

Light-Cone Distribution Amplitudes for Non-Relativistic Bound States

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Abstract. We calculate light-cone distribution amplitudes for non-relativistic bound states, including radiative corrections from relativistic gluon exchange to first order in the strong coupling constant. Our results apply to hard exclusive reactions with non-relativistic bound states in the QCD factorization approach like, for instance, $B_c \rightarrow \eta_c \ell \nu$ or $e^+ e^- \rightarrow J/\psi \eta_c$. They also serve as a toy model for light-cone distribution amplitudes of light mesons or heavy B and D mesons.

Keywords: QCD, Non-relativistic approximation, Light-cone distribution amplitudes

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INTRODUCTION

Exclusive hadron reactions with large momentum transfer involve strong interaction dynamics at very different momentum scales. In cases where the hard-scattering process is dominated by light-like distances, the long-distance hadronic information is given in terms of so-called light-cone distribution amplitudes (LCDAs) which are defined from hadron-to-vacuum matrix elements of non-local operators with quark and gluon field operators separated along the light-cone. Representing universal hadronic properties, LCDAs can either be extracted from experimental data, or they have to be constrained by non-perturbative methods. The most extensively studied and probably best understood case is the leading-twist pion LCDA, for which experimental constraints from the $\pi - \gamma$ transition form factor [1], as well as estimates for the lowest moments from QCD sum rules [2, 3, 4] and lattice QCD [5] exist. On the other hand, our knowledge on LCDAs for heavy B mesons [6, 7, 8], and even more so for heavy quarkonia [9, 10], had been relatively poor until recently.

The situation becomes somewhat simpler, if the hadron under consideration can be approximated as a non-relativistic bound state of two sufficiently heavy quarks. In this case we expect exclusive matrix elements – like transition form factors [11] and, in particular, the LCDAs – to be calculable perturbatively, since the quark masses provide an intrinsic physical infrared regulator. In these proceedings we report about results from [12], where we have calculated the LCDAs for non-relativistic meson bound states including relativistic QCD corrections to first order in the strong coupling constant at the non-relativistic matching scale which is set by the mass of the lighter quark in the hadron.

LIGHT-CONE DISTRIBUTION AMPLITUDES

The wave function for a non-relativistic (NR) bound state of a quark and an antiquark can be obtained from the solution of the Schrödinger equation with the QCD Coulomb potential. To first approximation it describes a quark with momentum $m_1 v_\mu$ and an antiquark with momentum $m_2 v_\mu$, where v_μ is the four-velocity of the meson. The spinor degrees of freedom for a non-relativistic pseudoscalar bound state are represented by the Dirac projector $\frac{1}{2}(1 + \not{v})\gamma_5$. The non-relativistic approximation can also serve as a toy model for bound states of light (relativistic) quarks. We will in the following refer to “heavy mesons” as “ B ” (where we mean the realistic example of a B_c meson, or the toy model for a B_q meson, with $m_1 \gg m_2$) and “light mesons” as “ π ” (where the realistic example is η_c , and the toy-model application would be the pion, with $m_1 \approx m_2$).

Definition of LCDAs for light pseudoscalar mesons

Following [13, 2] we define the 2-particle LCDAs of a light pseudoscalar meson via

$$\begin{aligned} \langle \pi(P) | \bar{q}_1(y) \gamma_\mu \gamma_5 q_2(x) | 0 \rangle &= -i f_\pi \int_0^1 du e^{i(u p \cdot y + \bar{u} p \cdot x)} \left[p_\mu \phi_\pi(u) + \frac{m_\pi^2}{2 p \cdot z} z_\mu g_\pi(u) \right], \\ \langle \pi(P) | \bar{q}_1(y) i \gamma_5 q_2(x) | 0 \rangle &= f_\pi \mu_\pi \int_0^1 du e^{i(u p \cdot y + \bar{u} p \cdot x)} \phi_p(u), \\ \langle \pi(P) | \bar{q}_1(y) \sigma_{\mu\nu} \gamma_5 q_2(x) | 0 \rangle &= i f_\pi \tilde{\mu}_\pi (p_\mu z_\nu - p_\nu z_\mu) \int_0^1 du e^{i(u p \cdot y + \bar{u} p \cdot x)} \frac{\phi_\sigma(u)}{2D-2} \end{aligned} \quad (1)$$

