0.003	0.017
4	0.999	0.003	0.009	0.031	0.003	0.032

2. Quark mass determination in N³LO

As discussed in the literature^{3,4,5,6}, moments of the charm production cross section $\sigma(e^+e^- \rightarrow c\bar{c} + X) \equiv R_c\sigma_0$ with $\sigma_0 \equiv \frac{4\pi}{3}\frac{\alpha_s^2}{s}$, allow for a fairly precise determination of the charm mass. The n -th moment of R_c , as defined through

$$\mathcal{M}_n^{\text{exp}} \equiv \int \frac{ds}{s^{n+1}} R_Q(s), \quad (1)$$

can be experimentally determined from analysis of e^+e^- data. The quark mass (defined in the \overline{MS} scheme at renormalization scale μ) is then obtained from

$$m_Q(\mu) = \frac{1}{2} \left(\frac{9Q_Q^2 \bar{C}_n}{4\mathcal{M}_n^{\text{exp}}} \right)^{1/(2n)}. \quad (2)$$

The coefficients \bar{C}_n which are required for this analysis depend on μ and the strong coupling constant and have been evaluated in three-^{7,8}, later in four-loop approximation^{9,10,11,12,13}. The corresponding NNLO and N³LO charm- and bottom-quark-mass determinations have been performed in Ref. 3 and Refs. 4, 5, 6, respectively. The moments are conveniently split into three pieces, one from the narrow resonances J/ψ and ψ' , one from the threshold for open charm production up to 4.8 GeV and one from the perturbative continuum above 4.8 GeV. Their respective contributions and the corresponding errors are shown in Table 1, the results for the quark mass $m_c(3 \text{ GeV})$ are given in Table 2. A detailed discussion of the theory uncertainty can be found in Refs. 4, 6.

The path to further improvements is evident from Tables 1 and 2. The experimental input is dominated by the electronic width Γ_e of the narrow resonances. Considering the enormous improvements in luminosity and experimental techniques during the past years, a reduction of the error on Γ_e by a factor two seems feasible¹⁴.

The planned scanning with drastically increased luminosity will, furthermore, allow for a similar reduction of the error in the threshold region¹⁵. At the same time a precise measurement at the highest accessible energies around 4.6 GeV and the comparison of the result with the prediction of perturbative QCD will strengthen the confidence in the applicability of pQCD at higher energies. Performing a combined fit for the lowest three moments, thus exploiting the information of the data in an optimal way, may lead to a further reduction of the experimental error. The reduction by a factor two of the error on $\mathcal{M}_n^{\text{exp}}$ is thus well within reach.

The choice of the strong coupling constant α_s , its central value as well as its error, is a matter of disput¹⁶. In our analysis $\alpha_s(M_Z) = 0.1189 \pm 0.0020$ has been adopted. The dependence of our result on α_s can be directly deduced from the final result

$$m_c(3 \text{ GeV}) = (986 - \frac{\alpha_s - 0.1189}{0.002} 9 \pm 10) \text{ MeV} \quad (3)$$

which had been based on the second moment. Evolving, for example, to the scale of m_H , one obtains

$$m_c(126 \text{ GeV}) = (609 - \frac{\alpha_s - 0.0189}{2} 15 \pm 6) \text{ MeV} \quad (4)$$

where the parametric α_s -dependence affecting both the evaluation of $m_c(3 \text{ GeV})$ and its evolution from $\mu = 3 \text{ GeV}$ to 126 GeV are combined. This result is evidently a critical input for predictions of the Higgs boson decay rate into $c\bar{c}$ and implies an error of 5.3% from this source. Note that this error is largely dominated by the error on the strong coupling. Adopting a more optimistic attitude¹⁷ and assuming $\alpha_s = 0.1184 \pm 0.0007$ evidently leads to a reduction down to 2.5%.

Similar considerations apply to the analysis of the bottom quark mass but are outside the scope of this presentation.

3. Direct Production of χ_{c1} and χ_{c2} at Electron-Positron colliders

3.1. Search for χ_{c1} in the scanning mode

With the forementioned high luminosity operation of BEPC in the energy region between 2 and 4.6 GeV and plans to perform a dedicated energy scan, the possibility of direct resonant production of χ_{c1} and χ_{c2} through the reaction

$$e^+e^- \rightarrow \chi_{cJ} \quad (5)$$

with $J = 1$ or 2 is within reach. This reaction, originally suggested in Ref. 18 long time ago, proceeds through two virtual photons. Its strength is characterized by the respective electronic widths, $\Gamma(\chi_{cJ} \rightarrow e^+e^-) \equiv \Gamma_J$, which were investigated in Ref. 18. (At that time this investigation was motivated by the idea¹⁹ that direct resonant production of a $J^{PC} = 1^{++}$ quarkonium state, composed of bottom or top quarks, could proceed through the axial part of the neutral current, a possibility

which seems to be out of reach.) The peak cross section for a narrow resonance, normalized to the point cross section σ_0 , is given by

$$R_{\text{peak}} \equiv \frac{\sigma_{\text{peak}}}{\sigma_0} = (2J + 1) \frac{3\pi}{2\alpha^2 \sqrt{2\pi}} \frac{\Gamma_J}{\Delta M} C_{\text{rad}}. \quad (6)$$