with two light-like vectors $z_\mu = y_\mu - x_\mu$ and $p_\mu = P_\mu - m_\pi^2 / (2P \cdot z) z_\mu$, with the usual gauge link factor $[y, x]$ (Wilson line) understood implicitly. Here $u = 1 - \bar{u}$ denotes the light-cone momentum fraction of the quark in the pion, with $\phi_\pi(u)$ being the twist-2 LCDA, while $\phi_p(u)$ and $\phi_\sigma(u)$ are of twist-3. For completeness, we have also quoted the twist-4 LCDA $g_\pi(u)$ which, like the 3-particle LCDAs, will not be considered further. All LCDAs are normalized to 1, such that the prefactors in (1) are defined in the local limit $x \rightarrow y$. In the definition of $\phi_\sigma(u)$, we have included a factor $3/(D-1)$, such that the relation between μ_π and $\tilde{\mu}_\pi$ from the equations of motion (eom),

$$\tilde{\mu}_\pi = \mu_\pi - (m_1 + m_2), \quad (2)$$

is maintained in $D \neq 4$ dimensions. In the local limit the eom further imply

$$\mu_\pi = \frac{m_\pi^2}{m_1 + m_2}, \quad \int_0^1 du u \phi_p(u) = \frac{1}{2} + \frac{m_1 - m_2}{2\mu_\pi}. \quad (3)$$

Notice that (2,3) hold for the *bare* parameters and distribution amplitudes.

At tree level, and in leading order of the expansion in the non-relativistic velocities, the two quarks in the non-relativistic wave function simply share the momentum of the meson according to their masses, $p_i^\mu \simeq m_i / (m_1 + m_2) P^\mu$. For “light mesons” this implies

$$\phi_\pi(u) \simeq \phi_p(u) \simeq g_\pi(u) \simeq \delta(u - u_0), \quad (4)$$

where $u_0 = m_1/(m_1 + m_2)$. Consequently, all positive and negative moments of the distribution amplitudes are simply given in terms of the corresponding power of u_0 . Notice that $\tilde{\mu}_\pi \simeq 0$ at tree-level, and the corresponding LCDA $\phi_\sigma(u)$ can only be determined by considering the corresponding one-loop expressions (see [12]).

Definition of LCDAs for heavy pseudoscalar mesons

We define the 2-particle LCDAs of a heavy pseudoscalar B meson following [6, 14],

$$\langle 0 | \bar{q}^\beta(z) h_v^\alpha(0) | B(v) \rangle = -\frac{i\hat{f}_B(\mu)M}{4} \left[\frac{1+\not{v}}{2} \left\{ 2\tilde{\phi}_B^+(t) + \frac{\tilde{\phi}_B^-(t) - \tilde{\phi}_B^+(t)}{t} \not{z} \right\} \gamma_5 \right]^{\alpha\beta}, \quad (5)$$

where v^μ is the heavy meson's velocity, $t \equiv v \cdot z$ and $z^2 = 0$. Here \hat{f}_B is the (renormalization-scale dependent) decay constant in HQET. The Fourier-transformed expressions, which usually appear in factorization formulas, are given through

$$\tilde{\phi}_B^\pm(t) = \int_0^\infty d\omega e^{-i\omega t} \phi_B^\pm(\omega), \quad (6)$$

where ω denotes the light-cone energy of the light quark in the B meson rest frame.

Including a finite spectator quark mass m and the effect of the 3-particle LCDAs Ψ_A, Ψ_V as defined in [15], the eom become

$$\begin{aligned} & \omega \phi_B^-(\omega) - m \phi_B^+(\omega) + \frac{D-2}{2} \int_0^\omega d\eta [\phi_B^+(\eta) - \phi_B^-(\eta)] \\ & = (D-2) \int_0^\omega d\eta \int_{\omega-\eta}^\infty \frac{d\xi}{\xi} \frac{\partial}{\partial \xi} [\Psi_A(\eta, \xi) - \Psi_V(\eta, \xi)], \end{aligned} \quad (7)$$

which is trivially fulfilled at tree-level, where $\phi_B^+(\omega) \simeq \phi_B^-(\omega) \simeq \delta(\omega - m)$, and $\Psi_{V,A}(\eta, \xi) = \mathcal{O}(\alpha_s)$. We have shown in [12] that this relation also holds after including α_s corrections to the NR limit. (A second relation, which has been presented in [15] and extended here to the case $m \neq 0$, is found to be not valid beyond tree-level.) Moreover, at tree level, the moments of the ‘‘heavy meson’s’’ LCDAs can be related to matrix elements of local operators in HQET [6].

RELATIVISTIC CORRECTIONS AT ONE-LOOP

The NR bound states are described by parton configurations with fixed momenta. Relativistic gluon exchange as in Fig. 1 leads to modifications: First, there is a correction from matching QCD (or, in the case of heavy mesons, the corresponding low-energy effective theory HQET) on the NR theory,

$$\phi_M = \phi_M^{(0)} + \frac{\alpha_s C_F}{4\pi} \phi_M^{(1)} + \mathcal{O}(\alpha_s^2). \quad (8)$$

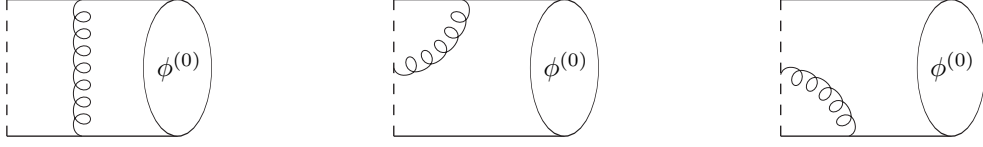


FIGURE 1. *Relativistic corrections to the light-cone distribution amplitudes. The dashed line indicates the Wilson line in the definition of the LCDAs.*

Secondly, there is the usual evolution under the change of the renormalization scale [16, 7]. In particular, the support region for the parton momenta is extended to $0 \leq u \leq 1$ for light mesons and $0 \leq \omega < \infty$ for heavy mesons, respectively.

Light mesons

We first consider the leading-order relativistic corrections to the local matrix elements. We will focus on the case of equal quark masses (results for $m_1 \neq m_2$ can be found in [12]). Our result for the decay constant,

$$f_\pi = f_\pi^{\text{NR}} \left[1 - 6 \frac{\alpha_s C_F}{4\pi} + \mathcal{O}(\alpha_s^2) \right], \quad (9)$$

is in agreement with [17], and the result for μ_π and $\tilde{\mu}_\pi$ is consistent with the eom-constraint in (2,3), using $m_\pi \simeq m_1^{\text{OS}} + m_2^{\text{OS}}$ in the on-shell scheme.

The remaining contributions to the NLO correction to the leading-twist LCDA contain an UV-divergent piece,

$$\phi_\pi^{(1)}(u)|_{\text{div.}} = \frac{2}{\varepsilon} \int_0^1 dv V(u, v) \phi^{(0)}(v), \quad (10)$$

which involves the well-known Efremov-Radyushkin-Brodsky-Lepage (ERBL) evolution kernel [16], and a finite term,

$$\begin{aligned} \phi_\pi^{(1)}(u; \mu) = & 4 \left\{ \left(\ln \frac{\mu^2}{m_\pi^2 (1/2 - u)^2} - 1 \right) \left[\left(1 + \frac{1}{1/2 - u} \right) u \theta(1/2 - u) + (u \leftrightarrow \bar{u}) \right] \right\}_+ \\ & + 4 \left\{ \frac{u(1-u)}{(1/2 - u)^2} \right\}_{++}. \end{aligned} \quad (11)$$

Here the plus-distributions are defined as

$$\begin{aligned} \int_0^1 du \{ \dots \}_+ f(u) & \equiv \int_0^1 du \{ \dots \} \left(f(u) - f(1/2) \right), \\ \int_0^1 du \{ \dots \}_{++} f(u) & \equiv \int_0^1 du \{ \dots \} \left(f(u) - f(1/2) - f'(1/2)(u - 1/2) \right). \end{aligned} \quad (12)$$