For the present discussion we assume a Gaussian spread cms energy spread of the center-of-mass energy with width $\Delta M = 1.5$ MeV. The factor $C_{\text{rad}} \approx (2\Delta M/M)^t \approx 0.5$ with $t = 2\frac{\alpha}{\pi}(\ln(s/m_e^2) - 1)$ arises from radiative corrections due to initial-state radiation. In numerical form

$$R_{\text{peak}} = (2J + 1) 0.0176 \frac{\Gamma_J[\text{eV}]}{\Delta M[\text{MeV}]}. \quad (7)$$

Estimates for the electronic widths Γ_J can be found in Table 2 of Ref. 18. A sizable model dependence has been observed with results for $J = 1$ varying between 0.044 eV, as nearly rigorous lower limit and 0.46 eV as optimistic choice. The results for $J = 2$ are even more uncertain and vary between 0.0023 eV and 0.027 eV. Helicity conservation leads to $\Gamma_J = 0$ for $J = 0$ up to terms of order $(m_e/M_\chi)^2$. Let us, for the moment, concentrate on $J = 1$ and use $\Gamma_1 = 0.4$ eV for the analysis and 1.5 MeV for the energy spread. In this case we find

$$R_{\text{peak}}(J = 1) \approx 0.014 \quad (8)$$

for the peak cross section on top of a continuum cross section of $R_{\text{cont}} \approx 2$. This would require the sensitivity to a variation of the cross section to exceed a relative precision of 7 permille.

As an alternative one may concentrate on a selected final state with significantly improved signal-to-background ratio, which arises from the decay chain

$$e^+e^- \rightarrow \chi_J \rightarrow J/\psi\gamma \quad (9)$$

With a branching ratio $\text{Br}(\chi_{c1} \rightarrow J/\psi\gamma) = 0.348 \pm 0.015$ this would lead to

$$R_{\text{peak}}(e^+e^- \rightarrow \chi_{c1} \rightarrow J/\psi\gamma) \approx 0.0049. \quad (10)$$

In this case the continuum background originates from the (non-resonant) radiative return to the J/ψ , which proceeds through initial state radiation. This cross section is given by ($z \equiv M_{J/\psi}^2/s$)

$$R_B = \frac{9}{\alpha} \frac{\Gamma(J/\psi \rightarrow e^+e^-)}{M_{J/\psi}} (1-z) \left[\frac{1+z^2}{(1-z)^2} \ln \frac{1+\Delta}{1-\Delta} - \Delta \right] \quad (11)$$

$$\approx \frac{9\Gamma(J/\psi \rightarrow e^+e^-)}{\alpha(M_\chi - M_{J/\psi})} \ln \frac{1+\Delta}{1-\Delta} \quad (12)$$

$$(13)$$

$$(14)$$

with $z \equiv M_{J/\psi}^2/s$ and $\Delta \equiv \cos\theta_{\text{max}}$ defining the acceptance range for the radiated photon. With $\theta_{\text{max}} = 30^\circ$ one finds $R_B = 0.045$, to be contrasted with a resonance peak value $R_{\text{peak}} = 0.0049$.

We thus arrive at a signal/background ratio of roughly 0.10 and a relatively clean final state, namely a photon plus a lepton pair with an invariant mass of the J/ψ . To finally estimate the required event rates we consider the e^+e^- and $\mu^+\mu^-$ decay modes of J/ψ with branching ratios of 6% each. This affects signal and background in the same way with a reduction factor of 0.12. The final R value for the background reaction $e^+e^- \rightarrow J/\psi\gamma$ including the the branching ratio of J/ψ into e^+e^- or $\mu^+\mu^-$ amounts to 0.0054 and corresponds to 38 picobarn. To observe a one-sigma effect at one point would require 100 events, corresponding to 2.6 pb^{-1} per point. More realistically, with 3 points and 24 pb^{-1} per point (corresponding to 3σ) one would definitely be on the safe side. (Note that these estimates are based on the optimistic assumption of $\Gamma_e = 0.4 \text{ eV}$.)

On the other hand, 24 pb^{-1} correspond to about 0.3 million hadronic events, which would give a statistical precision of better than 3.3×10^{-3} in the total cross section, to be compared to the variation of 7×10^{-3} . The total cross section measurement thus could lead to an independent confirmation of the resonance.

A more refined analysis²⁰ will exploit the difference in the angular distribution of photon and leptons from signal and background, as well as the non-vanishing relative phase of signal versus background, which could give rise to an interesting interference pattern.

3.2. Search for χ_{c1} through the radiative return

As an alternative one might consider using the radiative return (including small angle photon emission) from one fixed energy point where a large amount of luminosity has been collected. For a case study let us take $E_{\text{cm}} = 3.770 \text{ GeV}$. The R -value for the production of a narrow resonance with mass M and electronic width Γ_e plus a photon emitted at arbitrary angle is given by

$$R = \frac{9 \Gamma_e}{\alpha M} \frac{1+z^2}{(1-z)} (L-1) \quad (15)$$

For $M = 3.511 \text{ GeV}$ and $\Gamma_e = 0.4 \text{ eV}$ as before one finds $R_{\chi\gamma} = 7.8 \times 10^{-6}$, corresponding to $\sigma_{\chi\gamma} = 190 \text{ fb}^{-1}$. Assuming, furthermore, an integrated luminosity of 3 fb^{-1} , one arrives at 23 events in the $\gamma\gamma\mu^+\mu^-$ or e^+e^- configuration where the invariant mass of the lepton pair plus one of the photons is given by the mass of the χ_1 state. It remains to be seen if the energy resolution is sufficient to distinguish this signal from the non-resonant background $e^+e^- \rightarrow \gamma\gamma J/\psi \rightarrow \gamma\gamma\mu^+\mu^-$ or e^+e^- .

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