TABLE 1. Convergence of $\langle \xi^n \rangle_\pi$ moments ($\eta = \alpha_s(\mu)/\alpha_s(m)$).

n	2	4	6	8	10
NLO ($\mu = m$, in units of α_s)	0.333	0.053	0.019	0.009	0.005
LL ($\eta = 1/5$)	0.126	0.048	0.025	0.015	0.010
LL ($\eta = 1/25$)	0.173	0.070	0.038	0.024	0.016
asymptotic	0.200	0.086	0.048	0.030	0.021

An independent calculation of the leading-twist LCDAs for the η_c and J/ψ meson has been presented in [9]. Our result is not in complete agreement with their findings. In particular, we find that the LCDA quoted in [9] is not normalized to unity as it should be.

At the non-relativistic scale, $\mu \simeq m$, the usual expansion of $\phi_\pi(u)$ into Gegenbauer polynomials (the eigenfunctions of the leading-order ERBL evolution equations), does not converge very well, i.e. the Gegenbauer coefficients a_n drop off slower than $1/n$. A better characterization of the LCDAs at NLO is given in terms of the moments

$$\langle \xi^n \rangle_\pi \equiv \int_0^1 du (2u-1)^n \phi_\pi(u), \quad (13)$$

which are linear combinations of Gegenbauer coefficients of order $\leq n$. This corresponds to an expansion in terms of δ -function and its derivatives,

$$\phi_\pi(u) = 2 \sum_n \langle \xi^n \rangle_\pi \frac{(-1)^n}{n!} \delta^{(n)}(2u-1). \quad (14)$$

Results for the first few moments $\langle \xi^n \rangle_\pi$ are shown in Table 1. (Notice that the moments $\langle \xi^n \rangle_\pi$ also receive corrections from sub-leading terms in the non-relativistic expansion, see [10].)

Table 1 also contains the moments generated by ERBL evolution of the LO result (4) for two values of $\eta = \alpha_s(\mu)/\alpha_s(m)$ and in the asymptotic limit. To illustrate the change of the shape of $\phi_\pi(u)$ under evolution, we employ a parametrization which is obtained from a slight modification of the strategy developed in [18],

$$\phi_\pi(u) \equiv \frac{3u\bar{u}}{\Gamma[a, -\ln t_c]} \int_0^{t_c} dt (-\ln t)^{a-1} \left(f(2u-1, it^{1/b}) + f(2u-1, -it^{1/b}) \right). \quad (15)$$

It involves three real parameters $a > 0$, $b > 0$, $t_c \leq 1$, which can be fitted to the first three moments $\langle \xi^{2,4,6} \rangle$, and the generating function for the Gegenbauer polynomials,

$$f(\xi, \theta) = \frac{1}{(1 - 2\xi\theta + \theta^2)^{3/2}} = \sum_{n=0}^{\infty} C_n^{3/2}(\xi) \theta^n. \quad (16)$$

Fig. 2(a) shows the evolution of the model LCDA as a function of u . For $\eta = 1/5$ the functional form still “remembers” the non-relativistic profile, while for $\eta = 1/25$ the LCDA gets close to the asymptotic form.

The twist-3 LCDAs for the 2-particle Fock states are obtained in the same way as the twist-2 one. Details can be found in [12]. In particular, all our results are in manifest agreement with the eom-constraint from (3).

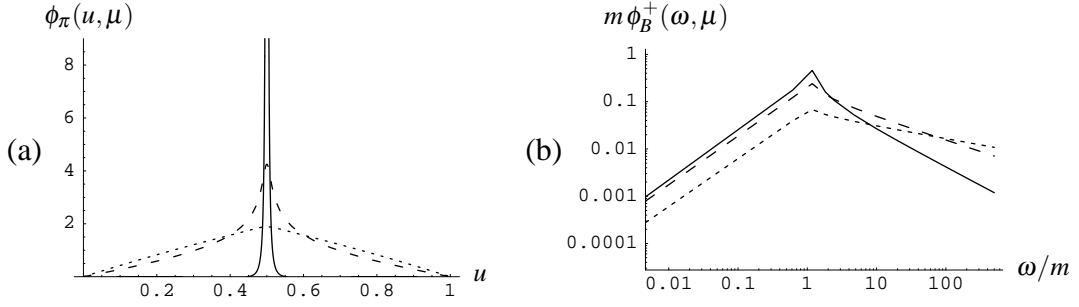


FIGURE 2. (a) Solid line: approximation for $\phi_\pi(u) = \delta(u - 1/2)$ in terms of the parametrization (15), and its evolution for $\eta = 1/5$ (dashed line) and $\eta = 1/25$ (dotted line). (b) Evolution of the heavy-meson LCDA $\phi_B^+(\omega) = \delta(\omega - m)$. The three curves (solid, long-dashed, short-dashed) correspond to $\eta = 1/2, 1/5, 1/10$.

Heavy mesons

The calculation of the LCDA for a heavy meson goes along the same lines as for the light-meson case. However, important differences arise because the heavier quark is to be treated in HQET which modifies the divergence structure of the loop integrals. As a consequence, the evolution equations for the LCDA of heavy mesons [7] differ from those of light mesons.

Let us focus on the distribution amplitude $\phi_B^+(\omega)$ which enters the QCD factorization formulas for exclusive heavy-to-light decays. In the local limit we derive the corrections from soft gluon exchange to the decay constant in HQET,

$$\hat{f}_M(\mu) = f_M^{\text{NR}} \left[1 + \frac{\alpha_s C_F}{4\pi} \left(3 \ln \frac{\mu}{m} - 4 \right) + \mathcal{O}(\alpha_s^2) \right]. \quad (17)$$

Notice that the decay constant of a heavy meson exhibits the well-known scale dependence [19]. The remaining NLO corrections to the distribution amplitude $\phi_B^+(\omega)$ contain an UV-divergent piece, which involves the Lange-Neubert evolution kernel $\gamma_+(\omega, \omega', \mu)$ [7]. As has been shown by Lee and Neubert [20], the solution of the evolution equation can be written in closed form. The resulting evolution of $\phi_B^+(\omega, \mu)$ is illustrated in Fig. 2(b), starting from $\delta(\omega - m)$ at the non-relativistic scale, for three different values of $\eta = \alpha_s(\mu)/\alpha_s(m)$ and taking $\alpha_s(m) = 1$. From the double-logarithmic plot we can read off the asymptotic behaviour of the LCDA for $\omega \rightarrow 0$ and $\omega \rightarrow \infty$. As argued on general grounds [7], $\phi_B^+(\omega)$ develops a linear behaviour for $\omega \rightarrow 0$, whereas for $\omega \rightarrow \infty$ the evolution generates a radiative tail which tends to fall off slower than $1/\omega$ at higher scales.

The finite NLO correction to $\phi_B^+(\omega)$ reads

$$\begin{aligned} \frac{\phi_B^{(+,1)}(\omega; \mu)}{\omega} &= 2 \left[\left(\ln \left[\frac{\mu^2}{(\omega - m)^2} \right] - 1 \right) \left(\frac{\theta(m - \omega)}{m(m - \omega)} + \frac{\theta(\omega - m)}{\omega(\omega - m)} \right) \right]_+ \\ &+ 4 \left[\frac{\theta(2m - \omega)}{(\omega - m)^2} \right]_{++} + \frac{4\theta(\omega - 2m)}{(\omega - m)^2} - \frac{\delta(\omega - m)}{m} \left(\frac{1}{2} \ln^2 \frac{\mu^2}{m^2} - \ln \frac{\mu^2}{m^2} + \frac{3\pi^2}{4} + 2 \right) \end{aligned} \quad (18)$$

with an analogous definition of plus-distributions as in (12). In contrast to the light-meson case, the normalization of the heavy meson distribution amplitude is ill-defined. Imposing a hard cutoff $\Lambda_{UV} \gg m$ and expanding to first order in m/Λ_{UV} , we derive

$$\int_0^{\Lambda_{UV}} d\omega \phi_B^+(\omega; \mu) \simeq 1 - \frac{\alpha_s C_F}{4\pi} \left[\frac{1}{2} \ln^2 \frac{\mu^2}{\Lambda_{UV}^2} + \ln \frac{\mu^2}{\Lambda_{UV}^2} + \frac{\pi^2}{12} \right] + \dots \quad (19)$$

$$\int_0^{\Lambda_{UV}} d\omega \omega \phi_B^+(\omega; \mu) \simeq \frac{\alpha_s C_F}{4\pi} \left[2 \ln \frac{\mu^2}{\Lambda_{UV}^2} + 6 \right] \Lambda_{UV} + \dots \quad (20)$$

The last two expressions provide model-independent properties of the distribution amplitude which agree with the general results in [20]. The two phenomenologically relevant moments in the factorization approach to heavy-to-light decays read

$$\begin{aligned} \lambda_B^{-1}(\mu) &\equiv \int_0^\infty d\omega \frac{\phi_B^+(\omega; \mu)}{\omega} = \frac{1}{m} \left(1 - \frac{\alpha_s C_F}{4\pi} \left[\frac{1}{2} \ln^2 \frac{\mu^2}{m^2} - \ln \frac{\mu^2}{m^2} + \frac{3\pi^2}{4} - 2 \right] \right), \\ \sigma_B(\mu) &\equiv \lambda_B(\mu) \int_0^\infty d\omega \frac{\phi_B^+(\omega; \mu)}{\omega} \ln \frac{\mu}{\omega} = \ln \frac{\mu}{m} + \frac{\alpha_s C_F}{4\pi} [8\zeta(3)]. \end{aligned} \quad (21)$$

A similar analysis can be performed for the LCDA $\phi_B^-(\omega)$, for details we refer to [12]. In particular, we can read off the anomalous dimension,

$$\begin{aligned} \gamma_-^{(1)}(\omega, \omega'; \mu) &= \left(4 \ln \frac{\mu}{\omega} - 2 \right) \delta(\omega - \omega') - 4 \frac{\theta(\omega' - \omega)}{\omega'} \\ &- 4 \omega \left[\frac{\theta(\omega' - \omega)}{\omega'(\omega' - \omega)} \right]_+ - 4 \omega \left[\frac{\theta(\omega - \omega')}{\omega(\omega - \omega')} \right]_+, \end{aligned} \quad (22)$$

which describes the evolution of $\phi_B^-(\omega, \mu)$ in the Wandzura-Wilczek approximation, where 3-particle LCDAs (and the light quark mass m) are neglected. Among others, γ_- is needed to show the factorization of correlation functions in SCET sum rules for heavy-to-light form factors [21]. Another new result are the first positive moments of $\phi_B^-(\omega)$ as a function of the UV cutoff,

$$\int_0^{\Lambda_{UV}} d\omega \phi_B^-(\omega; \mu) \simeq 1 - \frac{\alpha_s C_F}{4\pi} \left[\frac{1}{2} \ln^2 \frac{\mu^2}{\Lambda_{UV}^2} - \ln \frac{\mu^2}{\Lambda_{UV}^2} + \frac{\pi^2}{12} \right] + \dots \quad (23)$$

$$\int_0^{\Lambda_{UV}} d\omega \omega \phi_B^-(\omega; \mu) \simeq \frac{\alpha_s C_F}{4\pi} \left[2 \ln \frac{\mu^2}{\Lambda_{UV}^2} + 2 \right] \Lambda_{UV} + \dots \quad (24)$$

where the divergent pieces again are expected to be model-independent.

SUMMARY

Non-relativistic $q\bar{q}$ bound states have been used as a starting point to construct light-cone distribution amplitudes in QCD and in HQET. We considered relativistic gluon corrections at NLO in the strong coupling at the non-relativistic scale, as well as the leading logarithmic evolution towards higher scales needed in QCD factorization theorems. We also studied certain model-independent properties of light and heavy LCDAs, including new results for the LCDA $\phi_-^B(\omega, \mu)$ in HQET.

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